

## DIAGNOSING READINESS

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1. 1, 2, 3, 4, 6, 12 2. 1, 2, 4, 7, 8, 14, 28, 56 3. 1, 31  
 4. 1, 3, 9, 27 5. 1, 2, 5, 10, 11, 22, 55, 110 6. 1, 5, 13, 65  
 7. 1, 2, 5, 10, 25, 50 8. 1, 2, 4, 5, 8, 10, 20, 25, 40, 50, 100,  
 200 9. 1, 11 10. 1, 2, 3, 6, 7, 14, 21, 42 11. 1, 2, 3, 6, 11, 22,  
 33, 66 12. 1, 73 13.  $2x^2 - x + x^2 - 3x = 3x^2 - 4x$   
 14.  $-b + 2 + 3b + 4 = (-1 + 3)b + 2 + 4 = 2b + 6$   
 15.  $-5y - y^2 + 4y^2 - 6y = (4 - 1)y^2 - (5 + 6)y =$   
 $3y^2 - 11y$  16.  $(3w - 2w^2 + 4w - 2w^2) \frac{1}{6} =$   
 $-(2 - 2)w^2 + (3 + 4)w \frac{1}{6} = (-4w^2 + 7w) \frac{1}{6} =$   
 $-\frac{4}{6}w^2 + \frac{7}{6}w = -\frac{2}{3}w^2 + \frac{7}{6}w$  17.  $-8(z + 2) + 5(3z - 10) =$   
 $-8z - 16 + 15z - 50 = 7z - 66$   
 18.  $2(x + 4x^2 - 2x - 2x^2) = 2(2x^2 - x) = 2(2x^2) - 2(x) =$   
 $4x^2 - 2x$  19.  $12t - 5t^2 - 2t - t^2 = -6t^2 + 10t$   
 20.  $p - 3 - (p^2 - 3) = -p^2 + p$  21.  $(7w)^2 = 7^2w^2 =$   
 $49w^2$  22.  $(-5n^2)(-5n) = 25n^{2+1} = 25n^3$  23.  $(3z^2)^2 =$   
 $3^2(z^2)^2 = 9z^{2+2} = 9z^4$  24.  $(2t^3)(5t^4) = 10t^{3+4} = 10t^7$   
 25.  $(4y^3)^2 = 4^2y^{3+2} = 16y^6$  26.  $(-9ab)^2 = (-9)^2a^2b^2 =$   
 $81a^2b^2$  27.  $4(x^2)^2 = 4x^{2+2} = 4x^4$  28.  $(-6p^4)^2 =$   
 $(-6)^2p^{4+2} = 36p^8$  29.  $\frac{x^5y^8}{x^3y^4} = x^{5-3}y^{8-4} = x^2y^4$   
 30.  $\frac{(3c)^2}{(3c)} = \frac{9c^2}{3c} = 3c$  31.  $\frac{-5t}{(10t^3)(2t)} = \frac{-5t}{20t^4} = -\frac{1}{4t^{4-1}} = -\frac{1}{4t^3}$   
 32.  $\frac{(3a)(4a^3)}{6a^2} = 2a^{1+3-2} = 2a^2$

## 9-1 Adding and Subtracting Polynomials

pages 456–461

**Check Skills You'll Need p. 456** For complete solutions see *Daily Skills Check and Lesson Quiz Transparencies or Presentation Pro CD-ROM*.

1.  $19t$  2.  $39g$  3.  $-8k$  4.  $11b - 6$  5.  $-3n^2$  6.  $7x^2$

**Investigation** 1. B; Casic bought  $s$  bags of birdseed and  $m$  bags of millet. 2. Davis:  $24m$ ; Brooks:  $3.99s + 2c$ ; Martino:  $3.99s + 2.29g + 1.89p$  3.  $3.99 \cdot 10 + 2.29 \cdot 4 + 1.89 \cdot 2 = 39.90 + 9.16 + 3.78 = 52.84$ ; \$52.84

**Check Understanding** 1.  $9x^0 = 9$ ; degree is 0 (the power of  $x$ ); the degree of a nonzero constant is zero. 2a.  $-9x^4 + 6x^2 + 7$ ; fourth-degree trinomial 2b.  $-y^3 + 3y - 4$ ; cubic trinomial 2c.  $-4v + 8$ ; linear binomial

3a.

$$\begin{array}{r} 12m^2 + 4 \\ + 8m^2 + 5 \\ \hline 20m^2 + 9 \end{array}$$

3b.  $(t^2 - 6) + (3t^2 + 11) = (t^2 + 3t^2) + (-6 + 11) = 4t^2 + 5$  3c.  $(9w^3 + 8w^2) + (7w^3 + 4) = (9 + 7)w^3 + 8w^2 + 4 = 16w^3 + 8w^2 + 4$

- 4a.
- $$\begin{array}{r} v^3 + 6v^2 - v \\ - 9v^3 - 7v^2 + 3v \\ \hline -8v^3 + 13v^2 - 4v \end{array}$$
- 4b.  $(30d^3 - 29d^2 - 3d) - (2d^3 + d^2) =$   
 $(30 - 2)d^3 + (-29 - 1)d^2 - 3d =$   
 $28d^3 - 30d^2 - 3d$  4c.  $(4x^2 + 5x + 1) - (6x^2 + x + 8) =$   
 $(4 - 6)x^2 + (5 - 1)x + (1 - 8) = -2x^2 + 4x - 7$
- Exercises** 1. 1 2. 3 3. 0 4. 2 + 8 = 10 5. 1 + 3 = 4 6. 0  
 7. 4 8. 0 9. quadratic trinomial 10. linear binomial  
 11. cubic trinomial 12. not a polynomial 13. constant monomial 14. quadratic binomial 15.  $4x - 3x^2 = -3x^2 + 4x$ ; quadratic binomial 16.  $4x + 9$ ; linear binomial 17.  $c^2 - 2 + 4c = c^2 + 4c - 2$ ; quadratic trinomial 18.  $9z^2 - 11z^2 + 5z - 5 = -2z^2 + 5z - 5$ ; quadratic trinomial 19.  $y - 7y^3 + 15y^8 = 15y^8 - 7y^3 + y$ ; eighth-degree trinomial 20.  $-10 + 4q^4 - 8q + 3q^2 = 4q^4 + 3q^2 - 8q - 10$ ; fourth-degree polynomial with 4 terms
21.  $5m^2 + 9$
- $$\begin{array}{r} + 3m^2 + 6 \\ \hline 8m^2 + 15 \end{array}$$
22.  $3k - 8$
- $$\begin{array}{r} + 7k + 12 \\ \hline 10k + 4 \end{array}$$
23.  $w^2 + w - 4$
- $$\begin{array}{r} + 7w^2 - 4w + 8 \\ \hline 8w^2 - 3w + 4 \end{array}$$
24.  $8x^2 + 1$
- $$\begin{array}{r} + 12x^2 + 6 \\ \hline 20x^2 + 7 \end{array}$$
25.  $(g^4 + 4g) + (9g^4 + 7g) = (1 + 9)g^4 + (4 + 7)g = 10g^4 + 11g$  26.  $(a^2 + a + 1) + (5a^2 - 8a + 20) = (1 + 5)a^2 + (1 - 8)a + (1 + 20) = 6a^2 - 7a + 21$
27.  $7y^3 - 3y^2 + 4y$
- $$\begin{array}{r} + 8y^4 + 3y^2 \\ \hline 8y^4 + 7y^3 + 4y \end{array}$$
28.  $6c - 5 - (4c + 9) = 6c - 5 - 4c - 9 = (6c - 4c) + (-5 - 9) = 2c - 14$
29.  $2b + 6 - (b + 5) = 2b + 6 - b - 5 = (2b - b) + (6 - 5) = b + 1$
30.  $7h^2 + 4h - 8 - 3h^2 + 2h - 10 = (7h^2 - 3h^2) + (4h + 2h) + (-8 - 10) = 4h^2 + 6h - 18$
31.  $(17n^4 + 2n^3) - (10n^4 + n^3) = (17 - 10)n^4 + (2 - 1)n^3 = 7n^4 + n^3$
32.  $(24x^5 + 12x) - (9x^5 + 11x) = (24 - 9)x^5 + (12 - 11)x = 15x^5 + x$
33.  $(6w^2 - 3w + 1) - (w^2 + w - 9) = (6 - 1)w^2 - (3 + 1)w + (1 + 9) = 5w^2 - 4w + 10$
34.  $(-5x^4 + x^2) - (x^3 + 8x^2 - x) = -5x^4 - x^3 - 7x^2 + x$
35.  $(7y^2 - 3y + 4y) + (8y^2 + 3y^2 + 4y) = (7 + 8 + 3)y^2 + (-3 + 4 + 4)y = 18y^2 + 5y$
36.  $(2x^3 - 5x^2 - 1) - (8x^3 + 3 - 8x^2) = -6x^3 + 3x^2 - 4$  37.  $(-7z^3 + 3z - 1) - (-6z^2 + z + 4) = -7z^3 + 6z^2 + 2z - 5$

38.  $(7a^3 - a + 3a^2) + (8a^2 - 3a - 4) =$   
 $7a^3 + 11a^2 - 4a - 4$  39.  $2(9c - 10) + 2(5c + 2) =$   
 $(18 + 10)c + (-20 + 4) = 28c - 16$   
40.  $9x + (8x - 2) + (17x - 6) + (5x + 1) =$   
 $(9 + 8 + 17 + 5)x + (-2 - 6 + 1) = 39x - 7$   
41. Kwan wrote  $-(-4x - 2) = -4x - 2$ ; correct result  
is  $-(-4x - 2) = 4x + 2$ . 42a. *monogram*: several  
letters combined to form a single (*mono-*) design  
(*gram*); *binocular*: relating to the use of both (two, *bi-*)  
eyes (*oculus*); *tricuspid*: having three cusps (high  
points), as of a molar tooth; *polyglot*: a person with  
knowledge of several (*poly-*) languages 42b. Answers  
may vary. Samples: monopoly, biathlon, tripod,  
polychrome 42c. Yes; the prefixes are used to identify  
the number of terms in a polynomial.

43.  $(x^3 + 3x) + (12x - x^4) = -x^4 + x^3 + 15x$

44.  $(6g - 7g^8) - (4g + 2g^3 + 11g^2) =$   
 $-7g^8 - 2g^3 - 11g^2 + 2g$

45.  $(2h^4 - 5h^9) - (-8h^5 + h^{10}) =$   
 $-h^{10} - 5h^9 + 8h^5 + 2h^4$

46.  $(-4t^4 - 9t + 6) + (13t + 5t^4) = t^4 + 4t + 6$

47.  $(8b - 6b^7 + 3b^8) + (2b^7 - 5b^9) =$   
 $-5b^9 + 3b^8 - 4b^7 + 8b$

48.  $(11 + k^3 - 6k^4) - (k^2 - k^4) =$   
 $-5k^4 + k^3 - k^2 + 11$  49. Perimeter =  
 $5x + 2 + 5x - 4 + 6x - 8 + ax + b + 4x =$   
 $(20 + a)x - 10 + b = 25x + 8$ ;

20 + a = 25

a = 5

-10 + b = 8

b = 18

Missing length is  $ax + b = 5x + 18$ .

50. Perimeter =  $xa + y + 8a - 9 + 6a + 8 =$   
 $(14 + x)a - 1 + y = 23a - 7$ ;

14 + x = 23

x = 9

-1 + y = -7

y = -6

Missing length is  $xa + y = 9a - 6$ .

51. No; both terms of a binomial cannot be constants.

52a. P:  $y = 2x - 1$ ; Q:  $y = 0.5x + 3$

52b.  $D(x) = y_P - y_Q = 2x - 1 - (0.5x + 3) = 1.5x - 4$

52c. D = 0 for  $1.5x - 4 = 0$ ;  $1.5x = 4$ ;  $x = \frac{4}{1.5} = \frac{8}{3} = 2\frac{2}{3}$

52d. The lines intersect at  $x = 2\frac{2}{3}$ .

53.  $(ab^2 + ba^3) + (4a^3b - ab^2 - 5ab) =$

$(1 + 4)a^3b - 5ab = 5a^3b - 5ab$

54.  $(9pq^6 - 11p^4q) - (-5pq^6 + p^4q^4) =$

$-p^4q^4 + 14pq^6 - 11p^4q$  55a.  $p(t) = m(t) + w(t) =$

$57t + 2332.3$  55b.  $p(5) = 57 \cdot 5 + 2332.3 = 2617.3$ ;

about 2,617,300 men and women enrolled. 55c. the

difference between the number of men and women

enrolled in a college 56.  $n + n + 2 + n + 4 + n + 6 =$

$4n + 12$ ; the answer is D. 57.  $(8x^2 + 3) + (7x^2 + 10) =$

$15x^2 + 13$ ; the answer is G. 58. A. sum =  $3 - 2 + 1 + 8 =$

10; B. sum =  $3 - 6 + 9 = 6$ ; the answer is A.

59. A.  $5 + 3 + 0 = 8$ . B.  $4 + 3 + 1 + 0 = 8$ ; the answer is C. 60. A.  $4 \cdot 2^2 - 9 \cdot 2 + 7 = 16 - 18 + 7 = 5$ ;  
B.  $-2^2 + 12 \cdot 2 + 8 = -4 + 24 + 8 = 28$ ; the answer is B. 61. A.  $(2k - 6) + (3k + 1) = 5k - 5$ ;  
B.  $(k^2 + 4k) - (k^2 - k + 5) = 5k - 5$ ; the answer is C. 62. [2]  $(9x^3 - 4x^2 + 1) - (x^2 + 2) =$   
 $9x^3 - (4 + 1)x^2 + (1 - 2) = 9x^3 - 5x^2 - 1$   
[1] one incorrect term OR no work shown
63. 2 64. 1.4 65. 5 66. 5 67. exponential growth;  $3 > 1$   
68. exponential decay;  $0.4 < 1$  69. exponential growth;  
 $7 > 1$  70. exponential decay;  $0.5 < 1$  71.  $7^8 \cdot 7^{10} =$   
 $7^{8+10} = 7^{18}$  72.  $2^6 \cdot 2^{-7} = 2^{6+(-7)} = 2^{-1} = \frac{1}{2}$
73.  $(4x^2)(9x^3) = (4 \cdot 9)(x^{2+3}) = 36x^5$  74.  $(3ab)(a^2b) =$   
 $3a^{1+2}b^{1+1} = 3a^3b^2$  75.  $(-5t^2)(6t^{-9}) = (-5 \cdot 6)t^{2-9} =$   
 $-30t^{-7} = -\frac{30}{t^7}$  76.  $(-3)^6 \cdot (-3)^{-4} = (-3)^{6-4} =$   
 $(-3)^2 = 9$  77.  $(6h^2)(-2h^8) = 6(-2)h^{2+8} = -12h^{10}$
78.  $(2q^5)(5q^2) = 10q^7$  79.  $y = |x| + 5$  80.  $y = |x - 6|$   
81.  $y = |x| - 12$  82.  $y = |x| + 7$  83.  $y = |x + 10|$   
84.  $y = |x + 0.4|$  85.  $y = |x| + 5.2$  86.  $y = |x| - 2.3$

## 9-2 Multiplying and Factoring

pages 462–46

**Check Skills You'll Need p. 462** For complete solutions see *Daily Skills Check and Lesson Quiz Transparencies* or *Presentation Pro CD-ROM*.

1. 906 2. 287 3. 4536 4.  $24 + 20x$  5.  $-16y - 8$

6.  $25v - 5$  7.  $7p - 14$  8.  $54 - 9x$  9.  $-8q + 2$

**Check Understanding** 1a.  $4b(5b^2 + b + 6) =$   
 $(4b)(5b^2) + (4b)b + (4b)6 = 20b^{1+2} + 4b^{1+1} + 24b =$   
 $20b^3 + 4b^2 + 24b$  1b.  $-7h(3h^2 - 8h - 1) =$   
 $-(7 \cdot 3)(hh^2) + (7 \cdot 8)hh + 7h = -21h^3 + 56h^2 + 7h$

1c.  $2x(x^2 - 6x + 5) = 2x^3 - 12x^2 + 10x$

2a.  $5v^5 = 5 \cdot v \cdot v \cdot v \cdot v \cdot v$

$10v^3 = 2 \cdot 5 \cdot v \cdot v \cdot v$

GCF =  $5 \cdot v \cdot v \cdot v = 5v^3$

2b.  $3t^2 - 18 = (3)t^2 - (3)6$ ; GCF = 3

2c.  $4b^3 - 2b^2 - 6b = (2b)2b^2 - (2b)b - (2b)3$ ; GCF = 2b

3a.  $8x^2 - 12x = (4x)2x - (4x)3 = 4x(2x - 3)$

3b.  $5d^3 + 10d = (5d)d^2 + (5d)2 = 5d(d^2 + 2)$

3c.  $6m^3 - 12m^2 - 24m = (6m)m^2 - (6m)2m - (6m)4$   
 $6m(m^2 - 2m - 4)$

**Exercises** 1.  $8m(m + 6) = 8m^2 + 48m$  2.  $(x + 10)3x$

$x \cdot 3x + 10 \cdot 3x = 3x^2 + 30x$  3.  $9k(7k + 4) =$

$(9 \cdot 7)k^{1+1} + 9k \cdot 4 = 63k^2 + 36k$  4.  $-5a(a - 1) =$

$-5a^2 + 5a$  5.  $2x^2(9 + x) = 18x^2 + 2x^3$

6.  $-p^2(p - 11) = -p^3 + 11p^2$  7.  $2x(6x^3 - x^2 + 5x)$

$(2 \cdot 6)x^{1+3} - 2x^{1+2} + (2 \cdot 5)x^{1+1} =$

$12x^4 - 2x^3 + 10x^2$  8.  $4y^2(9y^3 + 8y^2 - 11) =$

$36y^{2+3} + 32y^{2+2} - 44y^2 = 36y^5 + 32y^4 - 44y^2$

9.  $-5c^3(9c^2 - 8c - 5) = -45c^5 + 40c^4 + 25c^3$

10.  $-7q^2(6q^5 - 2q - 7) = -42q^{2+5} + 14q^{2+1} + 49q^2$

$-42q^7 + 14q^3 + 49q^2$  11.  $-3g^7(g^4 - 6g^2 + 5) =$

$-3g^{11} + 18g^9 - 15g^7$  12.  $-4x^6(10x^3 + 3x^2 - 7) =$

$-40x^9 - 12x^8 + 28x^6$  13.  $15w + 21 = (3)5w + (3)7$ ;  
GCF = 3 14.  $6a^2 - 8a = (2a)3a - (2a)4$ ; GCF = 2a

15.  $36v + 24 = (12)3v + (12)2$ ; GCF = 12  
 16.  $x^3 + 7x^2 - 5x = (x)x^2 + (x)7x - (x)5$ ; GCF =  $x$   
 17.  $5b^3 + 15b - 30 = (5)b^3 + (5)3b - (5)6$ ; GCF = 5  
 18.  $9x^3 - 6x^2 + 12x = (3x)3x^2 - (3x)2x + (3x)4$ ;  
 GCF =  $3x$  19.  $6x - 4 = 2(3x - 2)$  20.  $v^2 + 4v =$   
 $(v + 4)$  21.  $10x^3 - 25x^2 + 20 = 5(2x^3 - 5x^2 + 4)$   
 22.  $2t^2 - 10t^4 = 2t^2(1 - 5t^2)$  23.  $15n^3 - 3n^2 + 12n =$   
 $3n(5n^2 - n + 4)$  24.  $6p^6 + 24p^5 + 18p^3 =$   
 $6p^3(p^3 + 4p^2 + 3)$  25. Karla; Kevin wrote  $-2x \cdot -3 =$   
 $-6x$  instead of  $+6x$ . 26. Answers may vary. Sample:  
 $3x^3 + 12x^2 + 24x; 4x(2x^2 + 3x + 6)$   
 27.  $-3a(4a^2 - 5a + 9) = -12a^{1+2} + 15a^{1+1} - 27a =$   
 $-12a^3 + 15a^2 - 27a$  28.  $-7p^2(-2p^3 + 5p) =$   
 $4p^5 - 35p^3$  29.  $12c(-5c^2 + 3c - 4) =$   
 $-60c^3 + 36c^2 - 48c$  30.  $y(y + 3) - 5y(y - 2) =$   
 $y^2 + 3y - 5y^2 + 10y = -4y^2 + 13y$   
 31.  $x^2(x + 1) - x(x^2 - 1) = x^3 + x^2 - x^3 + x =$   
 $x^2 + x$  32.  $4t(3t^2 - 4t) - t(7t) = 12t^3 - 16t^2 - 7t^2 =$   
 $12t^3 - 23t^2$  33a.  $A = \pi(4x)^2 - (2x)^2 =$   
 $6\pi x^2 - 4x^2$  33b.  $A = 4x^2(4\pi - 1)$   
 34.  $9m^{12} - 36m^7 + 81m^5 = 9m^5(m^7 - 4m^2 + 9)$   
 35.  $24x^3 - 96x^2 + 48x = 24x(x^2 - 4x + 2)$   
 36.  $16n^3 + 48n^2 - 80n = 16n(n^2 + 3n - 5)$   
 37.  $5x^4 + 4x^3 + 3x^2 = x^2(5x^2 + 4x + 3)$   
 38.  $13ab^3 + 39a^2b^4 = 13ab^3(1 + 3ab)$   
 39.  $7g^2k^3 - 35g^5k^2 = 7g^2k^2(k - 5g^3)$  40. 25; since  
 $p$  and  $q$  only have one 5 as a common factor,  $p^2 = p \cdot p$   
 and  $q^2 = q \cdot q$  only have  $5 \cdot 5 = 25$  as a GCF.  
 41a.  $n^2 - n = n(n - 1)$  41b. Always; the product of two  
 consecutive integers is always even, since one of the  
 integers is even. 42a.  $T(1) = \frac{1}{2}(1 + 1) = 1$ ;  $T(2) =$   
 $\frac{1}{2}(2 + 1) = 3$ ;  $T(3) = \frac{3}{2}(3 + 1) = 6$ ;  $T(4) = \frac{4}{2}(4 + 1) =$   
 10; the pattern shows that  $T(n) = \frac{n}{2}(n + 1)$ .  
 42b.  $T(100) = \frac{100}{2}(100 + 1) = 5050$  43a. 6; 3  
 43b.  $n - 3$ ; diagonals connect two nonconsecutive  
 vertices. 43c.  $\frac{n}{2}(n - 3) = \frac{1}{2}n^2 - \frac{3}{2}n$  43d.  $\frac{8}{2}(8 - 3) = 20$   
 44a.  $V = (4s)^3 = 64s^3$  44b.  $V = 48\pi s^2$  44c.  $V =$   
 $64s^3 - 48\pi s^2 = 16s^2(4s - 3\pi)$  44e.  $V =$   
 $16 \cdot 15^2(4 \cdot 15 - 3\pi) \approx 182,071$ ; about 182,071 in.<sup>3</sup>  
 45.  $x(6x^2 - 4x - 2) = 6x^3 - 4x^2 - 2x$ ; the answer is B.  
 46.  $(p^2 - 3) - (5 - p + 2p^2) - (4p + 5 - 2p^2) =$   
 $(1 - 2 + 2)p^2 + (1 - 4)p + (-3 - 5 - 5) =$   
 $p^2 - 3p - 13$ ; the answer is F. 47.  $-24 = -24 \times 1 =$   
 $-12 \times 2 = -8 \times 3 = -6 \times 4 = -4 \times 6 = -3 \times 8 =$   
 $-2 \times 12 = -1 \times 24$ ;  $[-24] = 8$ ; the answer is C. 48.  $2n$   
 must be even, so  $2n + 1$  must be odd; the answer is G.  
 49.  $6g^8 - 3g^4 + 9g^2 = 3g^2(2g^6 - g^2 + 3)$ ; the answer is  
 B. 50. [2]  $10x^4 + 6x^3 + 2x^2 = 2x^2(5x^2 + 3x + 1)$ ; the  
 terms  $5x^2, 3x, 1$  have no common factor other than 1.  
 [1] incorrect factoring OR incorrect explanation  
 51.  $(x^2 + 3) - (4x^2 - 7) = (1 - 4)x^2 + (3 + 7) =$   
 $-3x^2 + 10$  52.  $(m^3 + 8m + 6) + (-5m^2 + 4m) =$   
 $m^3 - 5m^2 + 12m + 6$   
 53.  $(g^2 + 6g - 2) + (4g^2 - 7g + 2) =$   
 $(1 + 4)g^2 + (6 - 7)g = 5g^2 - g$   
 54.  $(3r^2 - 8r + 7) - (2r^2 + 8r - 9) = r^2 - 16r + 16$   
 55.  $(t^4 - t^3 + 1) + (t^3 + 5t^2 - 10) = t^4 + 5t^2 - 9$   
 56.  $(3b^3 - b^2) - (5b^2 + 12) = 3b^3 - 6b^2 - 12$

57.  $5^{-1} = \frac{1}{5}$  58.  $5^{-2} = \frac{1}{5^2} = \frac{1}{25}$  59.  $(-2)^{-3} =$   
 $\frac{1}{(-2)^3} = -\frac{1}{8}$  60.  $8^0 = 1$  61.  $n^{-3}m^2 = \frac{m^2}{n^3}$  62.  $v^3w^{-5} = \frac{v^3}{w^5}$   
 63.  $\frac{4}{c^{-3}} = 4c^3$  64.  $\frac{ab^{-8}}{c^5} = \frac{a}{b^8c^5}$   
 65.  $7x + 6y = 33$   
 $\underline{2x - 6y = -6}$   
 $9x = 27$   
 $x = 3$   
 $2 \cdot 3 - 6y = -6$   
 $-6y = -12$   
 $y = 2$   
 66.  $3x - 2y = 21$   
 $\underline{6x - 4y = 42}$   
 $8x + 4y = 28$   
 $\underline{14x = 70}$   
 $x = 5$   
 $3 \cdot 5 - 2y = 21$   
 $-2y = 6$   
 $y = -3$   
 67.  $4x + 2y = 16$   
 $\underline{11x - 3y = -7}$   
 $12x + 6y = 48$   
 $\underline{22x - 6y = -14}$   
 $34x = 34$   
 $x = 1$   
 $4 \cdot 1 + 2y = 16$   
 $2y = 12$   
 $y = 6$

### INVESTIGATION

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1.  $(x + 1)(x + 6) = x^2 + 7x + 6$  2.  $(x + 1)(x - 2) =$   
 $x^2 - x - 2$  3.  $(x + 1)(4x - 1) = 4x^2 + 3x - 1$   
 4.  $(x + 4)(2x + 1) = 2x^2 + 9x + 4$  5.  $(x - 3)(3x + 5) =$   
 $3x^2 - 4x - 15$  6.  $(2x + 3)(3x + 5) = 6x^2 + 19x + 15$

### 9-3 Multiplying Binomials

pages 467-473

Check Skills You'll Need p. 467 For complete  
 solutions see Daily Skills Check and Lesson Quiz  
 Transparencies or Presentation Pro CD-ROM.

1.  $4r^2 - r$  2.  $6h^3 + 48h^2 - 18h$  3.  $2y^5 - 7y^2$   
 4.  $x^3 + 8x^2 + 2x + 1$  5.  $8t^3 + t + 6$  6.  $5w^2 - 27w$   
 7.  $-2b^2 - 15b$  8.  $7m^3 + 27m^2 - 6m$  9.  $d^5 - 4d^3 - 18d^2$

- Check Understanding 1a.  $(6h - 7)(2h + 3) =$   
 $6h(2h + 3) - 7(2h + 3) = 12h^2 + 18h - 14h - 21 =$   
 $12h^2 + 4h - 21$  1b.  $(5m + 2)(8m - 1) =$   
 $5m(8m - 1) + 2(8m - 1) = 40m^2 - 5m + 16m - 2 =$   
 $40m^2 + 11m - 2$  1c.  $(9a - 8)(7a + 4) =$   
 $9a(7a + 4) - 8(7a + 4) = 63a^2 + 36a - 56a - 32 =$   
 $63a^2 - 20a - 32$  2a.  $(3x + 4)(2x + 5) =$   
 $(3x)(2x) + (3x)(5) + (4)(2x) + (4)(5) =$   
 $6x^2 + 15x + 8x + 20 = 6x^2 + 23x + 20$   
 2b.  $(3x - 4)(2x + 5) =$   
 $(3x)(2x) + (3x)(5) - (4)(2x) - (4)(5) =$   
 $6x^2 + 15x - 8x - 20 = 6x^2 + 7x - 20$

2c.  $(3x + 4)(2x - 5) =$   
 $(3x)(2x) - (3x)(5) + (4)(2x) - (4)(5) =$   
 $6x^2 - 15x + 8x - 20 = 6x^2 - 7x - 20$

2d.  $(3x - 4)(2x - 5) =$   
 $(3x)(2x) - (3x)(5) - (4)(2x) + (4)(5) =$   
 $6x^2 - 15x - 8x + 20 = 6x^2 - 23x + 20$

3a.  $(5x + 8)(6x + 2) - 5x(x + 6) =$   
 $30x^2 + 10x + 48x + 16 - 5x^2 - 30x =$   
 $30x^2 - 5x^2 + 10x + 48x - 30x + 16 = 25x^2 + 28x + 16$   
 3b.  $(x + 1)(2x - 2) - x(x - 2) =$   
 $2x^2 - 2x + 2x - 2 - x^2 + 2x = x^2 + 2x - 2$

4. 
$$\begin{array}{r} 2n^2 + n + 7 \\ \times \quad 6n - 8 \\ \hline - 16n^2 - 8n - 56 \end{array}$$

$\underline{12n^3 + 6n^2 + 42n}$   
 $12n^3 - 10n^2 + 34n - 56;$   
 $(6n - 8)(2n^2 + n + 7) = 12n^3 + 6n^2 + 42n - 16n^2 -$   
 $8n - 56 = 12n^3 - 10n^2 + 34n - 56$

**Exercises** 1.  $(5a + 2)(6a - 1) = 30a^2 + 7a - 2$   
 2.  $(3c - 7)(2c - 5) = 6c^2 - 29c + 35$  3.  $(z - 4)(2z + 1) = 2z^2 - 7z - 4$  4.  $(2x + 9)(x + 2) = 2x^2 + 13x + 18$   
 5.  $(x + 2)(x + 5) = x(x + 5) + 2(x + 5) = x^2 + 5x + 2x + 10 = x^2 + 7x + 10$  6.  $(h + 3)(h + 4) = h(h + 4) + 3(h + 4) = h^2 + 4h + 3h + 12 = h^2 + 7h + 12$  7.  $(k + 7)(k - 6) = k(k - 6) + 7(k - 6) = k^2 - 6k + 7k - 42 = k^2 + k - 42$  8.  $(a - 8)(a - 9) = a(a - 9) - 8(a - 9) = a^2 - 9a - 8a + 72 = a^2 - 17a + 72$   
 9.  $(2x - 1)(x + 2) = 2x(x + 2) - (x + 2) = 2x^2 + 4x - x - 2 = 2x^2 + 3x - 2$  10.  $(2y + 5)(y - 3) = 2y(y - 3) + 5(y - 3) = 2y^2 - 6y + 5y - 15 = 2y^2 - y - 15$  11.  $(r + 6)(r - 4) = r^2 - 4r + 6r - 24 = r^2 + 2r - 24$  12.  $(y + 4)(5y - 8) = 5y^2 - 8y + 20y - 32 = 5y^2 + 12y - 32$   
 13.  $(x + 6)(x - 7) = x^2 - 7x + 6x - 42 = x^2 - x - 42$   
 14.  $(m - 6)(m - 9) = m^2 - 9m - 6m + 54 = m^2 - 15m + 54$  15.  $(4b - 2)(b + 3) = 4b^2 + 12b - 2b - 6 = 4b^2 + 10b - 6$

16.  $(8w + 2)(w + 5) = 8w^2 + 40w + 2w + 10 = 8w^2 + 42w + 10$  17.  $(x - 7)(x + 9) = x^2 + 9x - 7x - 63 = x^2 + 2x - 63$  18.  $(a + 11)(a + 5) = a^2 + 5a + 11a + 55 = a^2 + 16a + 55$   
 19.  $(p - 1)(p + 10) = p^2 + 10p - p - 10 = p^2 + 9p - 10$  20.  $(x + 3)(x + 2) - x(x - 3) = x^2 + 5x + 6 - x^2 + 3x = 8x + 6$   
 21.  $(x + 8)(x + 6) - 3x(x + 3) = x^2 + 14x + 48 - 3x^2 - 9x = -2x^2 + 5x + 48$

22. 
$$\begin{array}{r} x^2 - 4x + 1 \\ \times \quad x + 9 \\ \hline 9x^2 - 36x + 9 \\ x^3 - 4x^2 + x \\ \hline x^3 + 5x^2 - 35x + 9 \end{array}$$

23. 
$$\begin{array}{r} a^2 - 2a + 1 \\ \times \quad a - 4 \\ \hline -4a^2 + 8a - 4 \\ a^3 - 2a^2 + a \\ \hline a^3 - 6a^2 + 9a - 4 \end{array}$$

24. 
$$\begin{array}{r} 2g^2 + 3g + 3 \\ \times \quad g - 3 \\ \hline -6g^2 - 9g - 9 \\ 2g^3 + 3g^2 + 3g \\ \hline 2g^3 - 3g^2 - 6g - 9 \end{array}$$

25. 
$$\begin{array}{r} 3k^2 - 5k + 7 \\ \times \quad k + 8 \\ \hline 24k^2 - 40k + 56 \\ 3k^3 - 5k^2 + 7k \\ \hline 3k^3 + 19k^2 - 33k + 56 \end{array}$$

26.  $(9x - 3)(x^2 + 2x + 1) = 9x^3 + 18x^2 + 9x - 3x^2 - 6x - 3 = 9x^3 + 15x^2 + 3x - 3$

27.  $(2t - 5)(t^2 - 6t + 3) = 2t^3 - 12t^2 + 6t - 5t^2 + 30t - 15 =$

$2t^3 - 17t^2 + 36t - 15$  28.  $(8p + 9)(7p^2 + 5p - 1) = 56p^3 + 40p^2 - 8p + 63p^2 + 45p - 9 =$

$56p^3 + 103p^2 + 37p - 9$  29.  $(4w - 2)(12w^2 - w - 1) = 48w^3 - 4w^2 - 4w - 24w^2 + 2w + 2 =$

$48w^3 - 28w^2 - 2w + 2$  30.  $(p - 7)(p + 8) = p^2 + 8p - 7p + 56 = p^2 + p + 56$

31.  $(-7 + p)(8 + p) = -56 - 7p + 8p + p^2 = p^2 + p - 56$  32.  $(p^2 - 7)(p + 8) = p^3 + 8p^2 - 7p - 56$

33.  $(5c - 9)(5c + 1) = 25c^2 + 5c - 45c - 9 = 25c^2 - 40c - 9$  34.  $(n^2 + 3)(n + 11) = n^3 + 11n^2 + 3n + 33$  35.  $(3k^2 + 2)(5k^2 + k) = 15k^4 + 3k^3 + 10k^2 + 2k$  36.  $(6h - 1)(4h^2 + h + 3) = 24h^3 + 6h^2 + 18h - 4h^2 - h - 3 = 24h^3 + 2h^2 + 17h - 3$

37.  $(9y^2 + 2)(y^2 - y - 1) = 9y^4 - 9y^3 - 9y^2 + 2y^2 - 2y - 2 =$

$9y^4 - 9y^3 - 7y^2 - 2y - 2$  38.  $(8q - 4)(6q^2 + q + 1) = 48q^3 + 8q^2 + 8q - 24q^2 - 4q - 4 =$

$48q^3 - 16q^2 + 4q - 4$  39a. Let  $x$  = width of garden.  
 Area of garden =  $x(2x) = 2x^2$ . Area of garden and walk =  $(x + 4)(2x + 4) = 2x^2 + 12x + 16$ .

39b. Area of walk only =  $(2x^2 + 12x + 16) - 2x^2 = 12x + 16$ .

39c. 
$$\begin{array}{r} 12x + 16 = 76 \\ 12x = 60 \\ x = 5 \end{array}$$

Garden should be 5 ft by 10 ft.

40. Answers may vary. Sample:  $(x + 2)(x^2 + 3x + 4) = x^3 + 3x^2 + 4x + 2x^2 + 6x + 8 = x^3 + 5x^2 + 10x + 8$

41. Answers may vary. Sample: vertical method, in which the terms are aligned

42.  $0.5(x + 6)(2x + 5) - x(x + 1) = 0.5(2x^2 + 17x + 30) - x^2 - x =$

$x^2 + 8.5x + 15 - x^2 - x = 7.5x + 15$  43.  $0.5(x + 2x - 1)(x + 2) = 0.5(3x - 1)(x + 2) = 0.5(3x^2 + 5x - 2) = 1.5x^2 + 2.5x - 1$

44a.i.  $(x + 1)(x + 1) = x^2 + 2x + 1; 11 \cdot 11 = 121$   
 ii.  $(x + 1)(x + 2) = x^2 + 3x + 2; 11 \cdot 12 = 132$

iii.  $(x + 1)(x + 3) = x^2 + 4x + 3; 11 \cdot 13 = 143$  44b. The two problems in each case are identical if  $x = 10$ . In the result  $ax^2 + bx + c$ ,  $a$  corresponds to the hundreds digit,  $b$  to the tens digit, and  $c$  to the ones digit.

45.  $V = (n + 7)(n)(n + 8) = (n + 7)(n^2 + 8n) = n^3 + 15n^2 + 56n$  46.  $(n + 2)(n + 4) = n^2 + 6n + 8$

47.  $6(x+3)(x+3) = 6(x^2 + 6x + 9) = 6x^2 + 36x + 54$   
 48.  $6(4t+1)(4t+1) = 6(16t^2 + 8t + 1) = 96t^2 + 48t + 6$   
 49.  $6(2w^2 + 7)(2w^2 + 7) = 6(4w^4 + 28w^2 + 49) = 24w^4 + 168w^2 + 294$  50a.  $V(t) = C(t) \cdot P(t) = (2.7t + 165)(2.6t + 248) = 7.02t^2 + 1098.6t + 40,920$   
 50b.  $V(5) = 7.02 \cdot 5^2 + 1098.6 \cdot 5 + 40,920 = 46,588.5$ ; about 46,588,500,000 lb  
 51a.  $2000(1+r)(1+r)(1+r) = 2000(1+r)(1+2r+r^2) = 2000(1+2r+r^2+r+2r^2+r^3) = 2000(1+3r+3r^2+r^3) = 2000r^3 + 6000r^2 + 6000r + 2000$  51b.  $2000(1.03)^3 = 2000 \cdot 1.092727 \approx 2185.45$ ; \$2185.45 52.  $\pi(g+2)^2 = \pi g^2 + 4\pi g + 4\pi$  53.  $\pi(4k+5)^2 = \pi(4k+5)(4k+5) = \pi(16k^2 + 40k + 25) = 16\pi k^2 + 40\pi k + 25\pi$   
 54.  $\pi(3x+1)(3x+1) = \pi(9x^2 + 6x + 1) = 9\pi x^2 + 6\pi x + \pi$  55.  $14 \cdot 72 = 1008$  56.  $53 \cdot 87 = 4611$  57.  $91 \cdot 64 = 5824$  58.  $38 \cdot 64 = 2432$   
 59.  $(n-1)(n-4) = n^2 - 5n + 4$ ; the answer is A.  
 60.  $(8k-3)(k^2-k+1) = 8k^3 - 8k^2 + 8k - 3k^2 + 3k - 3 = 8k^3 - 11k^2 + 11k - 3$ ; the answer is H. 61. A. even if  $n$  is odd B.  $(2n-1)(2n+1) = 4n^2 - 1$ ;  $4n^2$  is even so  $4n^2$  is odd C.  $(2n-1)(n+1) = 2n^2 + n - 1$  is even if  $n$  is odd D.  $(2n+1)(n-1) = 2n^2 - n - 1$  is even if  $n$  is odd; the answer is B. 62. [2] Multiply each term in the trinomial by  $4v$ , and then each original term by  $-1$ ; add the 6 products.  $(4v-1)(2v^2+v+1) = 8v^3 + 4v^2 + 4v - 2v^2 - v - 1 = 8v^3 + 2v^2 + 3v - 1$   
 [1] incorrect calculation OR incorrect explanation  
 63. [4]  $(5n-2)(2n+6) - (n+2)(3n+2) = 10n^2 + 30n - 4n - 12 - 3n^2 - 2n - 6n - 4 = 7n^2 + 18n - 16$  [3] one computational error  
 [2] incorrect products subtracted correctly OR correct products subtracted incorrectly [1] no work shown  
 64.  $4v(5v-7) = 20v^2 - 28v$  65.  $(c-9)3c = 3c^2 - 27c$   
 66.  $8t^2(t+6) = 8t^3 + 48t^2$  67.  $y(3y-10) = 3y^2 - 10y$   
 68.  $5x^2(11-x) = -5x^3 + 55x^2$  69.  $-t^3(6t-1) = -6t^4 + t^3$  70.  $4r(3-r^5) = -4r^6 + 12r$  71.  $9b^2(b^3+2b) = 9b^5 + 18b^3$  72.  $5w+45 = 5(w+9)$  73.  $3x^2 - 11x = x(3x-11)$  74.  $4a^2 + 12a = 4a(a+3)$  75.  $9n^2 - n^3 = n^2(9-n)$  76.  $34t - 51 = 17(2t-3)$  77.  $63v^2 + 45v = 9v(7v+5)$  78.  $25m - 60m^3 = 5m(5 - 12m^2)$   
 79.  $11k + 77k^6 = 11k(1 + 7k^5)$   
 80.  $\frac{3^5}{3^2} = 3^{5-2} = 3^3 = 27$  81.  $\frac{3^2}{3^5} = \frac{1}{3^3} = \frac{1}{27}$   
 82.  $\frac{y^{12}}{y^8} = y^4$  83.  $\frac{2w^{-3}}{6w^2} = \frac{1}{3w^5}$  84.  $\frac{x^{-8}}{2x^3} = \frac{1}{2x^{11}}$   
 85.  $\left(\frac{5}{3}\right)^{-1} = \frac{3}{5}$  86.  $\left(\frac{5}{3}\right)^{-2} = \left(\frac{3}{5}\right)^2 = \frac{3^2}{5^2} = \frac{9}{25}$   
 87.  $\left(\frac{5}{3}\right)^0 = 1$  88.  $\left(\frac{4x}{7}\right)^{-2} = \left(\frac{7}{4x}\right)^2 = \frac{7^2}{4^2x^2} = \frac{49}{16x^2}$   
 89.  $\left(\frac{y^{-2}}{8}\right)^{-2} = \left(\frac{8}{y^{-2}}\right)^2 = (8y^2)^2 = 64y^4$

### CHECKPOINT QUIZ 1

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1.  $(4x^2 + x + 3) + (5x^2 + 9x - 2) = 9x^2 + 10x + 1$   
 2.  $(7b^2 - 5b + 3) - (b^2 + 8b - 6) = 6b^2 - 13b + 9$

3.  $(g^2 + 4)(4g^2 + 8g - 9) = 4g^4 + 8g^3 - 9g^2 + 16g^2 + 32g - 36 = 4g^4 + 8g^3 + 7g^2 + 32g - 36$   
 4.  $6k(4k + k^2) + 9k(2k - 6k^2) = 24k^2 + 6k^3 + 18k^2 - 54k^3 = -48k^3 + 42k^2$  5.  $(x+3)(x-5) = x^2 - 2x - 15$  6.  $(2n^3 - 5)(6n^2 + n) = 12n^5 + 2n^4 - 30n^2 - 5n$  7.  $3w(12w - 1) - 8w = 36w^2 - 3w - 8w = 36w^2 - 11w$  8.  $12y^2 - 10 = 2(6y^2 - 5)$  9.  $5t^6 + 25t^3 - 10t = 5t(t^5 + 5t^2 - 2)$   
 10.  $18v^4 + 27v^3 + 36v^2 = 9v^2(2v^2 + 3v + 4)$

### READING MATH

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Total area of outer box – area of white box =  
 $(x+4)(x+4) - x(x+1) = x^2 + 4x + 4x + 16 - x^2 - x = 7x + 16$ .

### 9.4 Multiplying Special Cases

pages 474–479

Check Skills You'll Need p. 474 For complete solutions see Daily Skills Check and Lesson Quiz Transparencies or Presentation Pro CD-ROM.

1.  $49x^2$  2.  $9v^2$  3.  $16c^2$  4.  $25g^6$  5.  $j^2 + 12j + 35$   
 6.  $6b^2 - 34b + 48$  7.  $20y^2 - 3y - 2$  8.  $x^2 - x - 12$   
 9.  $8c^4 - 78c^2 - 20$  10.  $54y^4 - 21y^2 - 3$

Investigation 1. Row 1:  $(x+8)(x+8) = x^2 + 8x + 64 = x^2 + 16x + 64$ ;  $(y+5)(y+5) = y^2 + 10y + 25$ ;  $(2p+3)(2p+3) = 4p^2 + 12p + 9$ ; Row 2:  $(d-3)(d-3) = d^2 - 3d - 3d + 9 = d^2 - 6d + 9$ ;  $(t-1)(t-1) = t^2 - 2t + 1$ ;  $(9r-2)(9r-2) = 81r^2 - 36r + 4$ ; Row 3:  
 $(x+4)(x-4) = x^2 - 4x + 4x - 16 = x^2 - 16$ ;  $(k+9)(k-9) = k^2 - 81$ ;  $(3c+7)(3c-7) = 9c^2 - 49$  2. Row 1:  $(a+b)(a+b) = a^2 + 2(ab) + b^2$ ; Row 2:  $(a-b)(a-b) = a^2 - 2(ab) + b^2$ ; Row 3:  
 $(a+b)(a-b) = a^2 - b^2$  3.  $(p+6)(p+6) = p^2 + 2(6p) + 6^2 = p^2 + 12p + 36$ ;  $(v-5)(v-5) = v^2 - 2(5v) + 5^2 = v^2 - 10v + 25$ ;  $(x+8)(x-8) = x^2 - 8^2 = x^2 - 64$  4. yes

Check Understanding 1a.  $(t+6)^2 = t^2 + 2t(6) + 6^2 = t^2 + 12t + 36$  1b.  $(5y+1)^2 = (5y)^2 + 2(5y) + 1 = 25y^2 + 10y + 1$  1c.  $(7m-2p) = (7m)^2 - 2(7m)(2p) + (2p)^2 = 49m^2 - 28mp + 4p^2$   
 1d.  $(9c-8)^2 = (9c)^2 - 2(9c)(8) + 8^2 = 81c^2 - 144c + 64$  2a.  $\left(\frac{1}{3}A + \frac{2}{3}B\right)^2 = \left(\frac{1}{3}A\right)^2 + 2\left(\frac{1}{3}A\right)\left(\frac{2}{3}B\right) + \left(\frac{2}{3}B\right)^2 = \frac{1}{9}A^2 + \frac{4}{9}AB + \frac{4}{9}B^2$   
 2b.  $P(AA) = \frac{1}{9}$  2c.  $P(AB) = \frac{4}{9}$  2d.  $P(BB) = \frac{4}{9}$   
 3a.  $31^2 = (30+1)^2 = 30^2 + 2(30) + 1 = 900 + 60 + 1 = 961$  3b.  $29^2 = (30-1)^2 = 30^2 - 2(30) + 1 = 900 - 60 + 1 = 841$  3c.  $98^2 = (100-2)^2 = 100^2 - 2(100)2 + 4 = 10,000 - 400 + 4 = 9604$  3d.  $203^2 = (200+3)^2 = 200^2 + 6(200) + 3^2 = 40,000 + 1200 + 9 = 41,209$  4a.  $(d+11)(d-11) = d^2 - 11^2 = d^2 - 121$  4b.  $(c^2 + 8)(c^2 - 8) =$

$$(c^2)^2 - 8^2 = c^4 - 64 \quad 4c. \quad (9v^3 + w^4)(9v^3 - w^4) = \\ (9v^3)^2 - (w^4)^2 = 81v^6 - w^8 \quad 5a. \quad 18 \cdot 22 = \\ (20 - 2)(20 + 2) = 400 - 4 = 396$$

$$5b. \quad 19 \cdot 21 = (20 - 1)(20 + 1) = 400 - 1 = 399 \quad 5c. \quad 59 \cdot 61 = (60 - 1)(60 + 1) = 3600 - 1 = 3599 \quad 5d. \quad 87 \cdot 93 = (90 - 3)(90 + 3) = 8100 - 9 = 8091$$

**Exercises**

1.  $(c + 1)^2 = c^2 + 2c + 1$
2.  $(x + 4)^2 = x^2 + 2(4x) + 4^2 = x^2 + 8x + 16$
3.  $(2v + 11)^2 = (2v)^2 + 2(2v)11 + 11^2 = 4v^2 + 44v + 121$
4.  $(3m + 7)^2 = (3m)^2 + 2(3m)7 + 7^2 = 9m^2 + 42m + 49$
5.  $(w - 12)^2 = w^2 - 24w + 144$
6.  $(b - 5)^2 = b^2 - 10b + 25$
7.  $(6x - 8)^2 = (6x)^2 - 2(6x)8 + 8^2 = 36x^2 - 96x + 64$
8.  $(9j - 2)^2 = 81j^2 - 36j + 4$
- 9a.  $\left(\frac{1}{4}C + \frac{3}{4}D\right)^2 = \left(\frac{1}{4}C\right)^2 + 2\left(\frac{1}{4}C\right)\left(\frac{3}{4}D\right) + \left(\frac{3}{4}D\right)^2 = \frac{1}{16}C^2 + \frac{3}{8}CD + \frac{9}{16}D^2$
- 9b.  $P(CC) = P(1)P(1) = \frac{1}{4} \cdot \frac{1}{4} = \frac{1}{16}$
- 9c. It is the coefficient of  $C^2$ .

10.  $61^2 = (60 + 1)^2 = 3600 + 120 + 1 = 3721$
11.  $99^2 = (100 - 1)^2 = 10,000 - 200 + 1 = 9801$
12.  $48^2 = (50 - 2)^2 = 2500 - 200 + 4 = 2304$
13.  $302^2 = (300 + 2)^2 = 90,000 + 1200 + 4 = 91,204$
14.  $499^2 = (500 - 1)^2 = 250,000 - 1000 + 1 = 249,001$
15.  $(x + 4)(x - 4) = x^2 - 4x + 4x - 4^2 = x^2 - 16$
16.  $(a + 8)(a - 8) = a^2 - 64$
17.  $(d + 7)(d - 7) = d^2 - 49$
18.  $(h + 15)(h - 15) = h^2 - 225$
19.  $(y + 12)(y - 12) = y^2 - 144$
20.  $(k + 5)(k - 5) = k^2 - 25$
21.  $31 \cdot 29 = (30 + 1)(30 - 1) = 900 - 1 = 899$
22.  $89 \cdot 91 = (90 - 1)(90 + 1) = 8100 - 1 = 8099$
23.  $52 \cdot 48 = (50 + 2)(50 - 2) = 2500 - 4 = 2496$
24.  $197 \cdot 203 = (200 - 3)(200 + 3) = 40,000 - 9 = 39,991$
25.  $299 \cdot 301 = (300 - 1)(300 + 1) = 90,000 - 1 = 89,999$
26.  $(x + 3)^2 - x^2 = x^2 + 6x + 9 - x^2 = 6x + 9; (6x + 9) \text{ units}^2$
27.  $(x + 4)^2 - (x - 1)^2 = x^2 + 8x + 16 - (x^2 - 2x + 1) = 10x - 15; (10x - 15) \text{ units}^2$
28.  $(x + 3y)^2 = x^2 + 2(3xy) + (3y)^2 = x^2 + 6xy + 9y^2$
29.  $(5p - 9)^2 = (5p)^2 - 2(5p)q + q^2 = 25p^2 - 10pq + q^2$
30.  $(6m + n)^2 = 36m^2 + 12mn + n^2$
31.  $(x - 7y)^2 = x^2 - 14xy + 49y^2$
32.  $(4k + 7j)^2 = 16k^2 + 56kj + 49j^2$
33.  $(2y - 9x)^2 = 4y^2 - 36xy + 81x^2$
34.  $(3w + 10t)^2 = 9w^2 + 60wt + 100t^2$
35.  $(6a + 11b)^2 = 36a^2 + 132ab + 121b^2$
36.  $(5p - 6q)^2 = 25p^2 - 60pq + 36q^2$
37.  $(6h - 8p)^2 = 36h^2 - 96hp + 64p^2$
38.  $(y^5 - 9x^4)^2 = y^{10} - 18x^4y^5 + 81x^8$
39.  $(8k + 4h)^2 = 64k^2 + 64kh + 16h^2$

$$40a. \quad \left(\frac{1}{2}R + \frac{1}{2}W\right)^2 = \frac{1}{4}R^2 + \frac{1}{2}RW + \frac{1}{4}W^2 \quad 40b. \quad \frac{1}{2}$$

$$40c. \quad \left(\frac{1}{2}R + \frac{1}{2}W\right)(R) = \frac{1}{2}R^2 + \frac{1}{2}RW \quad 40d. \quad 0$$

41a.

$4^2 = 16$	$3 \cdot 5 = 15$
$5^2 = 25$	$4 \cdot 6 = 24$
$6^2 = 36$	$5 \cdot 7 = 35$
$7^2 = 49$	$6 \cdot 8 = 48$

41b.  $n^2$  is one more than the product  $(n - 1)(n + 1)$ .

41c. The product  $(n - 1)(n + 1)$  is  $n^2 - 1$ .

42. Answers may vary.  
 $(x + y)^2 = x^2 + 2xy + y^2$ ,

so any example where  $x \neq 0$  and  $y \neq 0$  will suffice.

$$43 \text{ No; } \left(\frac{3}{2}\right)^2 = \left(3 + \frac{1}{2}\right)^2 = 3^2 + 2 \cdot 3 \cdot \frac{1}{2} + \left(\frac{1}{2}\right)^2 = 9 + 3 + \frac{1}{4} = 12\frac{1}{4}; \text{ the example omitted the middle term.}$$

$$44. \quad (3y + 5w)(3y - 5w) = (3y)^2 - (3y)(5w) + (3y)(5w) + (5w)^2 = 9y^2 - 25w^2$$

$$45. \quad (p + 9q)(p - 9q) = p^2 - 81q^2$$

$$46. \quad (2d + 7g)(2d - 7g) = 4d^2 - 49g^2$$

$$47. \quad (7b - 8c)(7b + 8c) = 49b^2 - 64c^2$$

$$48. \quad (g + 7h)(g - 7h) = g^2 - 49h^2$$

$$49. \quad (g^3 + 7h^2)(g^3 - 7h^2) = g^6 - 49h^4$$

$$50. \quad (2a^2 + b)(2a^2 - b) = 4a^4 - b^2$$

$$51. \quad (11x - y^3)(11x + y^3) = 121x^2 - y^6$$

$$52. \quad (4k - 3h^2)(4k + 3h^2) = 16k^2 - 9h^4$$

$$53. \quad (a + b + c)^2 = (a + b + c)(a + b + c) = a^2 + ab + ac + ba + b^2 + bc + ca + cb + c^2 =$$

$$a^2 + b^2 + c^2 + 2ab + 2bc + 2ac$$

$$54a. \quad \left(\frac{1}{2}H + \frac{1}{2}T\right)^3 = \left(\frac{1}{2}H + \frac{1}{2}T\right)\left(\frac{1}{2}H + \frac{1}{2}T\right)\left(\frac{1}{2}H + \frac{1}{2}T\right) =$$

$$\left(\frac{1}{2}H + \frac{1}{2}T\right)\left(\frac{1}{4}H^2 + \frac{1}{2}HT + \frac{1}{4}T^2\right) =$$

$$\frac{1}{8}H^3 + \frac{1}{4}H^2T + \frac{1}{8}HT^2 + \frac{1}{8}H^2T + \frac{1}{4}HT^2 + \frac{1}{8}T^3 =$$

$$\frac{1}{8}H^3 + \frac{3}{8}H^2T + \frac{3}{8}HT^2 + \frac{1}{8}T^3 \quad 54b. \quad P(HT^2) = \frac{3}{8}$$

$$55a. \quad m = 3n + 1; m^2 = (3n + 1)^2 = 9n^2 + 6n + 1 =$$

$$3(3n^2 + 2n) + 1 = (\text{multiple of 3}) + 1$$

$$55b. \quad \text{no; } (3n + 2)^2 = 9n^2 + 12n + 4 =$$

$$3(3n^2 + 4n + 1) + 1 = (\text{multiple of 3}) + 1 \quad 56. \quad V =$$

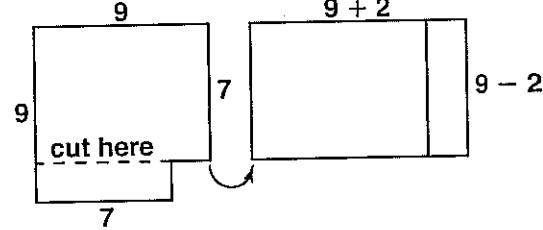
$$\frac{4}{3}\pi(r + 3)^3 = \frac{4}{3}\pi(r + 3)(r + 3)(r + 3) =$$

$$\frac{4}{3}\pi(r + 3)(r^2 + 6r + 9) =$$

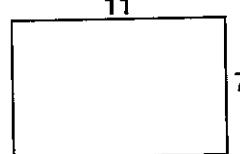
$$\frac{4}{3}\pi(r^3 + 6r^2 + 9r + 3r^2 + 18r + 27) =$$

$$\frac{4}{3}\pi(r^3 + 9r^2 + 27r + 27) = \frac{4}{3}\pi r^3 + 12\pi r^2 + 36\pi r + 36\pi$$

57a.



57b.



$$58. \quad (9x - 1)^2 =$$

$$81x^2 - 18x + 1;$$

the answer is D.

$$59. \quad (b^7 + 2)^2 =$$

$$b^{14} + 4b^7 + 4; \text{ the answer is F.}$$

$$60. \quad A. \quad (3a - 10)(3a + 10) = 9a^2 - 100$$

$$B. \quad (9b - 10)(b - 10) = 9b^2 - 100b + 100; \text{ the answer is C.}$$

$$61. \quad A. \quad (4a - 6)(5a + 1) = 20a^2 - 26a - 6$$

$$B. \quad (8b - 7)(3b + 9) = 24b^2 + 51b - 63; \text{ the answer is E.}$$

$$62. \quad A. \quad (7a + 3)(8a + 2) = 56a^2 + 38a + 6$$

$$B. \quad (12b - 1)(b - 6) = 12b^2 - 73b + 6; \text{ the answer is C.}$$

63. [2] The middle term is twice the product of the first and last terms;  $2(3x)(-4y) = -24xy$ .

$$64. \quad (k + 7)(k - 9) = k^2 - 9k + 7k - 63 =$$

$$k^2 - 2k - 63 \quad 65. \quad (2x - 11)(x - 6) = 2x^2 - 23x + 66$$

$$66. \quad (5p + 4)(3p - 1) = 15p^2 + 7p - 4$$

$$67. \quad (3y + 1)(y + 1) = 3y^2 + 4y + 1$$

$$68. \quad (4h - 2)(6h + 1) = 24h^2 - 8h - 2$$

$$69. \quad (9b + 7)(8b + 2) = 72b^2 + 74b + 14$$

$$70. \quad (2w^2 + 5)(w + 8) = 2w^3 + 16w^2 + 5w + 40$$

71.  $(r - 7)(r^2 + 3r - 9) = r^3 + 3r^2 - 9r - 7r^2 - 21r + 63 = r^3 - 4r^2 - 30r + 63$   
 72.  $(5m^2 - 2)(6m^3 + 4m) = 30m^5 + 8m^3 - 8m$   
 73.  $8713 = 8.713 \times 10^3$  74.  $0.031 = 3.1 \times 10^{-2}$   
 75.  $68,952 = 6.8952 \times 10^4$  76. 1.2 million =  $1.2 \times 10^6$   
 77.  $11 = 1.1 \times 10^1$  78.  $523 = 5.23 \times 10^2$  79. 6 billion =  $6 \times 10^9$  80.  $0.72 = 7.2 \times 10^{-1}$

## INVESTIGATION

page 480

1.  $x^2 + 8x + 15 = (x + 3)(x + 5)$  2.  $x^2 + 4x + 4 = (x + 2)(x + 2)$  3.  $x^2 + 8x + 7 = (x + 7)(x + 1)$   
 4.  $2x^2 + 7x + 3 = (2x + 1)(x + 3)$  5.  $4x^2 + 12x + 5 = (2x + 5)(2x + 1)$  6.  $6x^2 + 7x + 2 = (3x + 2)(2x + 1)$   
 7.  $x^2 + 3x + 5$  cannot be written as a product of two binomials. 8.  $\blacksquare = 7, (2x + 3)(x + 2); \blacksquare = 8, (2x + 2)(x + 3)$  or  $(2x + 6)(x + 1); \blacksquare = 13, (2x + 1)(x + 6)$

## 9.5 Factoring Trinomials of the Type $x^2 + bx + c$

pages 481–485

Check Skills You'll Need p. 481 For complete solutions see Daily Skills Check and Lesson Quiz Transparencies or Presentation Pro CD-ROM.

1. 1, 2, 3, 4, 6, 8, 12, 24 2. 1, 2, 3, 4, 6 12 3. 1, 2, 3, 6, 9, 18, 27, 54 4. 1, 3, 5, 15 5. 1, 2, 3, 4, 6, 9, 12, 18, 36 6. 1, 2, 4, 7, 8, 14, 28, 56 7. 1, 2, 4, 8, 16, 32, 64 8. 1, 2, 3, 4, 6, 8, 12, 16, 24, 32, 48, 96

Check Understanding 1a.  $10 = 1 \cdot 10 = 2 \cdot 5$ ;

$$2 + 5 = 7; \text{check: } (g + 2)(g + 5) = g^2 + 5g + 2g + 10 = g^2 + 7g + 10 \checkmark$$

1b.  $20 = 1 \cdot 20 = 2 \cdot 10 = 4 \cdot 5; 1 + 20 = 21$ ;

$$\text{check: } (v + 1)(v + 20) = v^2 + 20v + v + 20 = v^2 + 21v + 20 \checkmark$$

1c.  $30 = 1 \cdot 30 = 2 \cdot 15 = 3 \cdot 10 = 5 \cdot 6; 3 + 10 = 13$ ;

$$\text{check: } (a + 3)(a + 10) = a^2 + 10a + 3a + 30 = a^2 + 13a + 30 \checkmark$$

2a.  $25 = -1 \cdot -25 = -5 \cdot -5; -5 + (-5) = -10$ ;

$$\text{check: } (k - 5)(k - 5) = k^2 - 5k - 5k + 25 = k^2 - 10k + 25 \checkmark$$

2b.  $18 = -1 \cdot -18 = -2 \cdot -9 = -3 \cdot -6; -2 + (-9) = -11$ ;

$$\text{check: } (x - 2)(x - 9) = x - 11 + 18 \checkmark$$

2c.  $36 = -1 \cdot -36 = -2 \cdot -18 = -3 \cdot -12 =$

$$-4 \cdot -9 = -6 \cdot -6; -3 + (-12) = -15$$

$$\text{check: } (q - 3)(q - 12) = q^2 - 15q + 36 \checkmark$$

3a.  $-20 = -1 \cdot 20 = 1 \cdot -20 = -2 \cdot 10 = 2 \cdot -10 =$

$$-4 \cdot 5 = 4 \cdot -5; -2 + 10 = 8$$

$$\text{check: } (m - 2)(m + 10) = m^2 + 10m - 2m - 20 = m^2 + 8m - 20 \checkmark$$

3b.  $-40 = -1 \cdot 40 = 1 \cdot -40 = -2 \cdot 20 = 2 \cdot -20 = -4 \cdot 10 = 4 \cdot -10 = -5 \cdot 8 = 5 \cdot -8; 5 + (-8) = -3$

$$\text{check: } (p + 5)(p - 8) = p^2 - 3p - 40 \checkmark$$

3c.  $-56 = -1 \cdot 56 = 1 \cdot -56 = -2 \cdot 28 = 2 \cdot -28 = -4 \cdot 14 = 4 \cdot -14 = -7 \cdot 8 = 7 \cdot -8; 7 + (-8) = -1$

$$\text{check: } (y + 7)(y - 8) = y^2 - y - 56 \checkmark$$

4a.  $24 = 1 \cdot 24 = 2 \cdot 12 = 3 \cdot 8 = 4 \cdot 6; 3 + 8 = 11$ ;

$$\text{check: } (x + 3y)(x + 8y) = x^2 + 11xy + 24y^2 \checkmark$$

- 4b.  $-48 = -1 \cdot 48 = 1 \cdot 48 = -2 \cdot 24 = 2 \cdot -24 = -3 \cdot 16 = 3 \cdot -16 = -4 \cdot 12 = 4 \cdot -12 = -6 \cdot 8 = 6 \cdot -8; -6 + 8 = 2$ ;  
 check:  $(v - 6w)(v + 8w) = v^2 + 2vw - 48w^2 \checkmark$
- 4c.  $-60 = -1 \cdot 60 = 1 \cdot -60 = -2 \cdot 30 = 2 \cdot -30 = -3 \cdot 20 = 3 \cdot -20 = -4 \cdot 15 = 4 \cdot -15 = -6 \cdot 10 = 6 \cdot -10; 3 + (-20) = -17$ ;  
 check:  $(m + 3n)(m - 20n) = m^2 - 17mn - 60n^2 \checkmark$
- Exercises 5.  $3 \cdot 1 = 3; 3 + 1 = 4; r^2 + 4r + 3 = (r + 3)(r + 1)$  6.  $-2 \cdot -1 = 2; -2 + (-1) = -3; n^2 - 3n + 2 = (n - 2)(n - 1)$  7.  $3 \cdot 2 = 6; 3 + 2 = 5; k^2 + 5k + 6 = (k + 3)(k + 2)$  8.  $4 \cdot 2 = 8; 4 + 2 = 6; y^2 + 6y + 8 = (y + 4)(y + 2)$  9.  $-1 \cdot -1 = 1; -1 + (-1) = -2; x^2 - 2x + 1 = (x - 1)(x - 1)$  10.  $18 \cdot 1 = 18; 18 + 1 = 19; p^2 + 19p + 18 = (p + 18)(p + 1)$  11.  $-2 \cdot -14 = 28; -2 + (-14) = -16; k^2 - 16k + 28 = (k - 2)(k - 14)$  12.  $5 \cdot 1 = 6; 5 + 1 = 6; w^2 + 6w + 5 = (w + 5)(w + 1)$  13.  $-8 \cdot -1 = 8; -8 + (-1) = -9; m^2 - 9m + 8 = (m - 8)(m - 1)$  14.  $2 \cdot 19 = 38; 2 + 19 = 21; d^2 + 21d + 38 = (d + 2)(d + 19)$  15.  $-6 \cdot -7 = 42; -6 + -7 = -13; t^2 - 13t + 42 = (t - 6)(t - 7)$  16.  $-3 \cdot -15 = 45; -3 + (-15) = -18; q^2 - 18q + 45 = (q - 3)(q - 15)$  17.  $m^2 + 3m - 10 = (m - 2)(m + 5)$  18.  $v^2 - 2v - 24 = (v + 4)(v - 6)$  19.  $k^2 - 8k - 9 = (k + 1)(k - 9)$  20.  $q^2 + 3q - 18 = (q - 3)(q + 6)$  21.  $-1 \cdot 4 = -4; -1 + 4 = 3; x^2 + 3x - 4 = (x - 1)(x + 4)$  22.  $-4 \cdot 2 = -8; -4 + 2 = -2; q^2 - 2q - 8 = (q - 4)(q + 2)$  23.  $-4 \cdot 5 = -20; -4 + 5 = -1; y^2 + y - 20 = (y - 4)(y + 5)$  24.  $-1 \cdot 17 = -17; -1 + 17 = 16; h^2 + 16h - 17 = (h - 1)(h + 17)$  25.  $-16 \cdot 2 = -32; -16 + 2 = -14; x^2 - 14x - 32 = (x - 16)(x + 2)$  26.  $-4 \cdot 10 = -40; -4 + 10 = 6; d^2 + 6d - 40 = (d - 4)(d + 10)$  27.  $-15 \cdot 2 = -30; -15 + 2 = -13; m^2 - 13m - 30 = (m - 15)(m + 2)$  28.  $-6 \cdot 9 = -54; -6 + 9 = 3; p^2 + 3p - 54 = (p - 6)(p + 9)$  29.  $-18 \cdot 3 = -54; -18 + 3 = -15; p^2 - 15p - 54 = (p - 18)(p + 3)$  30. A 31. B 32. B 33.  $-2 \cdot 9 = -18; -2 + 9 = 7; t^2 + 7tv - 18v^2 = (t - 2v)(t + 9v)$  34.  $7 \cdot 5 = 35; 7 + 5 = 12; x^2 + 12xy + 35y^2 = (x + 7y)(x + 5y)$  35.  $-8 \cdot -2 = 16; -8 + (-2) = -10; p^2 - 10pq + 16q^2 = (p - 8q)(p - 2q)$  36.  $-9 \cdot 6 = -54; -9 + 6 = -3; (p - 8q)(p - 2q) = (m - 9n)(m + 6n)$  37.  $17 \cdot 1 = 17; m^2 - 3mn - 54n^2 = (h + 17j)(h + j)$  38.  $-13 \cdot 3 = -39; -13 + 3 = -10; x^2 - 10xy - 39y^2 = (x - 13y)(x + 3y)$  39–40. Answers may vary. Samples are given.
39.  $(x + 2)(x - 5); \blacksquare = 10$   
 $(x + 3)(x - 6); \blacksquare = 18$   
 $(x + 4)(x - 7); \blacksquare = 28$
40.  $(x - 1)(x + 2); \blacksquare = 2$   
 $(x - 3)(x + 4); \blacksquare = 12$   
 $(x - 4)(x + 5); \blacksquare = 20$
41.  $(x + 1)(x + 12); \blacksquare = 13$   
 $(x + 2)(x + 6); \blacksquare = 8$   
 $(x + 3)(x + 4); \blacksquare = 7$

- 42.** Let  $x^2 + bx + c = (x + p)(x + q)$ . **42a.** If  $c > 0$ , then  $p$  and  $q$  must be of the same sign. If  $b > 0$ , then  $p$  and  $q$  are both positive. If  $b < 0$ , then  $p$  and  $q$  are negative. **42b.** If  $c < 0$ , then  $p$  and  $q$  are of opposite sign. **43.**  $8 \cdot 2 = 16$ ;  $8 + 2 = 10$ ;  $k^2 + 10k + 16 = (k + 8)(k + 2)$  **44.**  $-2 \cdot 12 = -24$ ;  $-2 + 12 = 10$ ;  $m^2 + 10m - 24 = (m - 2)(m + 12)$  **45.**  $-4 \cdot 14 = -56$ ;  $-4 + 14 = 10$ ;  $n^2 + 10n - 56 = (n - 4)(n + 14)$  **46.**  $8 \cdot 12 = 96$ ;  $8 + 12 = 20$ ;  $g^2 + 20g + 96 = (g + 8)(g + 12)$  **47.**  $-5 \cdot 13 = -65$ ;  $-5 + 13 = 8$ ;  $x^2 + 8x - 65 = (x - 5)(x + 13)$  **48.**  $3 \cdot 25 = 75$ ;  $3 + 25 = 28$ ;  $t^2 + 28t + 75 = (t + 3)(t + 25)$  **49.**  $-14 \cdot 3 = -42$ ;  $-14 + 3 = -11$ ;  $x^2 - 11x - 42 = (x - 14)(x + 3)$  **50.**  $2 \cdot 21 = 42$ ;  $2 + 21 = 23$ ;  $k^2 + 23k + 42 = (k + 2)(k + 21)$  **51.**  $-3 \cdot 17 = -51$ ;  $-3 + 17 = 14$ ;  $m^2 + 14m - 51 = (m - 3)(m + 17)$  **52.**  $4 \cdot 25 = 100$ ;  $4 + 25 = 29$ ;  $x^2 + 29xy + 100y^2 = (x + 4y)(x + 25y)$  **53.**  $-15 \cdot 5 = -75$ ;  $-15 + 5 = -10$ ;  $t^2 - 10t - 75 = (t - 15)(t + 5)$  **54.**  $-3 \cdot -16 = 48$ ;  $-3 + (-16) = -19$ ;  $d^2 - 19de + 48e^2 = (d - 3e)(d - 16e)$  **55.**  $4x^2 + 10x + 2x + 5 = 4x^2 + (10 + 2)x + 5 = 4x^2 + 12x + 5$ ;  $4x^2 + 12x + 5 = (2x + 1)(2x + 5)$  **56.**  $6x^2 + 9x + 4x + 6 = 6x^2 + (9 + 4)x + 6 = 6x^2 + 13x + 6$ ;  $6x^2 + 13x + 6 = (3x + 2)(2x + 3)$  **57a.** The signs of  $a$  and  $b$  must be opposite. **57b.** Because the middle term is negative, the number with the larger absolute value must be negative. So  $a$  must be a negative integer. **58a.** The signs of  $a$  and  $b$  must be opposite. **58b.** Because the middle term is positive, the number with the larger absolute value must be positive. So  $b$  is a negative integer. **59.**  $7 \cdot 5 = 35$ ;  $7 + 5 = 12$ ;  $x^{12} + 12x^6 + 35 = x^{6+6} + 12x^6 + 35 = (x^6 + 7)(x^6 + 5)$  **60.**  $-3 \cdot 8 = -24$ ;  $-3 + 8 = 5$ ;  $t^8 + 5t^4 - 24 = t^{4+4} + 5t^4 - 24 = (t^4 - 3)(t^4 + 8)$  **61.**  $-16 \cdot -5 = -80$ ;  $-16 + (-5) = -21$ ;  $r^6 - 21r^3 + 80 = r^{3+3} - 21r^3 + 80 = (r^3 - 16)(r^3 - 5)$  **62.**  $17 \cdot 1 = 17$ ;  $17 + 1 = 18$ ;  $m^{10} + 18m^5 + 17 = m^{5+5} + 18m^5 + 17 = (m^5 + 17)(m^5 + 1)$  **63.**  $-24 \cdot 5 = -120$ ;  $-24 + 5 = -21$ ;  $x^{12} - 19x^6 - 120 = x^{6+6} - 19x^6 - 120 = (x^6 - 24)(x^6 + 5)$  **64.**  $-4 \cdot 18 = -72$ ;  $-4 + 18 = 14$ ;  $p^6 + 14p^3 - 72 = p^{3+3} + 14p^3 - 72 = (p^3 - 4)(p^3 + 18)$  **65.**  $72 \div 16 = 4.5$ ; the answer is B. **66.**  $-36 = -4 \cdot 9$ ;  $-4 + 9 = 5$ ; the answer is F. **67.** A.  $25 = 5 \cdot 5$ ; sum = 10 B.  $24 = 4 \cdot 6$ ; sum = 10 C.  $21 = 3 \cdot 7$ ; sum = 10 D.  $18 = 1 \cdot 18 = 2 \cdot 9 = 3 \cdot 6$ ; no sum = 10; the answer is D. **68.** Area =  $x^2 + 11x + 18$ ; the answer is I. **69.**  $6 \cdot 12 = 72$ ;  $6 + 12 = 18$ ; the answer is A. **70.**  $-10 \cdot -5 = 50$ ;  $-10 + (-5) = -15$ ; the answer is F. **71.** Terms in factors must be of opposite sign. Factor  $-40$ ;  $-40 = -1 \cdot 40 = 1 \cdot -40 = -2 \cdot 20 = 2 \cdot -20 = -4 \cdot 10 = 4 \cdot -10 = -5 \cdot 8 = 5 \cdot -8$ ; search for products whose sum =  $-18$ ; find  $2 + (-20) = -18$ ; factors are  $(x + 2)(x - 20) = x^2 - 18 - 40$  [1] correct factors only OR explanation only **72.**  $(x + 4)(x + 4) = (x)^2 + 2x(4) + (4)^2 = x^2 + 8x + 16$  **73.**  $(w - 6)(w - 6) = (w)^2 - 2w(6) + (6)^2 = w^2 - 12w + 36$  **74.**  $(r - 5)(r + 5) = (r)^2 - (5)^2 =$

$$r^2 - 25$$

$$\text{75. } (2q + 7)(2q + 7) = (2q)^2 + 2(2q)(7) + (7)^2 = 4q^2 + 28q + 49$$

$$\text{76. } (8v - 2)(8v + 2) = (8v)^2 - (2)^2 = 64v^2 - 4$$

$$\text{77. } (3a - 9)(3a - 9) = (3a)^2 - 2(3a)(9) + (9)^2 = 9a^2 - 54a + 81$$

$$\text{78. } (3a - 5)(3a + 5) = (3a)^2 - (5)^2 = 9a^2 - 25$$

$$\text{79. } (6t + 9)(6t + 9) = (6t)^2 + 2(6t)(9) + (9)^2 = 36t^2 + 108t + 81$$

$$\text{80. } (2x + 8y)(2x - 8y) = (2x)^2 - (8y)^2 = 4x^2 - 64y^2$$

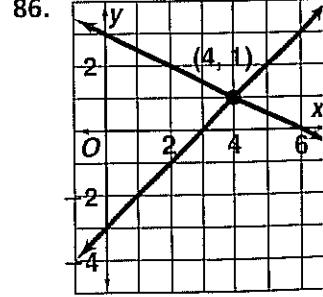
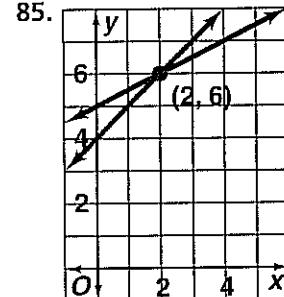
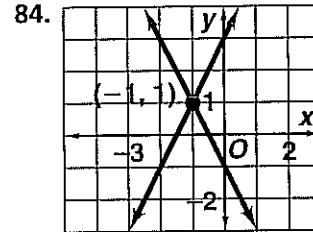
$$\text{81. } \begin{aligned} 40 + 18x &= 220 - 12x \\ 40 + 30x &= 220 \\ 30x &= 180 \\ x &= 6 \end{aligned}$$

The accounts will be the same after 6 weeks.

$$\text{82. } \begin{aligned} m + n &= 42 \\ n &= 42 - m \\ 2m - 63 &= n \\ 2m - 63 &= 42 - m \\ 3m - 63 &= 42 \\ 3m &= 105 \\ m &= 35 \\ n &= 42 - 35 = 7 \end{aligned}$$

$$\text{83a. } \begin{aligned} b + d &= 129 \\ 119.99b + 149.99d &= 16,918.71 \\ b &= 129 - d \\ 119.99(129 - d) + 149.99d &= 16,918.71 \\ 30d &= 16,918.71 - 15,478.71 \\ 30d &= 1440 \\ d &= 48 \\ b &= 129 - 48 = 81 \end{aligned}$$

81 basic players, 48 deluxe players



## 9-6 Factoring Trinomials of the Type $ax^2 + bx + c$ pages 486–489

Check Skills You'll Need p. 486 For complete solutions see Daily Skills Check and Lesson Quiz Transparencies or Presentation Pro CD-ROM.

1.  $6x$  2. 7 3. 2 4.  $(x + 1)(x + 4)$  5.  $(y - 7)(y + 4)$
6.  $(t - 5)(t - 6)$

### Check Understanding

- 1a.  $2y^2 + 5y + 2$   
 F    O    I    L  
 $1 \cdot 2 + 1 \cdot 2 = 4$     $1 \cdot 2$   
 $1 \cdot 2 + 2 \cdot 2 = 5 \checkmark$     $2 \cdot 1$   
 $(y+2)(2y+1) = 2y^2 + 5y + 2$
- 1b.  $6n^2 - 23n + 7$   
 F    O    I    L  
 $1 \cdot 6 + 1 \cdot -7 = -13$     $-1 \cdot -7$   
 $1 \cdot 6 + 1 \cdot -1 = -43$     $-7 \cdot -1$   
 $2 \cdot 3 + 2 \cdot -7 = -17$     $-1 \cdot -7$   
 $2 \cdot 3 + 2 \cdot -1 = -23 \checkmark$     $-7 \cdot -1$   
 $(2n-7)(3n-1) = 6n^2 - 23n + 7$
- 1c.  $2y^2 - 5y + 2$   
 F    O    I    L  
 $1 \cdot 2 + 1 \cdot -2 = -4$     $-1 \cdot -2$   
 $1 \cdot 2 + 1 \cdot -1 = -5 \checkmark$     $-2 \cdot -1$   
 $(y-2)(2y-1) = 2y^2 - 5y + 2$
- 2a.  $5d^2 - 14d - 3$   
 F    O    I    L  
 $1 \cdot 5 + 1 \cdot -3 = 2$     $1 \cdot -3$   
 $1 \cdot 5 + 1 \cdot -1 = 14$     $3 \cdot -1$   
 $1 \cdot 5 + 1 \cdot 1 = -14 \checkmark$     $-3 \cdot 1$   
 $(d-3)(5d+1) = 5d^2 - 14d - 3$
- 2b.  $2n^2 + 5n - 3$   
 F    O    I    L  
 $1 \cdot 2 + 1 \cdot -3 = -1$     $1 \cdot -3$   
 $1 \cdot 2 + 1 \cdot 3 = 1 \checkmark$     $-1 \cdot 3$   
 $(n-1)(2n+3) = 2n^2 + n - 3$
- 2c.  $20p^2 - 31p - 9$   
 F    O    I    L  
 $1 \cdot 20 + 1 \cdot -9 = 11$     $1 \cdot -9$   
 $1 \cdot 20 + 1 \cdot -3 = 57$     $3 \cdot -3$   
 $2 \cdot 10 + 2 \cdot -9 = -8$     $1 \cdot -9$   
 $2 \cdot 10 + 2 \cdot -3 = 24$     $3 \cdot -3$   
 $4 \cdot 5 + 4 \cdot -9 = -31 \checkmark$     $1 \cdot -9$   
 $(4p+1)(5p-9) = 20p^2 - 31p - 9$
- 3a.  $v^2 - 6v + 5$   
 F    O    I    L  
 $1 \cdot 1 + 1 \cdot -5 = -6 \checkmark$     $-1 \cdot -5$   
 $2(v-1)(v-5) = 2(v^2 - 6v + 5) = 2v^2 - 12v + 10$
- 3b.  $2y^2 + 7y + 3$   
 F    O    I    L  
 $1 \cdot 2 + 1 \cdot 3 = 5$     $1 \cdot 3$   
 $1 \cdot 2 + 1 \cdot 1 = 7 \checkmark$     $3 \cdot 1$   
 $2(y+3)(2y+1) = 2(2y^2 + 7y + 3) = 4y^2 + 14y + 6$

- 3c.  $3k^2 - 2k - 1$   
 F    O    I    L  
 $1 \cdot 3 + 1 \cdot -1 = 2$     $1 \cdot -1$   
 $1 \cdot 3 + 1 \cdot 1 = -2 \checkmark$     $-1 \cdot 1$   
 $6(k-1)(3k+1) = 6(3k^2 - 2k - 1) = 18k^2 - 12k - 6$
- Exercises**
1.  $2n^2 + 15n + 7$   
 F    O    I    L  
 $1 \cdot 2 + 1 \cdot 7 = 9$     $1 \cdot 7$   
 $1 \cdot 2 + 1 \cdot 1 = 15 \checkmark$     $7 \cdot 1$   
 $(n+7)(2n+1) = 2n^2 + 15n + 7$
2.  $7d^2 - 50d + 7$   
 F    O    I    L  
 $1 \cdot 7 + 1 \cdot 1 = 7 \cdot 7 = 50 \checkmark$     $7 \cdot 1$   
 $(d+7)(7d+1) = 7d^2 + 50d + 7$
3.  $11w^2 - 14w + 3$   
 F    O    I    L  
 $1 \cdot 11 + 1 \cdot -3 = -1 \cdot 11 = -14 \checkmark$     $-1 \cdot -3$   
 $(w-1)(11w+3) = 11w^2 - 14w + 3$
4.  $3x^2 - 17x + 10$   
 F    O    I    L  
 $1 \cdot 3 + 1 \cdot -10 = -1 \cdot 3 = -13$     $-1 \cdot -10$   
 $1 \cdot 3 + 1 \cdot -2 = -5 \cdot 3 = -17 \checkmark$     $-5 \cdot -2$   
 $(x-5)(3x-2) = 3x^2 - 17x + 10$
5.  $6t^2 + 25t + 11$   
 F    O    I    L  
 $1 \cdot 6 + 1 \cdot 1 = 11 \cdot 6 = 67$     $11 \cdot 1$   
 $2 \cdot 3 + 2 \cdot 11 = 1 \cdot 3 = 25 \checkmark$     $1 \cdot 11$   
 $(2t+1)(3t+11) = 6t^2 + 25t + 11$
6.  $3d^2 - 17d + 20$   
 F    O    I    L  
 $1 \cdot 3 + 1 \cdot -20 = -1 \cdot 3 = -23$     $-1 \cdot -20$   
 $1 \cdot 3 + 1 \cdot -5 = -4 \cdot 3 = -17 \checkmark$     $-4 \cdot -5$   
 $(d-4)(3d-5) = 3d^2 - 17d + 20$
7.  $16m^2 + 26m + 9$   
 F    O    I    L  
 $2 \cdot 8 + 2 \cdot 9 = 1 \cdot 8 = 26 \checkmark$     $1 \cdot 9$   
 $(2m+1)(8m+9) = 16m^2 + 26m + 9$
8.  $15p^2 - 26p + 11$   
 F    O    I    L  
 $1 \cdot 15 + 1 \cdot -11 = -1 \cdot 15 = -26 \checkmark$     $-1 \cdot -11$   
 $(p-1)(15p-11) = 15p^2 - 26p + 11$
9.  $8y^2 + 30y + 13$   
 F    O    I    L  
 $1 \cdot 8 + 1 \cdot 13 = 1 \cdot 8 = 21$     $1 \cdot 13$   
 $1 \cdot 8 + 1 \cdot 1 = 13 \cdot 8 = 105$     $13 \cdot 1$   
 $2 \cdot 4 + 2 \cdot 13 = 1 \cdot 4 = 30 \checkmark$     $1 \cdot 13$   
 $(2y+1)(4y+13) = 8y^2 + 30y + 13$

10. $2y^2$	$+ 35y$	$+ 17$
<input type="checkbox"/> F	<input type="checkbox"/> O	<input type="checkbox"/> I
$1 \cdot 2$	$1 \cdot 17 + 1 \cdot 2 = 19$	$1 \cdot 17$
$1 \cdot 2$	$1 \cdot 1 + 17 \cdot 2 = 35 \checkmark$	$17 \cdot 1$
$(y + 17)(2y + 1) = 2y^2 + 35y + 17$		
11. $7x^2$	$- 30x$	$+ 27$
<input type="checkbox"/> F	<input type="checkbox"/> O	<input type="checkbox"/> I
$1 \cdot 7$	$1 \cdot -27 + -1 \cdot 7 = -34$	$-1 \cdot -27$
$1 \cdot 7$	$1 \cdot -1 + -27 \cdot 7 = -190$	$-27 \cdot -1$
$1 \cdot 7$	$1 \cdot -9 + -3 \cdot 7 = -30 \checkmark$	$-3 \cdot -9$
$(x - 3)(7x - 9) = 7x^2 - 30x - 27$		
12. $8x^2$	$+ 18x$	$+ 9$
<input type="checkbox"/> F	<input type="checkbox"/> O	<input type="checkbox"/> I
$1 \cdot 8$	$1 \cdot 9 + 1 \cdot 8 = 17$	$1 \cdot 9$
$1 \cdot 8$	$1 \cdot 3 + 3 \cdot 8 = 27$	$3 \cdot 3$
$2 \cdot 4$	$2 \cdot 9 + 1 \cdot 4 = 22$	$1 \cdot 9$
$2 \cdot 4$	$2 \cdot 3 + 3 \cdot 4 = 18 \checkmark$	$3 \cdot 3$
$(2x + 3)(4x + 3) = 8x^2 + 18x + 9$		
13. $2t^2$	$- t$	$- 3$
<input type="checkbox"/> F	<input type="checkbox"/> O	<input type="checkbox"/> I
$1 \cdot 2$	$1 \cdot -3 + 1 \cdot 2 = -1 \checkmark$	$1 \cdot -3$
$(t + 1)(2t - 3) = 2t^2 - t - 3$		
14. $8y^2$	$- 10y$	$- 3$
$1 \cdot 8$	$1 \cdot -3 + 1 \cdot 8 = 5$	$1 \cdot -3$
$1 \cdot 8$	$1 \cdot -1 + 3 \cdot 8 = 23$	$3 \cdot -1$
$2 \cdot 4$	$2 \cdot -1 + 1 \cdot 4 = 2$	$1 \cdot -3$
$2 \cdot 4$	$2 \cdot -1 + 3 \cdot 4 = 10$	$3 \cdot -1$
$2 \cdot 4$	$2 \cdot 1 + -3 \cdot 4 = -10 \checkmark$	$-3 \cdot 1$
$(2y - 3)(4y + 1) = 8y^2 - 10y - 3$		
15. $2q^2$	$- 11q$	$- 21$
$1 \cdot 2$	$1 \cdot -21 + 1 \cdot 2 = -19$	$1 \cdot -21$
$1 \cdot 2$	$1 \cdot -7 + 3 \cdot 2 = -1$	$3 \cdot -7$
$2 \cdot 1$	$2 \cdot -7 + 3 \cdot 1 = -11 \checkmark$	$3 \cdot -7$
$(2q + 3)(q - 7) = 2q^2 - 11q - 21$		
16. $7x^2$	$- 20x$	$- 3$
$1 \cdot 7$	$1 \cdot -1 + 3 \cdot 7 = 20$	$3 \cdot -1$
$1 \cdot 7$	$1 \cdot 1 + -3 \cdot 7 = -20 \checkmark$	$-3 \cdot 1$
$(x - 3)(7x + 1) = 7x^2 - 20x - 3$		
17. $13p^2$	$+ 8p$	$- 5$
$1 \cdot 13$	$1 \cdot -5 + 1 \cdot 13 = 8 \checkmark$	$1 \cdot -5$
$(p + 1)(13p - 5) = 13p^2 + 8p - 5$		
18. $5k^2$	$- 2k$	$- 7$
$1 \cdot 5$	$1 \cdot -7 + 1 \cdot 5 = -2 \checkmark$	$1 \cdot -7$
$(k + 1)(5k - 7) = 5k^2 - 2k - 7$		
19. $10w^2$	$+ 11w$	$- 8$
$1 \cdot 10$	$1 \cdot -8 + 1 \cdot 10 = 2$	$1 \cdot -8$
$1 \cdot 10$	$1 \cdot -4 + 2 \cdot 10 = 16$	$2 \cdot -4$
$1 \cdot 10$	$1 \cdot -2 + 4 \cdot 10 = 38$	$4 \cdot -2$

20. $12d^2$	$- d$	$- 20$
$2 \cdot 6$	$2 \cdot -10 + 2 \cdot 6 = -8$	$2 \cdot -10$
$2 \cdot 6$	$2 \cdot -5 + 4 \cdot 6 = 14$	$4 \cdot -5$
$3 \cdot 4$	$3 \cdot -5 + 4 \cdot 4 = 1$	$4 \cdot -5$
$3 \cdot 4$	$3 \cdot 5 + -4 \cdot 4 = -1 \checkmark$	$-4 \cdot 5$
$(3d - 4)(4d + 5) = 12d^2 - d - 20$		
21. $14n^2$	$+ 23n$	$- 15$
$2 \cdot 7$	$2 \cdot -15 + 1 \cdot 7 = -23$	$1 \cdot -15$
$2 \cdot 7$	$2 \cdot 15 + -1 \cdot 7 = 23 \checkmark$	$-1 \cdot 15$
$(2n - 1)(7n + 15) = 14n^2 + 23n - 15$		
22. $3m^2$	$- 4m$	$+ 1$
<input type="checkbox"/> F	<input type="checkbox"/> O	<input type="checkbox"/> I
$1 \cdot 3$	$1 \cdot -1 + -1 \cdot 3 = -4 \checkmark$	$-1 \cdot -1$
$8(m - 1)(3m - 1) = 8(3m^2 - 4m + 1) =$		
$24m^2 - 32m + 8$		
23. $3v^2$	$- 10v$	$+ 7$
$1 \cdot 3$	$1 \cdot -7 + -1 \cdot 3 = -10 \checkmark$	$-7$
$7(v - 1)(3v - 7) = 7(3v^2 - 10v + 7) = 21v^2 - 70v + 4$		
24. $3t^2$	$+ 13t$	$+ 12$
$1 \cdot 3$	$1 \cdot 4 + 3 \cdot 3 = 13 \checkmark$	$3 \cdot 4$
$2(t + 3)(3t + 4) = 2(3t^2 + 13t + 12) = 6t^2 + 26t + 24$		
25. $5x^2$	$- 2x$	$- 3$
$1 \cdot 5$	$1 \cdot -3 + 1 \cdot 5 = 2$	$1 \cdot -3$
$1 \cdot 5$	$1 \cdot 3 + -1 \cdot 5 = -2 \checkmark$	$-1 \cdot 3$
$5(x - 1)(5x + 3) = 5(5x^2 - 2x - 3) = 25x^2 - 10x - 15$		
26. $p^2$	$+ 7p$	$+ 6$
$1 \cdot 1$	$1 \cdot 6 + 1 \cdot 1 = 7 \checkmark$	$1 \cdot 6$
$11(p + 1)(p + 6) = 11(p^2 + 7p + 6) = 11p^2 + 77p + 6$		
27. $12v^2$	$+ 5v$	$- 3$
$3 \cdot 4$	$3 \cdot -3 + 1 \cdot 4 = -5$	$1 \cdot -3$
$3 \cdot 4$	$3 \cdot 3 + -1 \cdot 4 = 5 \checkmark$	$-1 \cdot 3$
$2(3v - 1)(4v + 3) = 2(12v^2 + 5v - 3) =$		
$24v^2 + 10v - 6$		
28. Samples:		$\frac{x}{14}$
$4g^2 + xg + 10 = (g + 1)(4g + 10)$		14
$= (g + 2)(4g + 5)$		13
$= (g + 5)(4g + 2)$		22
$= (g + 10)(4g + 1)$		41
$= (2g + 1)(2g + 10)$		22
$= (2g + 2)(2g + 5)$		14
29. Samples:		
$15m^2 + xm - 24 = (m + 1)(15m - 24)$		-9
$= (m - 1)(15m + 24)$		9
$= (m - 24)(15m + 1)$		-359
$= (3m - 1)(5m + 24)$		67
$= (3m - 24)(5m + 1)$		-117
$= (3m + 24)(5m - 1)$		117

## 30. Samples:

$$\begin{aligned} 35g^2 + xg - 16 &= (g+1)(35g-16) & 19 \\ &= (g-16)(35g+1) & -559 \\ &= (5g-1)(7g+16) & 73 \\ &= (5g+16)(7g-1) & 107 \end{aligned}$$

31a.  $(2x+2)(x+2); (x+1)(2x+4)$

31b.  $(2x+2)(x+2) = 2x^2 + 6x + 4$ ;  $(x+1)(2x+4) = 2x^2 + 6x + 4$ ; yes  
**31c.**  $(2x+2)(x+2) = 2(x+1)(x+2)$ ;  
 $(x+1)(2x+4) = 2(x+1)(2x+2)$ ; upon complete  
factoring the two expressions are the same.

32. First factor out the GCF = 2;  $50x^2 - 90x + 16 = 2(25x^2 - 45x + 8)$ . Next factor 25 =  $1 \cdot 25 = 5 \cdot 5$  and  
 $8 = 1 \cdot 8 = 2 \cdot 4 = 4 \cdot 2 = 8 \cdot 1$ ; there are 6 possibilities.  
 $25x^2 - 45x + 8 = (px+q)(rx+s)$ ; p, r both positive. q  
and s are both negative in this case.

$$\begin{array}{rccccc} 25x^2 & -45x & +8 \\ 1 \cdot 25 & 1 \cdot -8 + & -1 \cdot 25 = -33 & -1 \cdot -8 \\ 5 \cdot 5 & 5 \cdot -8 + & -1 \cdot 5 = -45 & \checkmark & -1 \cdot -8 \end{array}$$

Check:  $2(5x-1)(5x-8) = 2(25x^2 - 45x + 8) = 50x^2 - 90x + 16$ .

$$\begin{array}{rccccc} 33. 54p^2 & +87p & +28 \\ 1 \cdot 54 & 1 \cdot 28 + & 1 \cdot 54 = 82 & 1 \cdot 28 \\ 1 \cdot 54 & 1 \cdot 7 + & 4 \cdot 54 = 223 & 4 \cdot 7 \\ 2 \cdot 27 & 2 \cdot 28 + & 1 \cdot 27 = 83 & 1 \cdot 28 \\ 2 \cdot 27 & 2 \cdot 14 + & 2 \cdot 27 = 82 & 2 \cdot 14 \\ 3 \cdot 18 & 3 \cdot 28 + & 1 \cdot 18 = 102 & 1 \cdot 28 \\ 3 \cdot 18 & 3 \cdot 7 + & 4 \cdot 18 = 93 & 4 \cdot 7 \\ 6 \cdot 9 & 6 \cdot 7 + & 4 \cdot 9 = 78 & 4 \cdot 7 \\ 6 \cdot 9 & 6 \cdot 4 + & 7 \cdot 9 = 87 & \checkmark & 7 \cdot 4 \end{array}$$

$$(6p+7)(9p+4) = 54p^2 + 87p + 28$$

$$\begin{array}{rccccc} 34. 22r^2 & +19r & +4 \\ 2 \cdot 11 & 2 \cdot 4 + & 1 \cdot 11 = 19 & \checkmark & 1 \cdot 4 \end{array}$$

$$3(2r+1)(11r+4) = 3(22r^2 + 19r + 4) = 66r^2 + 57r + 12$$

$$\begin{array}{rccccc} 35. 14x^2 & -53x & +14 \\ 1 \cdot 14 & 1 \cdot -14 + & -1 \cdot 14 = -28 & -1 \cdot -14 \\ 2 \cdot 7 & 2 \cdot -7 + & -2 \cdot 7 = -28 & -2 \cdot -7 \\ 2 \cdot 7 & 2 \cdot -2 + & -7 \cdot 7 = -53 & \checkmark & -7 \cdot -2 \end{array}$$

$$(2x-7)(7x-2) = 14x^2 - 53x + 14$$

$$36. 28m^2 + 28m - 56 = 28(m^2 + m - 1) = 28(m+2)(m-1)$$

$$\begin{array}{rccccc} 37. 7h^2 & +24h & -16 \\ 1 \cdot 7 & 1 \cdot -8 + & 2 \cdot 7 = 6 & 2 \cdot -8 \\ 1 \cdot 7 & 1 \cdot -4 + & 4 \cdot 7 = 24 & \checkmark & 4 \cdot -4 \end{array}$$

$$3(h+4)(7h-4) = 3(7h^2 + 24h - 16) = 21h^2 + 72h - 48$$

$$\begin{array}{rccccc} 38. 55n^2 & -52n & +12 \\ 5 \cdot 11 & 5 \cdot -12 + & -1 \cdot 11 = -71 & -1 \cdot -12 \\ 5 \cdot 11 & 5 \cdot -6 + & -2 \cdot 11 = -52 & \checkmark & -2 \cdot -6 \end{array}$$

$$(5n-2)(11n-6) = 55n^2 - 52n - 12$$

$$\begin{array}{rccccc} 39. 18y^2 & +57y & -10 \\ 2 \cdot 9 & 2 \cdot -10 + & 1 \cdot 9 = -11 & 1 \cdot -10 \\ 3 \cdot 6 & 3 \cdot -10 + & 1 \cdot 6 = -24 & 1 \cdot -10 \\ 3 \cdot 6 & 3 \cdot -1 + & 10 \cdot 6 = 57 & \checkmark & 10 \cdot -1 \end{array}$$

$$2(3y+10)(6y-1) = 2(18y^2 + 57y - 10) =$$

$$36y^2 + 114y - 20$$

$$\begin{array}{rccccc} 40. 63w^2 & -89w & +30 \\ 7 \cdot 9 & 7 \cdot -10 + & -3 \cdot 9 = -97 & -3 \cdot -10 \\ 7 \cdot 9 & 7 \cdot -6 + & -5 \cdot 9 = -87 & -5 \cdot -6 \\ 7 \cdot 9 & 7 \cdot -5 + & -6 \cdot 9 = -89 & \checkmark & -6 \cdot -5 \end{array}$$

$$(7w-6)(9w-5) = 63w^2 - 89w + 30$$

$$\begin{array}{rccccc} 41. 99q^2 & -92q & +9 \\ 1 \cdot 99 & 1 \cdot -9 + & -1 \cdot 99 = -108 & -1 \cdot -9 \\ 1 \cdot 99 & 1 \cdot -1 + & -9 \cdot 99 = -890 & -9 \cdot -1 \\ 1 \cdot 99 & 1 \cdot -3 + & -3 \cdot 99 = -300 & -3 \cdot -3 \\ 3 \cdot 33 & 3 \cdot -9 + & -1 \cdot 33 = -60 & -1 \cdot -9 \\ 3 \cdot 33 & 3 \cdot -3 + & -3 \cdot 33 = -108 & -3 \cdot -3 \\ 9 \cdot 11 & 9 \cdot -9 + & -1 \cdot 11 = -920 & \checkmark & -1 \cdot -9 \end{array}$$

$$(9q-1)(11q-9) = 99q^2 - 92q + 9$$

42. a and c cannot be factored;  $ax^2 + bx + c$  can be factored as  $(ax+1)(x+c)$  or  $(ax+c)(x+1)$ ; b = ac + 1 or b = a + c; there are two choices for b.

43.  $ax^2 - 12x + c = (px+q)(rx+s)$ ; choose p, r positive; ps + qr = -12; q, s are negative in this case.  
Samples:

p	s	q	r	ps + qr	a = pr	c = qs
1	-1	-1	11	-12	11	1
1	-1	-11	1	-12	1	11
2	-1	-1	10	-12	20	1
2	-1	-10	1	-12	2	10
2	-1	-2	5	-12	10	2
2	-1	-5	2	-12	4	5
3	-1	-1	9	-12	27	1

$$\begin{array}{rccccc} 44. 56x^2 & +43x & +5 \\ 7 \cdot 8 & 7 \cdot 5 + & 1 \cdot 8 = 43 & \checkmark & 1 \cdot 5 \end{array}$$

Mental math showed that 1 · 56 or 2 · 28 would not be helpful.  $x(7x+1)(8x+5) = x(56x^2 + 43x + 5) = 56x^3 + 43x^2 + 5x$

$$\begin{array}{rccccc} 45. 49p^2 & +63pq & -36q^2 \\ 7 \cdot 7 & 7 \cdot -12 + & 3 \cdot 7 = -63 & 3 \cdot -12 \\ 7 \cdot 7 & 7 \cdot 12 + & -3 \cdot 7 = 63 & \checkmark & -3 \cdot 12 \end{array}$$

$$(7p-3q)(7p+12q) = 49p^2 + 63pq - 36q^2$$

$$46. 108g^2h - 162gh + 54h = 54h(2g^2 - 3g + 1) = 54h(2g-1)(g-1) \checkmark$$

**47a.** -2 and -3  
**47b.**  $x^2 + 5x + 6 = (x+2)(x+3)$  **47c.** When y = (x+2)(x+3) = 0, then (x+2) = 0 so x = -2; or (x+3) = 0 so x = -3.

$$48. 12n^2 + 32n - 140 = 4(3n^2 + 8n - 30) = 4(n+5)(3n-7); \text{ the answer is D.}$$

$$\begin{array}{rccccc} 49. 8p^2 + xp + 11 & = (p+1)(8p+11); x = 19 \\ & = (p+11)(8p+1); x = 89 \\ & = (2p+1)(4p+11); x = 26 \\ & = (2p+11)(4p+1); x = 46 \end{array}$$

The answer is G.

$$\begin{array}{rccccc} 50. 13x^2 & +32x & -21 \\ 1 \cdot 13 & 1 \cdot -7 + & 3 \cdot 13 = 32 & \checkmark & 3 \cdot -7 \\ & & (x+3)(13x-7); \text{ the answer is D.} \end{array}$$

51.  $3x^2 + 22x + 24$   
 $1 \cdot 3 \quad 1 \cdot 12 + 2 \cdot 3 = 18$   
 $1 \cdot 3 \quad 1 \cdot 8 + 3 \cdot 3 = 17$   
 $1 \cdot 3 \quad 1 \cdot 6 + 4 \cdot 3 = 18$   
 $1 \cdot 3 \quad 1 \cdot 4 + 6 \cdot 3 = 22 \checkmark$

Sides of rectangle are  $(x + 6)$  and  $(3x + 4)$ . Perimeter is  $2(x + 6) + 2(3x + 4) = 8x + 20$ . The answer is H.

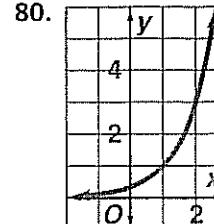
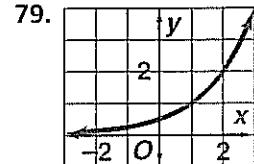
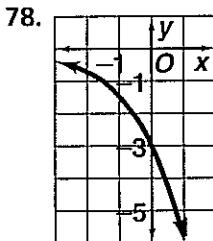
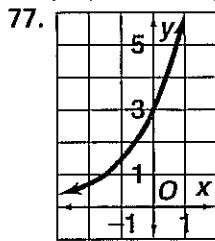
52. The median is the middle value; the answer is D.

53. [2]  $3x^2 + 40x - 75$   
 $1 \cdot 3 \quad 1 \cdot -15 + 5 \cdot 3 = 0$   
 $1 \cdot 3 \quad 1 \cdot -5 + 15 \cdot 3 = 40 \checkmark$

$$3x^2 + 40x - 75 = (x + 15)(3x - 5)$$

[1] minor error OR no work shown

54.  $1 \cdot 7 = 7$ ;  $1 \cdot 7 = 8$ ;  $y^2 + 8y + 7 = (y + 1)(y + 7)$   
 55.  $-4 \cdot -3 = 12$ ;  $-4 + (-3) = -7$ ;  $t^2 - 7t + 12 = (t - 4)(t - 3)$   
 56.  $-5 \cdot 4 = -20$ ;  $-5 + 4 = -1$ ;  $t^2 - 7t + 12 = (t - 5)(t + 4)$   
 57.  $-12 \cdot -3 = 36$ ;  $-12 + (-3) = -15$ ;  $m^2 - 15m + 36 = (m - 12)(m - 3)$   
 58.  $-2 \cdot 18 = -36$ ;  $-2 + 18 = 16$ ;  $k^2 + 16k - 36 = (k - 2)(k + 18)$   
 59.  $9 \cdot 8 = 72$ ;  $9 + 8 = 17$ ;  $g^2 + 17g + 72 = (g + 9)(g + 8)$   
 60.  $-16 \cdot 3 = -48$ ;  $-16 + 3 = -13$ ;  $h^2 - 13h - 48 = (h - 16)(h + 3)$   
 61.  $-15 \cdot 2 = -30$ ;  $-15 + 2 = -13$ ;  $x^2 - 13x - 30 = (x - 15)(x + 2)$   
 62.  $-14 \cdot -4 = 56$ ;  $-14 + (-4) = -18$ ;  $d^2 - 18d + 56 = (d - 14)(d - 4)$   
 63.  $89^2 = (90 - 1)^2 = 8100 - 180 + 1 = 7921$   
 64.  $401^2 = (400 + 1)^2 = 160,000 + 800 + 1 = 160,801$   
 65.  $903^3 = (900 + 3)^2 = 810,000 + 5400 + 9 = 815,409$   
 66.  $197^2 = (200 - 3)^2 = 40,000 - 1200 + 9 = 38,809$   
 67.  $39 \cdot 41 = (40 - 1)(40 + 1) = 1600 - 1 = 1599$   
 68.  $38 \cdot 42 = (40 - 2)(40 + 2) = 1600 - 4 = 1596$   
 69.  $198 \cdot 202 = (200 - 2)(200 + 2) = 40,000 - 4 = 39,996$   
 70.  $73 \cdot 67 = (70 + 3)(70 - 3) = 4900 - 9 = 4891$   
 71.  $f(-3) = 4 \cdot 2^{-3} = 4 \cdot \frac{1}{2^3} = \frac{1}{2}; 4 \cdot 2^0 = 4; 4 \cdot 2^2 = 4 \cdot 4 = 16$   
 72.  $h(-3) = -3 \cdot 3^{-3} = -\frac{3}{3^3} = -\frac{1}{9}; -3 \cdot 3^0 = -3$   
 $-3 \cdot 3^2 = -27$   
 73.  $k(-3) = \frac{1}{3} \cdot 3^{-3} = \frac{1}{3^4} = \frac{1}{81}; \frac{1}{3} \cdot 3^0 = \frac{1}{3}; \frac{1}{3} \cdot 3^2 = 3$   
 74.  $g(-3) = 5 \cdot \left(\frac{1}{10}\right)^{-3} = 5 \cdot 10^3 = 5000$   
 $5 \cdot \left(\frac{1}{10}\right)^0 = 5; 5 \cdot \left(\frac{1}{10}\right)^2 = \frac{5}{100} = \frac{1}{20}$   
 75.  $g(-3) = \frac{1}{10} \cdot 5^{-3} = \frac{1}{10} \cdot \frac{1}{5^3} = \frac{1}{1250}; \frac{1}{10} \cdot 5^0 = \frac{1}{10}; \frac{1}{10} \cdot 5^2 = \frac{25}{10} = \frac{5}{2} = 2\frac{1}{2}$   
 76.  $h(-3) = 8 \cdot (0.2)^{-3} = 8 \cdot (5)^3 = 1000$   
 $8 \cdot (0.2)^0 = 8; 8 \cdot (0.2)^2 = 8 \cdot 0.04 = 0.32$



## 9-7 Factoring Special Cases

Pages 490–491

Check Skills You'll Need p. 490 For complete solutions see Daily Skills Check and Lesson Quiz Transparencies or Presentation Pro CD-ROM.

1.  $9x^2$  2.  $25y^2$  3.  $225h^4$  4.  $4a^2b^4$  5.  $c^2 - 36$

6.  $p^2 - 22p + 121$  7.  $16d^2 + 56d + 49$

**Investigation** 1.  $x^2 + 6x + 9 = (x + 3)(x + 3)$ ;  $x^2 + 10x + 9 = (x + 9)(x + 1)$ ;  $m^2 + 15m + 36 = (m + 3)(m + 12)$ ;  $m^2 + 12m + 36 = (m + 6)(m + 6)$ ;  $k^2 + 26k + 25 = (k + 1)(k + 25)$ ;  $k^2 + 10k + 25 = (k + 5)(k + 5)$  2a.  $x^2 + 6x + 9$ ;  $m^2 + 12m + 36$ ;  $k^2 + 10k + 25$  2b. The last term equals the square of one half the coefficient of the middle term.

**Check Understanding** 1a.  $x^2 + 8x + 16 = x^2 + (2 \cdot 4)x + 4 \cdot 4 = (x + 4)(x + 4) = (x + 4)^2$   
 1b.  $n^2 + 16n + 64 = n^2 + 2 \cdot 8n + 8 \cdot 8 = (n + 8)^2$   
 1c.  $n^2 - 16n + 64 = n^2 - 2(n \cdot 8) + 8 \cdot 8 = (n - 8)^2$   
 2a.  $9g^2 - 12g + 4 = (3g)^2 - 2 \cdot 3 \cdot 2g + 2 \cdot 2 = (3g - 2)^2$  2b.  $4t^2 + 36t + 81 = (2t)^2 + 2(2t)(9) + 9^2 = (2t + 9)^2$  2c.  $4t^2 - 36t + 81 = (2t)^2 - 2(2t)(9) + 9^2 = (2t - 9)^2$  3a.  $x^2 - 36 = x^2 - 6^2 = (x + 6)(x - 6) = x^2 - 6x - 36 = x^2 - 36 \checkmark$  3b.  $m^2 - 100 = m^2 - 10^2 = (m + 10)(m - 10) = m^2 - 10m + 10m - 100 = m^2 - 100 \checkmark$  3c.  $p^2 - 49 = p^2 - 7^2 = (p + 7)(p - 7) = p^2 - 7p + 7p - 49 = p^2 - 49 \checkmark$  4a.  $9v^2 - 4 = (3v)^2 - 2^2 = (3v + 2)(3v - 2)$   
 4b.  $25x^2 - 64 = (5x)^2 - 8^2 = (5x + 8)(5x - 8)$   
 4c.  $4w^2 - 49 = (2w)^2 - 7^2 = (2w + 7)(2w - 7)$   
 5a.  $8y^2 - 50 = 2(4y^2 - 25) = 2(2y + 5)(2y - 5)$   
 5b.  $3c^2 - 75 = 3(c^2 - 25) = 3(c + 5)(c - 5)$   
 5c.  $28k^2 - 7 = 7(4k^2 - 1) = 7(2k + 1)(k - 1)$   
**Exercises** 1.  $c^2 + 10c + 25 = c^2 + (2 \cdot 5)c + 5^2 = (c + 5)^2$  2.  $x^2 - 2x + 1 = x^2 - 2(x)1 + 1^2 = (x - 1)(x - 1)$  3.  $h^2 + 12h + 36 = h^2 + 2(h)6 + 6^2 = (h + 6)(h + 6)$  4.  $m^2 - 24m + 144 = m^2 - 2(m)12 + 12^2 = (m - 12)(m - 12)$   
 5.  $k^2 - 16k + 64 = k^2 - 2(k)8 + 8^2 = (k - 8)(k - 8)$   
 6.  $t^2 - 14t + 49 = t^2 - 2(t)7 + 7^2 = t^2 - 14t + 49$   
 7.  $4m^2 + 20m + 25 = (2m)^2 + 2(2 \cdot 5)m + 5^2 = (2m + 5)^2$  8.  $49d^2 + 28d + 4 = (7d)^2 + 2(7d)2 + 2^2 = (7d + 2)^2$  9.  $25g^2 - 40g + 16 = (5g)^2 - 2(5g) + 4^2 = (5g - 4)(5g - 4)$   
 10.  $25g^2 - 30g + 9 = (5g - 3)^2 = 25g^2 - 2(5g)(3) + 9 = 25g^2 - 30g + 9 \checkmark$  11.  $64r^2 - 144r + 81 = (8r - 9)^2 = 64r^2 - 2(8r)(9) + 81 = 64r^2 - 144r + 81 \checkmark$   
 12.  $100v^2 - 220v + 121 = (10v)^2 - 2(10v)(11) + 11^2 =$

$$\begin{aligned}
(10v - 11)^2 &= 100v^2 - 2(110v) + 121 = \\
100v^2 - 220v + 121 &\checkmark \quad 13. x^2 - 4 = (x + 2)(x - 2) = \\
x^2 - 2x + 2x - 4 &= x^2 - 4 \checkmark \quad 14. y^2 - 81 = \\
(y + 9)(y - 9) &= y^2 - 9y + 9y - 81 = y^2 - 81 \checkmark \\
15. k^2 - 196 &= (k + 14)(k - 14) = \\
k^2 - 14k + 14k - 196 &= k^2 - 196 \checkmark \quad 16. r^2 - 144 = \\
(r + 12)(r - 12) &= r^2 - 12r + 12r - 144 = r^2 - 144 \checkmark \\
17. h^2 - 100 &= (h + 10)(h - 10) = \\
h^2 - 10h + 10h - 100 &= h^2 - 100 \checkmark \quad 18. m^2 - 225 = \\
(m + 15)(m - 15) &= m^2 - 15m + 15m - 225 = \\
m^2 - 225 \quad 19. w^2 - 256 &= (w + 16)(w - 16) = \\
w^2 - 16w + 16w - 256 &= w^2 - 256 \checkmark \quad 20. x^2 - 400 = \\
(x + 20)(x - 20) &= x^2 - 20x + 20x - 400 = \\
x^2 - 400 \checkmark \quad 21. y^2 - 900 &= (y + 30)(y - 30) = \\
y^2 - 30y + 30y - 900 &= y^2 - 900 \quad 22. 25q^2 - 9 = \\
(5q)^2 - 3^2 &= (5q + 3)(5q - 3) = \\
25q^2 - 15q + 15q - 9 &= 25q^2 - 9 \quad 23. 49y^2 - 4 = \\
(7y)^2 - 2^2 &= (7y + 2)(7y - 2) = 49y^2 - 14y + 14y - 4 = \\
49y^2 - 4 \checkmark \quad 24. 9c^2 - 64 &= (3c)^2 - 8^2 = \\
(3c + 8)(3c - 8) &= 9c^2 - 24c + 24c - 64 = 9c^2 - 64 \checkmark \\
25. 4m^2 - 81 &= (2m)^2 - 9^2 = (2m + 9)(2m - 9) = \\
4m^2 - 18m + 18m - 81 &= 4m^2 - 81 \checkmark \quad 26. 16k^2 - 49 = \\
(4k)^2 - 7^2 &= (4k + 7)(4k - 7) = \\
16k^2 - 28k + 28k - 49 &= 16k^2 - 49 \checkmark \quad 27. 144p^2 - 1 = \\
(12p)^2 - 1^2 &= (12p + 1)(12p - 1) = \\
144p^2 - 12p + 12p - 1 &= 144p^2 - 1 \checkmark \quad 28. 81v^2 - 100 = \\
(9v + 10)(9v - 10) &= 81v^2 - 90v + 90v - 100 = \\
81v^2 - 100 \quad 29. 400n^2 - 121 &= (20n + 11)(20n - 11) = \\
400n^2 - 220n + 220n - 121 &= 400n^2 - 121 \checkmark \\
30. 25w^2 - 196 &= (5w + 14)(5w - 14) = \\
25w^2 - 70w + 70w - 196 &= 25w - 196 \checkmark \\
31. 3m^2 - 12 &= 3(m^2 - 4) = 3(m + 2)(m - 2) = \\
3(m^2 - 2m + 2m - 4) &= 3m^2 - 12 \checkmark \quad 32. 5k^2 - 245 = \\
5(k^2 - 49) &= 5(k + 7)(k - 7) = 5(k^2 - 7k + 7k - 49) = \\
5k^2 - 245 \checkmark \quad 33. 3x^2 + 48x + 192 &= 3(x^2 + 16x + 64) = \\
3(x + 8)^2 &= 3(x^2 + 2(8x) + 8^2) = 3(x^2 + 16x + 64) = \\
3x^2 + 48x + 192 \checkmark \quad 34. 2t^2 - 36t + 162 = \\
2(t^2 - 18t + 81) &= 2(t - 9)^2 = 2(t^2 - 2(9t) + 81) = \\
2t^2 - 36t + 192 \checkmark \quad 35. 6r^3 - 150r &= 6r(r^2 - 25) = \\
6r(r + 5)(r - 5) &= 6r(r^2 - 5r + 5r - 25) = 6r^3 - 150r \checkmark \\
36. 7h^2 - 56h + 112 &= 7(h^2 - 8h + 16) = 7(h - 4)^2 = \\
7(h^2 - 2(4h) + 16) &= 7h^2 - 56h + 112 \checkmark \quad 37. \text{Answers} \\
\text{may vary. Sample: Rewrite the first and last terms as} \\
\text{squares } (ax)^2 \text{ and } (bx)^2. \text{ Check if the middle term can} \\
\text{be written as } 2ab. \text{ Factor as a square binomial.} \\
4x^2 + 12x + 9 &= (2x)^2 + 2(2 \cdot 3x) + 3^2 = (2x + 3)^2. \\
9x^2 - 30x + 25 &= (3x)^2 - 2(3 \cdot 5)x + 5^2 = (3x - 5)^2. \\
38. \text{two errors: sign and multiplication; } 4x^2 - 121 = \\
(2x + 11)(2x - 11); (4x - 11)(4x - 11) &= 16x^2 - 88 + 121 \\
39. 99 &= 100 - 1 = 10^2 - 1^2 = (10 + 1)(10 - 1) = \\
11 \cdot 9 \quad 40. 91 &= 100 - 9 = 10^2 - 3^2 = (10 + 3)(10 - 3) = \\
13 \cdot 7 \quad 41. 75 &= 100 - 25 = 10^2 - 5^2 = (10 + 5)(10 - 5) = \\
15 \cdot 5 \quad 42. 117 &= 121 - 4 = 11^2 - 2^2 = \\
(11 + 2)(11 - 2) &= 13 \cdot 9 \quad 43. 224 = 225 - 1 = \\
15^2 - 1^2 &= (15 + 1)(15 - 1) = 16 \cdot 14 \quad 44a. \text{Answers} \\
\text{may vary. Sample: } 4x^2 + 24x + 36 \quad 44b. \text{because } 4x^2 = \\
(2x)^2 \text{ and } 36 = 6^2; 2 \cdot 2 \cdot 6 = 24 \quad 45. 100v^2 - 25w^2 = \\
25(4v^2 - w^2) &= 25[(2v)^2 - w^2] = 25(2v - w)(2v + w) \\
46. 16p^2 - 48pq + 36q^2 &= 4(4p^2 - 12pq + 9q^2) =
\end{aligned}$$

$$\begin{aligned}
4[(2p)^2 - (3q)^2] &= 4(2p - 3q)(2p + 3q) \\
47. 28c^2 + 140cd + 175d^2 &= 7(4c^2 + 20cd + 25d^2) = \\
7[(2c)^2 + (5d)^2] &= 7(2c + 5d)^2 \\
48. \frac{1}{4}m^2 - \frac{1}{9} &= \left(\frac{1}{2}m\right)^2 - \left(\frac{1}{3}\right)^2 = \left(\frac{1}{2}m - \frac{1}{3}\right)\left(\frac{1}{2}m + \frac{1}{3}\right) \\
49. x^2 + x + \frac{1}{4} &= x^2 + 2(x)\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)^2 = \left(x + \frac{1}{2}\right)^2 \\
50. 64g^2 - 192gh + 144h^2 &= 16(4g^2 - 12gh + 9h^2) = \\
8[(2g)^2 - (3h)^2] &= 8(2g + 3h)(2g - 3h) \\
51. \frac{1}{4}p^2 - 2p + 4 &= \left(\frac{1}{2}p\right)^2 - 2\left(\frac{1}{2}p\right)2 + 2^2 = \left(\frac{1}{2}p - 2\right)^2 \\
52. \frac{1}{9}n^2 - \frac{1}{25} &= \left(\frac{1}{3}n\right)^2 - \left(\frac{1}{5}\right)^2 = \left(\frac{1}{3}n - \frac{1}{5}\right)\left(\frac{1}{3}n + \frac{1}{5}\right) \\
53. \frac{1}{25}k^2 + \frac{6}{5}k + 9 &= \left(\frac{1}{5}k\right)^2 + 2\left(\frac{1}{5}k\right)3 + 3^2 = \left(\frac{1}{5}k + 3\right)^2 \\
54a. (3.14n)n - 3.14m^2 &= 3.14(n + m)(n - m) \\
54b. 3.14(10 + 3)(10 - 3) &= 3.14 \cdot 13 \cdot 7 = 285.74; \\
285.74 \text{ in.}^2 \quad 55a. 4x^2 - 100 &= 4(x^2 - 25) = \\
4(x + 5)(x - 5) \quad 55b. 4x^2 - 100 &= (2x + 10)(2x - 10) = \\
4(x + 5)(x - 5) \quad 55c. \text{There is only one result for the} \\
\text{factoring of } 4x^2 - 100, \text{ but there are two different paths} \\
\text{to that result, because } 100 = 10^2 \text{ and } \frac{100}{4} = 25 = 5^2. \\
55d. \text{No, because } 3x^2 - 75 \text{ is not a difference of squares.} \\
56. 64r^6 - 144r^3 + 81 &= (8r^3)^2 - 2 \cdot 8 \cdot 9r^3 + 9^2 = \\
(8r^3 - 9)^2 \quad 57. p^6 + 40p^3q + 400q^2 &= \\
(p^3)^2 + 2(p^3q)20 + (20q)^2 &= (p^3 + 20q)^2 \\
58. 36m^4 + 84m^2 + 49 &= (6m^2)^2 + 2(6m^2)7 + 7^2 = \\
(6m^2 + 7)^2 \quad 59. 81p^{10} + 198p^5 + 121 &= \\
(9p^5)^2 + 2(9p^5)11 + 11^2 &= (9p^5 + 11)^2 \\
60. 108m^6 - 147 &= 3(36m^6 - 49) = 3[(6m^3)^2 - 72] = \\
3(6m^3 - 7)(6m^3 + 7) \quad 61. x^{20} - 4x^{10}y^5 + 4y^{10} &= \\
(x^{10})^2 - 2(x^{10})(2y^5) + (2y^5)^2 &= (x^{10} - 2y^5)^2 \\
62. 256g^4 - 100h^6 &= 4(64g^4 - 25h^6) = \\
4[(8g^2)^2 - (5h^3)^2] &= 4(8g^2 - 5h^3)(8g^2 + 5h^3) \\
63. 45x^4 - 60x^2y + 20y^2 &= 5(9x^4 - 12x^2y + 4y^2) = \\
5[(3x^2)^2 - 2(3x^2)(2y) + (2y)^2] &= 5(3x^2 - 2y)^2 \\
64. 37g^8 - 37h^8 &= 37(g^8 - h^8) = 37(g^4 + h^4)(g^4 - h^4) = \\
37(g^4 + h^4)(g^2 + h^2)(g^2 - h^2) &= \\
37(g^4 + h^4)(g^2 + h^2)(g + h)(g - h) \quad 65a. (t - 3)^2 - 16 = \\
a^2 - b^2; a = t - 3; b = 4 \quad 65b. (t - 3)^2 - 16 = \\
[(t - 3) + 4][(t - 3) - 4] &= (t + 1)(t - 7) \\
66a. 16 - 81n^4 &= (4 + 9n^2)(4 - 9n^2) = \\
(4 + 9n^2)(2 + 3n)(2 - 3n) \quad 66b. \text{They are squares of} \\
\text{square terms.} \quad 66c. \text{Answers may vary. Sample: } 16x^4 - 1 \\
67. 4x^2 + 28x + 49 &= (2x + 7)^2; \text{the answer is 9.} \\
68. x^2 - 24x + 144 &= (x - 12)^2; \text{the answer is -12.} \\
69. 225 &= 15^2; k = 2 \cdot 15 = 30; \text{the answer is 30.} \\
70. \text{The green area + the purple area} &= \\
4x^2 + 16x + 16 + 5x^2 + 14x + 9 &= 9x^2 + 30x + 25 = \\
(3x + 5)^2; \text{the answer is 5.} \quad 71. 144x^4 - 121 &= \\
(12x^2)^2 - (11)^2 &= (12x^2 - 11)(12x^2 + 11); \text{the answer is 12.} \\
72. 81x^2 - 36 &= 9(9x^2 - 4) = 9(3x + 2)(3x - 2); \\
\frac{3+2}{2} &= 2.5; \text{the answer is 2.5.} \\
73. 2d^2 &+ 11d \\
2 \cdot 1 &2 \cdot 1 + 1 \cdot 5 = 7 \\
2 \cdot 1 &2 \cdot 5 + 1 \cdot 1 = 11 \checkmark \\
(2d + 1)(d + 5) &= 2d^2 + 11d + 5
\end{aligned}$$

74.	$2x^2$	- 11x	+ 12
	$1 \cdot 2$	$1 \cdot -12 + -1 \cdot 2 = -14$	$-1 \cdot -12$
	$1 \cdot 2$	$1 \cdot -4 + -3 \cdot 2 = -10$	$-3 \cdot -4$
	$1 \cdot 2$	$1 \cdot -3 + -4 \cdot 2 = -11 \checkmark$	$-4 \cdot -3$
	$(x - 4)(2x - 3) = 2x^2 - 11x + 12$		
75.	$4t^2$	+ 16t	+ 7
	$4 \cdot 1$	$4 \cdot 1 + 1 \cdot 7 = 11$	$7 \cdot 1$
	$4 \cdot 1$	$2 \cdot 7 + 1 \cdot 1 = 15$	$1 \cdot 7$
	$2 \cdot 2$	$2 \cdot 1 + 2 \cdot 7 = 16 \checkmark$	$7 \cdot 1$
	$(2t + 7)(2t + 1) = 4t^2 + 16t + 7$		
76.	$5w^2$	- 44w	- 9
	$5 \cdot 1$	$5 \cdot 1 + 1 \cdot -9 = -4$	$-9 \cdot 1$
	$5 \cdot 1$	$5 \cdot -9 + 1 \cdot 1 = -44 \checkmark$	$1 \cdot -9$
	$(5w + 1)(w - 9) = 5w^2 - 44w - 9$		
77.	$6t^2$	+ 19t	+ 8
	$1 \cdot 6$	$1 \cdot 8 + 1 \cdot 6 = 14$	$1 \cdot 8$
	$1 \cdot 6$	$1 \cdot 4 + 2 \cdot 6 = 16$	$2 \cdot 4$
	$2 \cdot 3$	$2 \cdot 8 + 1 \cdot 3 = 19 \checkmark$	$1 \cdot 8$
	$(2t + 1)(3t + 8) = 6t^2 + 19t + 8$		
78.	$21m^2$	- 20m	- 9
	$3 \cdot 7$	$3 \cdot 1 + 7 \cdot -9 = -60$	$-9 \cdot 1$
	$3 \cdot 7$	$3 \cdot -9 + 7 \cdot 1 = -20 \checkmark$	$1 \cdot -9$
	$(3m + 1)(7m - 9) = 3m^2 - 20m - 9$		
79.	$14x^2$	- 11x	- 9
	$2 \cdot 7$	$2 \cdot 1 + 7 \cdot -9 = -61$	$-9 \cdot 1$
	$2 \cdot 7$	$2 \cdot -9 + 7 \cdot 1 = -11 \checkmark$	$1 \cdot -9$
	$(2x + 1)(7x - 9) = 14x^2 - 11x - 9$		
80.	$4y^2$	+ 32y	+ 55
	$2 \cdot 2$	$2 \cdot 11 + 5 \cdot 2 = 32 \checkmark$	$5 \cdot 11$
	$(2y + 5)(2y + 11) = 4y^2 + 32y + 55$		
81.	$12k^2$	- 5k	- 2
	$3 \cdot 4$	$3 \cdot -2 + 4 \cdot 1 = -2$	$1 \cdot -2$
	$3 \cdot 4$	$3 \cdot 1 + 4 \cdot -2 = -5 \checkmark$	$-2 \cdot 1$
	$(3k - 2)(4k + 1) = 12k^2 - 5k - 2$		
82.	768, 3072, 12,288; $3 \cdot 4^{n-1}$	83. 29, 37, 45; -11 + 8n	
84.	-11, -20, -29; 34 - 9n	85. 0.02, 0.002, 0.0002;	
	$2000 \cdot (0.1)^n$	86. -32, 64, -128; $(-2)^n$	
87.	129.6, 777.6, 4665.6; $0.1(6)^{n-1}$	88. $\frac{32}{125}, \frac{64}{625}, \frac{128}{3125}$ ; $10 \cdot \left(\frac{2}{5}\right)^{n-1}$	
	89. $6\frac{1}{2}, 8, 9\frac{1}{2}; -1 + \frac{3}{2}n$	90. 8, 32, 128; $\frac{1}{32} \cdot 4^{n-1}$	
91a.	Let $x$ = hours studying, $y$ = grade. Calculator gives $y = 11.4x + 64.8$		
91b.	$11.4(2.5) + 64.8 = 93.3; 93$		
91c.	$11.4(1.25) + 64.8 = 79.05; 79$		

### CHECKPOINT QUIZ 2 page 495

- $(k - 7)^2 = k^2 - 2(k)7 + 7^2 = k^2 - 14k + 49$
- $(5t + 9)^2 = (5t)2 + 2(5t)9 + 9^2 = 25t^2 + 90t + 81$
- $(h - 11)(h - 11) = h^2 - 2(h)11 + 11^2 = h^2 - 22h + 121$
- $v^2 + 2(v)10 + 102 = (v + 10)^2$
- $5. -10 \cdot 4 = -40; -10 + 4 = -6; p^2 - 6p - 40 = (p - 10)(p + 4)$
- $-12 \cdot -5 = 60; -12 + (-5) = -17; k^2 - 17k + 60 = (k - 12)(k - 5)$

7.	$2x^2$	+ 13x	+ 11
	$2 \cdot 1$	$2 \cdot 11 + 1 \cdot 1 = 23$	$1 \cdot 11$
	$2 \cdot 1$	$2 \cdot 1 + 1 \cdot 11 = 13 \checkmark$	$11 \cdot 1$
	$(2x + 11)(x + 1) = 2x^2 + 13x + 11$		
8.	$10m^2$	+ 19m	+ 7
	$2 \cdot 5$	$2 \cdot 1 + 7 \cdot 5 = 37$	$7 \cdot 1$
	$2 \cdot 5$	$2 \cdot 7 + 5 \cdot 1 = 19 \checkmark$	$1 \cdot 7$
	$(2m + 1)(5m + 7) = 2m^2 + 19m + 7$		
9.	$3w^2 - 6w - 24$	$= 3(w^2 - 2w - 8) = 3(w - 4)(w + 2)$	
10.	$9t^2 - 25$	$= (3t)^2 - 5^2 = (3t - 5)(3t + 5)$	

### 9-8 Factoring by Grouping

pages 496–507

**Check Skills You'll Need p. 496** For complete solutions see Daily Skills Check and Lesson Quiz Transparencies or Presentation Pro CD-ROM.

1. 2. 2. 3r 3. 5h 4. 4m 5.  $v^3 + 3v^2 + 5v + 15$
  6.  $2q^3 - 10q^2 - 4q + 20$
  7.  $6t^2 - 7t - 20$
  8.  $4x^3 + 7x^2 + 10x - 3$
- Check Understanding**
- $5t^4 + 20t^3 + 6t + 24 = 5t^3(t + 4) + 6(t + 4) = (5t^3 + 6)(t + 4) = 5t^4 + 20t^3 + 6t + 24 \checkmark$
  - $2w^3 + w^2 - 14w - 7 = w^2(2w + 1) - 7(2w + 1) = (w^2 - 7)(2w + 1) = 2w^3 + w^2 - 14w - 7 \checkmark$
  - $45m^4 - 9m^3 + 30m^2 - 6m = 3m(15m^3 - 3m^2 + 10m - 2) = 3m[3m^2(5m - 1) + 2(5m - 1)] = 3m(3m^2 + 2)(5m - 1)$
  - $ac = 63 \cdot 5 = 315 = 3 \cdot 105 = 5 \cdot 63 = 7 \cdot 45 = 9 \cdot 35; 9 + 35 = 44; 63d^2 + (9 + 35)d + 5 = 63d^2 + 9d + 35d + 5 = 9d(7d + 1) + 5(7d + 1) = (9d + 5)(7d + 1)$
  - $3b. ac = 11 \cdot 20 = 220 = 4 \cdot 55 = 5 \cdot 44; 5 + 44 = 49; 11k^2 + 49k + 20 = 11k^2 + (5 + 44)k + 20 = 11k^2 + 5k + 44k + 20 = k(11k + 5) + 4(11k + 5) = (k + 4)(11k + 5)$
  - $3c. ac = 4 \cdot -70 = -280 = 8 \cdot -35 = 40 \cdot -7; 40 + (-7) = 33; 4y^2 + 33y - 70 = 4y^2 + (40 - 7)y - 70 = 4y^2 + 40y - 7y - 70 = 4y(y + 10) - 7(y + 10) = (4y - 7)(y + 10)$
  - $4a. 6g^3 + 20g^2 + 16g = 2g(3g^2 + 10g + 8) = 2g(3g + 4)(g + 2); \text{dimensions are } 2g, 3g + 4, \text{ and } g + 2.$
  - $4b. 3m^3 + 10m^2 + 3m = m(3m^2 + 10m + 3) = m(3m + 1)(m + 3); \text{dimensions are } m, 3m + 1, \text{ and } m + 3.$

- Exercises**
1.  $2m^2, 3$
  2.  $5p^2, 2$
  3.  $2z^2, -5$
  4.  $3n^2, 1$
  5.  $6n^3 + 8n^2 + 3n + 4 = 2n^2(3n + 4) + (3n + 4) = (2n^2 + 1)(3n + 4)$
  6.  $14t^3 + 21t^2 + 16t + 24 = 7t^2(2t + 3) + 8(2t + 3) = (7t^2 + 8)(2t + 3)$
  7.  $27t^3 + 45t^2 - 3t - 5 = 9t^2(3t + 5) - (3t + 5) = (9t^2 - 1)(3t + 5) = (3t + 1)(3t - 1)(3t + 5)$
  8.  $13y^3 - 8y^2 + 13y - 8 = y^2(13y - 8) + (13y - 8) = (y^2 + 1)(13y - 8)$
  9.  $45x^3 + 20x^2 + 9x + 4 = 5x^2(9x + 4) + (9x + 4) = (5x^2 + 1)(9x + 4)$
  10.  $10w^3 + 16w^2 - 15w - 24 = 2w^2(5w + 8) - 3(5w + 8) = (2w^2 - 3)(5w + 8)$
  11.  $12v^3 - 32v^2 + 6v - 16 = 2(6v^3 - 16v^2 + 3v - 8) = 2[2v^2(3v - 8) + (3v - 8)] = 2(2v^2 + 1)(3v - 8)$
  12.  $7q^4 - 4q^3 + 28q^2 - 16q = q(7q^3 - 4q^2 + 28q - 16) = q[q^2(7q - 4) + 4(7q - 4)] = q(q^2 + 4)(7q - 4)$

**13.**  $20m^3 - 18m^2 + 40m - 36 =$

$$2(10m^3 - 9m^2 + 20m - 18) =$$

$$2[m^2(10m - 9) + 2(10m - 9)] = 2(m^2 + 2)(10m - 9)$$

**14.**  $6x^4 + 4x^3 - 6x^2 - 4x = 2x(3x^3 + 2x^2 - 3x - 2) =$

$$2x[x^2(3x + 2) - (3x + 2)] = 2x(x^2 - 1)(3x + 2) =$$

$$2x(x + 1)(x - 1)(3x + 2)$$

**15.**  $12y^3 - 20y^2 + 30y - 50 =$

$$2(6y^3 - 10y^2 + 15y - 25) =$$

$$2[2y^2(3y - 5) + 5(3y - 5)] = 2(2y^2 + 5)(3y - 5)$$

**16.**  $9c^3 - 12c^2 + 18c - 24 = 3(3c^3 - 4c^2 + 6c - 8) =$

$$3[c^2(3c - 4) + 2(3c - 4)] = 3(c^2 + 2)(3c - 4)$$

**17.**  $12p^2 + 16p + 5 = (6p + 5)(2p + 1)$

**18.**  $16 \cdot 9 = 144 = 12 \cdot 12; 12 + 12 = 24; 16t^2 + 12t + 12t + 9 =$

$$4t(4t + 3) + 3(4t + 3) = (4t + 3)^2$$

**19.**  $18 \cdot -10 = 60 \cdot -3; 60 + (-3) = 57; 18n^2 + 60n - 3n - 10 =$

$$6n(3n + 10) - (3n + 10) = (6n - 1)(3n + 10)$$

**20.**  $-9 \cdot -20 = -3 \cdot -60 = -12 \cdot -15; -12 + (-15) =$

$$-27; 9w^2 - 12w - 15w + 20 = 3w(3w - 4) - 5(3w - 4) =$$

$$(3w - 5)(3w - 4)$$

**21.**  $24m^2 + 8m - 2 =$

$$2(12m + 4m - 1) = 2(6m - 1)(2m + 1)$$

**22.**  $36 \cdot -7 = 12 \cdot -21; 12 - 21 = -9; 36v^2 + 12v - 21v - 7 =$

$$12v(3v + 1) - 7(3v + 1) = (12v - 7)(3v + 1)$$

**23.**  $6 \cdot -10 = -60 = -4 \cdot 15; -4 + 15 = 11;$

$$6x^2 + 11x - 10 = 6x^2 - 4x + 15x - 10 =$$

$$2x(3x - 2) + 5(3x - 2) = (2x + 5)(3x - 2)$$

**24.**  $-20 \cdot -9 = -5 \cdot -36; -5 + (-36) =$

$$-41; 20v^2 - 5v - 36v + 9 = 5v(4v - 1) - 9(4v - 1) =$$

$$(5v - 9)(4v - 1)$$

**25.**  $63 \cdot -20 = 7 \cdot -180 =$

$$12 \cdot -105 = 15 \cdot -84 = 18 \cdot -70; 18 - 70 = -52;$$

$$63q^2 + 18q - 70q - 20 = 9q(7q + 2) - 10(7q + 2) =$$

$$(9q - 10)(7q + 2)$$

**26.**  $3m^3 + 7m^2 + 2m =$

$$m(3m^2 + 7m + 2) = m(3m + 1)(m + 2); \text{ dimensions}$$

$$\text{are } m, 3m + 1, \text{ and } m + 2.$$

**27.**  $5k^3 + 30k^2 + 40k =$

$$5k(k^2 + 6k + 8) = 5k(k + 2)(k + 4) \text{ dimensions are } 5k,$$

$$k + 2, \text{ and } k + 4.$$

**28.**  $7h^3 - 35h^2 - 42h =$

$$7h(h^2 - 5h - 6) = 7h(h + 1)(h - 6)$$

**29.**  $60t^3 - 200t^2 - 66t + 220 =$

$$2(30t^3 - 100t^2 - 33t + 110) =$$

**30.**  $8d^3 + 16d^2 + 24d + 48 = 8(d^3 + 2d^2 + 3d + 6) =$

$$8[d^2(d + 2) + 3(d + 2)] = 8(d^2 + 3)(d + 2)$$

**31.**  $12x^2 - 4xy - 56y^2 = 4(3x^2 - xy - 14y^2) =$

$$4(3x - 7y)(x + 2y)$$

**32.**  $54r^3 - 45r^2 + 9r =$

$$9r(6r^2 - 5r + 1) = 9r(3r - 1)(2r - 1)$$

**33.**  $150k^3 + 350k^2 + 180k + 420 =$

$$10(15k^3 + 35k^2 + 18k + 42) =$$

$$10[5k^2(3k + 7) + 6(3k + 7)] = 10(5k^2 + 6)(3k + 7)$$

**34a.**  $(28x^3 - 7x^2) + (36x - 9) =$

$$7x^2(4x - 1) + 9(4x - 1) = (7x^2 + 9)(4x - 1)$$

**34b.**  $(28x^3 + 36x) + (-7x^2 - 9) =$

$$4x(7x^2 + 9) - (7x^2 + 9) = (4x - 1)(7x^2 + 9)$$

**34c.** Answers may vary. Sample: The sequence of the final factors may vary, but the final results are equivalent.

**35.**  $14w^3 + 49w^2 - 8w - 28 =$

$$7w^2(2w^2 + 7) - 4(2w + 7) = (7w^2 - 4)(2w^2 + 7)$$

**36.**  $2m^3 - 32m^2 - m + 16 = 2m^2(m - 16) - (m - 16) =$

$$(2m^2 - 1)(m - 16)$$

**37.**  $44t^3 - 4t^2 + 66t - 6 =$

$$2(22t^3 - 2t^2 + 33t - 3) = 2[2t^2(11t - 1) + 3(11t - 1)] =$$

$$2(2t^2 + 3)(11t - 1)$$

**38.**  $25x^3 - x^2 - 50x + 2 =$

$$x^2(25x - 1) - 2(25x - 1) = (x^2 - 2)(25x - 1)$$

**39.**  $84w^3 + 82w^2 + 10w = 2w(42w^2 + 41w + 5) =$

$2w(6w + 5)(7w + 1); \text{ the dimensions are } 2w, 6w + 5, \text{ and } 7w + 1.$

**40.** The easiest way to do this is to start with the factors. Sample:  $(2x^2 + 1)(x + 3) = 2x^3 + 6x^2 + x + 3 =$

$$2x^2(x + 3) + (x + 3) = (2x^2 + 1)(x + 3)$$

**41.**  $10x^3 - 15x^2 + 2x - 3; \text{ factor the first two terms.}$

$$= 5x^2(2x - 3) + (2x - 3); \text{ notice the repeated factor.}$$

$$= (5x^2 + 1)(2x - 3); \text{ factor out } (2x - 3).$$

**42.**  $30m^5 + 24m^3n - 35m^2n^2 - 28n^3 =$

$$6m^3(5m^2 + 4n) - 7n^2(5m^2 + 4n) =$$

$$(6m^3 - 7n^2)(5m^2 + 4n)$$

**43.**  $x^2p + x^2q^5 + yp + yq^5 =$

$$x^2(p + q^5) + y(p + q^5) = (x^2 + y)(p + q^5)$$

**44.**  $h^3 + 11h^2 - 4h - 44 = h^2(h + 11) - 4(h + 11) =$

$$(h^2 - 4)(h + 11) = (h + 2)(h - 2)(h + 11)$$

**45.**  $w^6 - w^4 - 9w^2 + 9 = w^4(w^2 - 1) - 9(w^2 - 1) =$

$$(w^4 - 9)(w^2 - 1) = (w^2 + 3)(w^2 - 3)(w + 1)(w - 1)$$

**46a.**  $2\pi x^3 + 12\pi x^2 + 18\pi x = 2\pi x(x^2 + 6x + 9) =$

$$2\pi x(x + 3)^2$$

**46b.**  $V = \pi r^2 h; h = 2x; r = (x + 3)$

**47.**  $(2^5 + 2^4 + 2^3) + (2^2 + 2^1 + 2^0) = 2^3(2^2 + 2^1 + 2^0) +$

$$(2^2 + 2^1 + 2^0) = (2^3 + 2^0)(2^2 + 2^1 + 2^0) = (9)(7)$$

**48.**  $(2^5 + 2^4) + (2^3 + 2^2) + (2^1 + 2^0) =$

$$2^4(2^1 + 2^0) + 2^2(2^1 + 2^0) + (2^1 + 2^0) =$$

$$(2^4 + 2^2 + 2^0)(2^1 + 2^0) = (21)(3)$$

**49a.** Answers may vary. Sample: width =  $x$ ; height =  $x + 4$ ; length =  $2x + 4$

**49b.** volume =  $x(x + 4)(2x + 4) = x(2x^2 + 12x + 16) =$

$$2x^3 + 12x^2 + 16x$$

**50.**  $27x^4 + 15x^3 + 63x + 35 =$

$$3x^3(9x + 5) + 7(9x + 5) = (3x^3 + 7)(9x + 5); \text{ the answer is C.}$$

**51.**  $6g^3 - 5g^2 + 24g - 20 =$

$$q^2(6g - 5) + 4(6g - 5) = (q^2 + 4)(6g - 5);$$

$$(q^2 + 4) + (6g - 5) = q^2 + 6g - 1; \text{ the answer is H.}$$

**52.** [2]  $9a^4 - 54a^3 - 2a + 12 = 9a^3(a - 6) - 2(a - 6) =$

$$(9a^3 - 2)(a - 6)$$

[1] one computational error

**53.** [4]  $96x^3 + 48x^2 + 6x = 6x(16x^2 + 8x + 1) =$

$$6x(4x + 1)^2; \text{ side of square measures } (4x + 1); \text{ perimeter} = 4(4x + 1) = 16x + 4$$

[3] one error in factoring

[2] found factors of polynomial, but did not find perimeter

[1] no work shown

**54.**  $k^2 + 14k + 49 = k^2 + 2(k)7 + 7^2 = (k + 7)^2$

**55.**  $r^2 + 6r + 9 = r^2 + 2(r)3 + 3^2 = (r + 3)^2$

**56.**  $y^2 - 16y + 64 = y^2 - 2(y)8 + 8^2 = (y - 8)^2$

**57.**  $2t^2 + 12t + 18 = 2(t^2 + 6t + 9) =$

**58.**  $m^2 - 64 = 2[t^2 + 2(t)3 + 3^2] = 2(t + 3)^2$

$$m^2 - 8^2 = (m - 8)(m + 8)$$

**59.**  $4g^2 + 40g + 100 = 4(g^2 + 10g + 25) = 4[g^2 + 2(g)5 + 5^2] = 4(g + 5)^2$

**60.**  $4d^2 - 25 = (2d)^2 - 5^2 = (2d - 5)(2d + 5)$

**61.**  $5n^2 - 45 = 5(n^2 - 9) = 5(n^2 - 3^2) =$

$$5(n - 3)(n + 3)$$

**62.**  $25q^2 + 40q + 16 = (5q)^2 + 2(5q)4 + 4^2 = (5q + 4)^2$

**63.**  $(b^2)^2 = b^{2 \cdot 2} = b^4$

**64.**  $x^4 \cdot x^{-2} = x^{4+(-2)} = x^2$

**65.**  $(t^3)^5 = t^{3 \cdot 5} = t^{15}$

**66.**  $(c^5d)^7 = (c^5)^7d^7 = c^{5 \cdot 7}d^7 = c^{35}d^7$

**67.**  $(2y)^3 = 2^3y^3 = 8y^3$

**68.**  $(9m)^0 = 1$

**69.**  $(x^3)(x^7)^{-2} = x^3x^{7-2} =$

$$x^3x^{-14} = x^{-11} = \frac{1}{x^{11}}$$

**70.**  $(3w^2v^3)^4 = 3^4w^8v^{12}$

$$81w^8v^{12}$$

**71.**  $(2 \times 10^5)^4 = 2^4 \cdot (10^5)^4 = 16 \cdot 10^{5 \cdot 4} =$

$$16 \cdot 10^{20} = 1.6 \times 10^{21}$$

**72.**  $(3 \times 10^6)^2 = 3^2 \cdot 10^{6 \cdot 2} =$

$$9 \times 10^{12}$$

**73.**  $(7 \times 10^{-6})^2 = 49 \cdot 10^{-12} = 4.9 \times 10^{-11}$

**74.**  $(2 \times 10^7)^5 = 32 \cdot 10^{35} = 3.2 \times 10^{36}$

**75.**  $(5.3 \times 10^2)^2 = 5.3^2 \cdot 10^4 = 28.09 \cdot 10^4 =$

$$2.809 \times 10^5 \quad 76. (8.1 \times 10^{-3})^2 = 8.1^2 \cdot 10^{-6} = \\ 65.61 \cdot 10^{-6} = 6.561 \times 10^{-5} \quad 77. (1.9 \times 10^8)^3 = \\ 1.9^3 \cdot 10^{24} = 6.859 \times 10^{24} \quad 78. (4 \times 10^{-3})^{-2} = \\ 4^{-2} \cdot 10^6 = 0.0625 \cdot 10^6 = 6.25 \times 10^4$$

79.  $-7x + 12 = 3x + 2$   
 $-10x + 12 = 2$   
 $-10x = -10$   
 $x = 1$   
 $y = 3 \cdot 1 + 2 = 5$

80.  $-3x + 4 = -5x + 12$   
 $2x + 4 = 12$   
 $2x = 8$   
 $x = 4$   
 $y = -3 \cdot 4 + 4 = -8$

81.  $y = -4x + 7$   
 $10x + 2y = 15$   
 $10x + 2(-4x + 7) = 15$   
 $10x - 8x + 14 = 15$   
 $2x + 14 = 15$   
 $2x = 1$   
 $x = 0.5$   
 $y = -4 \cdot 0.5 + 7 = 5$

82.  $y = -2x - 26$   
 $x + y = -28$   
 $x + (-2x - 26) = -28$   
 $-x - 26 = -28$   
 $-x = -2$   
 $x = 2$   
 $y = -2 \cdot 2 - 26 = -30$

83.  $8x + 2y = 50$   
 $2y = -8x + 50$   
 $y = -4x + 25$

The two equations are identical. There are infinitely many solutions  $(x, y)$  which satisfy  $y = -4x + 25$ .

84.  $y = x - 5$   
 $11x - 6y = 65$   
 $11x - 6(x - 5) = 65$   
 $5x + 30 = 65$   
 $5x = 35$   
 $x = 7$   
 $y = 7 - 5 = 2$

### TEST-TAKING STRATEGIES

page 502

1. B.  $(x - 1)(x^2 + 2x + 3) = x^3 + x^2 + x - 3$   
D.  $(x - 1)(x^2 - 2x + 3) = x^3 - 3x^2 + 5x - 3$ ; the answer is B.  $2. 5(-2) = -10$ , whereas B has  $-2$  for the constant term.  
3a. The correct answer must have a constant term of  $+6$ .  
3b. G and I differ in the sign of the middle term. Use mental math to get the  $x^2$  term in the product.  
G.  $-3x^2 + 5x^2 = 2x^2$  ✓ I.  $-3x^2 - 5x^2 = -8x^2$ , the answer is G.

### CHAPTER REVIEW

pages 503–505

1. A 2. D 3. E 4. C 5. B 6.  $-6y^2 + 8y + 2$ ; quadratic trinomial  
7.  $9h^2 + 1$ ; quadratic binomial  
8.  $3k^5 + k$ ; fifth-degree binomial  
9.  $7t^2 + 8t + 9$ ; quadratic

- trinomial  
10.  $x^2y^2$ ; fourth-degree monomial  
11.  $x^3 + x^2 + 5$ ; cubic trinomial  
12. Answers may vary.  
Sample:  $3z^4 - 5z^2 + 1; 4$   
13.  $(-4b^5 + 3b^3 - b + 10) + (3b^5 - b^3 + b - 4) = (-4 + 3)b^5 + (3 - 1)b^3 + (-1 + 1)b + (10 - 4) = -b^5 + 2b^3 + 6$   
14.  $(3g^4 + 5g^2 + 5) + (5g^4 - 10g^2 + 11g) = (3 + 5)g^4 + (5 - 10)g^2 + 11g + 5 = 8g^4 - 5g^2 + 11g + 5$   
15.  $(3x^3 + 8x^2 + 2x + 9) - (-4x^3 + 5x - 3) = [3 - (-4)]x^3 + 8x^2 + (2 - 5)x + 9 - (-3) = 7x^3 + 8x^2 - 3x + 12$   
16.  $(2t^3 - 4t^2 + 9t - 7) - (t^3 + t^2 - 3t + 1) = (2 - 1)t^3 + (-4 - 1)t^2 + [9 - (-3)]t - 7 - 1 = t^3 - 5t^2 + 12t - 8$   
17.  $(6y^2 + 3y + 5) - (2y^2 + 1) = (6 - 2)y^2 + 3y + (5 - 1) = 4y^2 + 3y + 4$   
18.  $(7w^5 - 7w^3 + 3w) - (5w^4 - w^2 + 3) = (7w^5 - 5w^4 - 7w^3 + w^2 + 3w - 3$   
19.  $8x(2 - 5x) = 8x(2) - 8x(5x) = 16x - 40x^2 = -40x^2 + 16x$   
20.  $5g(3g + 7g^2 - 9) = 5g(3g) + 5g(7g^2) - 5g(9) = 15g^2 + 35g^4 - 45g = 35g^4 + 15g^2 - 45g$   
21.  $8t^2(3t - 4 - 5t^2) = 8t^2(3t) - 8t^2(4) - 8t^2(5t^2) = 24t^3 - 32t^2 - 40t^4 = -40t^4 + 24t^3 - 32t^2$   
22.  $5m(3m + m^2) = 5m(3m) + 5m(m^2) = 15m^2 + 5m^3 = 5m^3 + 15m^2$   
23.  $-2w^2(4w - 10 + 3w^2) = -2w^2(4w) - 2w^2(-10) - 2w^2(3w^2) = -8w^3 + 20w^2 - 6w^4 = -6w^4 - 8w^3 + 20w^2$   
24.  $b(10 + 5b - 3b^2) = b(10) + b(5b) - b(3b^2) = 10b + 5b^2 - 3b^3 = -3b^3 + 5b^2 + 10b$   
25.  $9x^4 = 3 \cdot 3 \cdot x^4; 12x^3 = 3 \cdot 2 \cdot 2 \cdot x^3; 6x = 3 \cdot 2 \cdot x; GCF = 3x; 9x^4 + 12x^3 + 6x = 3x(3x^3 + 4x^2 + 2)$   
26.  $4t^5 = 2 \cdot 2 \cdot t^5; 12t^3 = 3 \cdot 2 \cdot 2 \cdot t^3; 8t^2 = 2 \cdot 2 \cdot 2 \cdot t^2; GCF = 4t^2; 4t^5 - 12t^3 + 8t^2 = 4t^2(t^3 - 3t + 2)$   
27.  $40n^5 = 5 \cdot 2 \cdot 2 \cdot 2 \cdot n^5; 70n^4 = 7 \cdot 5 \cdot 2 \cdot n^4; 30n^3 = 5 \cdot 3 \cdot 2 \cdot n^3; GCF = 10n^3; 40n^5 + 70n^4 - 30n^3 = 10n^3(4n^2 + 7n - 3)$   
28.  $2k^4 = 2 \cdot k^4; 4k^3 = 2 \cdot 2 \cdot k^3; 6k = 3 \cdot 2 \cdot k; 8 = 2 \cdot 2 \cdot 2; GCF = 2; 2k^4 + 4k^3 - 6k - 8 = 2(k^4 + 2k^3 - 3k - 4)$   
29.  $3d^2 = 3 \cdot d^2; 6d = 3 \cdot 2 \cdot d; GCF = 3d; 3d^2 - 6d = 3d(d - 2)$   
30.  $10m^4 = 5 \cdot 2 \cdot m^4; 12m^3 = 3 \cdot 2 \cdot 2 \cdot m^3 = 4m^2 = 2 \cdot 2 \cdot m^2; GCF = 2m^2; 10m^4 - 12m^3 + 4m^2 = 2m^2(5m^2 - 6m + 2)$   
31.  $10v = 5 \cdot 2 \cdot v; 5 = 5; GCF = 5; 10v - 5 = 5(2v - 2)$   
32.  $12w^3 = 3 \cdot 2 \cdot 2 \cdot w^3; 8w^2 = 2 \cdot 2 \cdot 2 \cdot w^2; 20w = 5 \cdot 2 \cdot 2 \cdot w; GCF = 4w; 12w^3 + 8w^2 + 20w = 4w(3w^2 + 2w + 5)$   
33.  $18d^5 = 3 \cdot 3 \cdot 2 \cdot d^5; 6d^4 = 3 \cdot 2 \cdot d^4; 9d^3 = 3 \cdot 3 \cdot d^3; GCF = 3d^3; 18d^5 + 6d^4 + 9d^3 = 3d^3(6d^2 + 2d + 3)$   
34. 12; if the GCF of  $x$  and  $y$  is 3, then the GCF of  $4x$  and  $3y$  is  $4 \cdot 3 = 12$ .  
35.  $8m^2n = 4mn(m)$  and  $4mn = 4mn(1)$ , so their GCF is  $4mn$ . Kim is correct.  
36.  $(x + 3)(x + 5) = x^2 + 5x + 3x + 15 = x^2 + 8x + 15$   
37.  $(5v + 2)(3v - 7) = 15v^2 - 35v + 6v - 14 = 15v^2 - 29v - 14$   
38.  $(2b + 5)(3b - 2) = 6b^2 - 4b + 15b - 10 = 6b^2 + 11b - 10$   
39.  $(k - 1)(-k + 4) = -k^2 + 4k + k - 4 = -k^2 + 5k - 4$   
40.  $(p + 2)(p^2 + p + 1) = p^3 + p^2 + p + 2p^2 + 2p + 2 = p^3 + 3p^2 + 3p + 2$   
41.  $(4a - 1)(a - 5) = 4a^2 - 20a - a + 5 = 4a^2 - 21a + 5$   
42.  $(y - 4)(y^2 - 5y - 2) = y^3 - 5y^2 - 2y - 4y^2 + 20y + 8 = y^3 - 9y^2 + 18y + 8$

43.  $(3x + 4)(x + 2) = 3x^2 + 6x + 4x + 8 = 3x^2 + 10x + 8$   
 44.  $(-2h^2 + h - 1)(h - 5) = -2h^3 + 10h^2 + h^2 - 5h - h + 5 = -2h^3 + 11h^2 - 6h + 5$

45.  $(q - 4)(q - 4) = q^2 - 2(q)4 + 4^2 = q^2 - 8q + 16$

46.  $(2k^3 + 5)^2 = (2k^3)^2 + 2(2k^3)5 + 5^2 = 4k^6 + 20k^3 + 25$

47.  $(8 - 3t^2)(8 + 3t^2) = 8^2 - (3t^2)^2 = 64 - 9t^4$

48.  $(2m^2 + 5)(2m^2 - 5) = (2m^2)^2 - 5^2 = 4m^4 - 25$

49.  $(w - 4)(w + 4) = w^2 - 4^2 = w^2 - 16$

50.  $(4g^2 - 5h^4)(4g^2 + 5h^4) = (4g^2)^2 - (5h^4)^2 =$

16g<sup>4</sup> - 25h<sup>8</sup>

51. Area =  $(2x + 1)(x + 4) = 2x^2 + 9x + 4$

52. No;  $(x - y)^2 = x^2 - 2xy + y^2 \neq x^2 - y^2$

53.  $1 \cdot 2 = 2; 1 + 2 = 3; x^2 + 3x + 2 = (x + 2)(x + 1)$

54.  $-7 \cdot -2 = 14; -7 + (-2) = -9; y^2 - 9y + 14 =$

(y - 7)(y - 2)

55.  $-5 \cdot 3 = -15; -5 + 3 = -2;$

x<sup>2</sup> - 2x - 15 = (x - 5)(x + 3)

56.  $2w^2 - w = 2 \cdot 1 \cdot 1 = -4$

$2 \cdot 1 \cdot 1 + 1 \cdot -3 = -1 \checkmark$

$2 \cdot 1 \cdot -3 = -6$

(2w + 1)(w - 3) = 2w<sup>2</sup> - w - 3

57.  $b^2 - 7b + 12 = (b - 3)(b - 4)$

58.  $2t^2 + 3t = 2 \cdot 1 \cdot 1 = -3$

$2 \cdot 1 \cdot -2 + 1 \cdot 1 = 0$

$2 \cdot 1 \cdot 1 + 1 \cdot -2 = -1 \checkmark$

$2 \cdot 1 \cdot -1 = 2$

(2t - 1)(t + 2) = 2t<sup>2</sup> + 3t - 2

59.  $x^2 + 5x - 6 = (x + 6)(x - 1)$

60.  $6x^2 + 10x + 4 = 2(3x^2 + 5x + 2) = 2(3x + 2)(x + 1)$

61.  $21 \cdot -8 = 3 \cdot -56 = 4 \cdot -42 = 6 \cdot -28; 6 + (-28) =$

-22;  $21x^2 + 6x - 28x - 8 = 3x(7x + 2) - 4(7x + 2) =$

(3x - 4)(7x + 2)

62.  $3x^2 + x = 3 \cdot 1 \cdot 1 = -5$

$3 \cdot 1 \cdot 1 + 1 \cdot -2 = 1 \checkmark$

(3x - 2)(x + 1) = 3x<sup>2</sup> + x - 2

63.  $15y^2 + 16y = 15 \cdot 1 \cdot 1 = 16 \checkmark$

(15y + 1)(y + 1) = 15y<sup>2</sup> + 16y + 1

64.  $15y^2 - 16y = 15 \cdot 1 \cdot 1 = 16$

$15 \cdot 1 \cdot 1 + 1 \cdot -1 = -16 \checkmark$

$15 \cdot 1 \cdot -1 + 1 \cdot 1 = 16$

(15y - 1)(y - 1) = 15y<sup>2</sup> - 16y + 1

65.  $q^2 + 2q + 1 = q^2 + 2(q)1 + 1^2 = (q + 1)^2$

66.  $b^2 - 16 = b^2 - 4^2 = (b + 4)(b - 4)$

67.  $x^2 - 4x + 4 = x^2 - 2(x)2 + 2^2 = (x - 2)^2$

68.  $4t^2 - 121 = (2t)^2 - 11^2 = (2t - 11)(2t + 11)$

69.  $4d^2 - 20d + 25 = (2d)^2 - 2(4d)5 + 5^2 = (2d - 5)^2$

70.  $9c^2 + 6c + 1 = (3c)^2 + 2(3c)1 + 1^2 = (3c + 1)^2$

71.  $9k^2 - 25 = (3k)^2 - 5^2 = (3k - 5)(3k + 5)$

72.  $x^2 + 6x + 9 = x^2 + 2(x)3 + 3^2 = (x + 3)^2$

73.  $24y^2 - 6 = 6(4y^2 - 1) = 6[(2y)^2 - 1^2] =$

$6(2y - 1)(2y + 1)$

74.  $\frac{1}{4}d^2 + d + 1 = (\frac{1}{2}d)^2 + 2(\frac{1}{2}d)1 + 1^2 = (\frac{1}{2}d + 1)^2$ ; side has length

$\frac{1}{2}d + 1$ .

75. The factors are equal.

76. No; only the square  $(5u + 6)^2$  would have  $25u^2$  and 36 as the first and last terms; however,  $2(5u)(6) \neq 65u$ .

77.  $4x^2$ ;

and last terms; however,  $2(5u)(6) \neq 65u$ .

78.  $3k^2$ ;

79.  $24y^2$ ;

80.  $10n^3$ ;

81.  $6x^3 + 3x^2 + 8x + 4 = 3x^2(2x + 1) + 4(2x + 1) =$

$(3x^2 + 4)(2x + 1)$

82.  $20y^4 - 45y^2 = 5y^2(4y^2 - 9) =$

$5y(2y + 3)(2y - 3)$

83.  $9g^2 + 15g - 6 = 3(3g^2 + 5g - 2) = 3(3g - 1)(g + 2)$

84.  $6c^2 - 5cd = 6 \cdot 1 \cdot 1 + 1 \cdot -1 = -7$

$3 \cdot 2 \cdot 1 + 3 \cdot -1 + 2 \cdot -1 = -5 \checkmark$

$(3c - d)(2c - d) = 6c^2 - 5cd + 1$

85.  $11k^2 + 23k = 11 \cdot 1 \cdot 1 + 1 \cdot 2 = 13$

$1 \cdot 11 + 1 \cdot 1 + 11 \cdot 2 = 23 \checkmark$

$(11k + 1)(k + 2) = 11k^2 + 23k + 2$

86.  $3u^2 + 21u + 18 = 3(u^2 + 7u + 6) = 3(u + 1)(u + 6)$

87.  $15p^2 + 14p = 15 \cdot 1 \cdot 1 + 1 \cdot 3 = 18$

$3 \cdot 5 + 3 \cdot 1 + 5 \cdot 3 = 18$

$3 \cdot 5 + 3 \cdot 3 + 5 \cdot 1 = 14 \checkmark$

$(3p + 1)(5p + 3) = 15p^2 + 14p + 3$

88.  $3u^2 - 21u + 18 = 3(u^2 - 7u + 6) = 3(u - 1)(u - 6)$

89.  $15h^3 + 11h^2 - 45h - 33 = h^2(15h + 11) - 3(15h + 11) = (h^2 - 3)(15h + 11)$

90.  $30x^3 + 42x^2 - 5x - 7 = 6x^2(5x + 7) - (5x + 7) =$

$(6x^2 - 1)(5x + 7)$

91.  $12s^4t + 20s^3t - 8s^2t = 4s^2t(3s^2 + 5s - 2) = 4s^2t(3s - 1)(s + 2)$

92.  $2x^3 + 7x^2 + 4x + 14 = x^2(2x + 7) + 2(2x + 7) =$

$(x^2 + 2)(2x + 7)$

93.  $6p^3 + 38p^2 + 40p = 2p(3p^2 + 19p + 20) = 2p(p + 5)(3p + 4)$ ; the

dimensions are  $2p$ ,  $p + 5$ , and  $3p + 4$ .

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1.  $-2y^2 - 3y + 5$ ; quadratic trinomial

2.  $-2v^3 - 6v^2 - 17v$ ; cubic trinomial

3.  $8x^4 - 6x^2 - 10$

fourth-degree trinomial

4.  $-3k^5 - k^2$ ; fifth-degree binomial

5.  $(4x^2 + 2x + 5) + (7x^2 - 5x + 2) =$

$(4 + 7)x^2 + (2 - 5)x + 5 + 2 = 11x^2 - 3x + 7$

6.  $(9a^2 - 4 - 5a) - (12a - 6a^2 + 3) =$

$(9 + 6)a^2 + (-5 - 12)a - 4 - 3 = 15a^2 - 17a - 7$

7.  $(-4m^2 + m - 10) + (3m + 12 - 7m^2) =$

$(-4 - 7)m^2 + (1 + 3)m - 10 + 12 =$

$-11m^2 + 4m + 2$

8.  $(3c - 4c^2 + c^3) - (5c^2 + 8c^3 - 6c) =$

$(1 - 8)c^3 + (-4 - 5)c^2 + (3 + 6)c = -7c^3 - 9c^2 + 9c$

9. Answers may vary. Sample:  $p^6 + p^2 + 1$

10.  $x^2 + 3x + 2x + 6 = x^2 + 5x + 6$

11.  $8b(3b + 7 - b^2) = 8b(3b) + 8b(7) - 8b(b^2) =$

$-8b^3 + 24b^2 + 56b$

12.  $-t(5t^2 + t) = -t(5t^2) - t(t) =$

$-5t^3 - t^2$

13.  $3q(4 - q + 3q^3) = 9q^4 - 3q^2 + 12q$

14.  $2c(c^5 + 4c^3) = 2c(c^5) + 2c(4c^3) = 2c^6 + 8c^4$

15.  $(x + 6)(x + 1) = x^2 + 1x + 6x + 6 = x^2 + 7x + 6$

16.  $(d + 4)(d - 3) = d^2 - 3d + 4d - 12 = d^2 + d - 12$

17.  $(2h - 1)(h - 4) = 2h^2 - 8h - 1h + 4 =$

$2h^2 - 9h + 4$

18.  $(2m + 5)(3m - 7) = 6m^2 - 14m + 15m - 35 = 6m^2 + m - 35$

19.  $(p + 2)(2p^2 - 5p + 4) =$

$2p^3 - 5p^2 + 4p + 4p^2 - 10p + 8 =$

$2p^3 - p^2 - 6p + 8$

20.  $(a - 4)(6a^2 + 10a - 3) =$

- $$6a^3 + 10a^2 - 3a - 24a^2 - 40a + 12 =$$
- $$6a^3 - 14a^2 - 43a + 12 \quad 21. (3x + 5)(7x^2 - 2x + 1) =$$
- $$21x^3 + 29x^2 - 7x + 5 \quad 22. 21x^4 = 7 \cdot 3 \cdot x^4; 18x^2 =$$
- $$3 \cdot 3 \cdot 2 \cdot x^2; 36x^3 = 3 \cdot 3 \cdot 2 \cdot 2 \cdot x^3; \text{GCF} = 3x^2$$
- $$23. \text{GCF} = t \quad 24. 3a^{10} = 3 \cdot a^{10}; 9a^5 = 3 \cdot 3 \cdot a^5; 6a^{15} =$$
- $$3 \cdot 2 \cdot a^{15}; \text{GCF} = 3a^5 \quad 25. 9m^3 = 3 \cdot 3 \cdot m^3; 7m^4 =$$
- $$7 \cdot m^4; 8m^2 = 2 \cdot 2 \cdot m^2; \text{GCF} = m^2 \quad 26. \text{Multiply each term of the first polynomial by each term of the second polynomial. Then combine like terms. Example: } (x+3)(x^2-x+1) = x^3 - x^2 + x + 3x^2 - 3x + 3 =$$
- $$x^3 + 2x^2 - 2x + 3 \quad 27. \text{width} = x; \text{length} = 3x + 5;$$
- $$\text{area} = x(3x + 5) = 3x^2 + 5x \text{ [m]} \quad 28. \text{width} = w;$$
- $$\text{height} = w - 2; \text{length} = 4w + 4; \text{volume} =$$
- $$w(w-2)(4w+3) = w(4w^2 - 5w - 6) =$$
- $$4w^3 - 5w^2 - 6w; (4w^3 - 5w^2 - 6w) \text{ in.}^3$$
- $$29. \frac{1}{2}(2x)(4x-3) = 4x^2 - 3x$$
- $$30. 3x(2x+1) - 2x(x+1) = 6x^2 + 3x - 2x^2 - 2x =$$
- $$4x^2 + x \quad 31. -7 \cdot 2 = -14; -7 + 2 =$$
- $$-5; w^2 - 5w - 14 = (w-7)(w+2)$$
- $$32. g^2 + 10g + 25 = g^2 + 2(g)5 + 5^2 = (g+5)^2$$
- $$33. 9k^2 + 24k + 16 = (3k)^2 + 2(3k) + 4^2 = (3k+4)^2$$
- $$34. n^2 - 100 = (n+10)(n-10) \quad 35. y^2 - 4y + 4 =$$
- $$(y-2)^2 \quad 36. 4x^2 - 49 = (2x)^2 - 7^2 = (2x+7)(2x-7)$$
- $$37. 4p^2 + 164p + 81$$
- $$4 \cdot 1 \quad 4 \cdot 81 + 1 \cdot 1 = 325 \quad 1 \cdot 81$$
- $$2 \cdot 2 \quad 2 \cdot 1 + 2 \cdot 81 = 164 \checkmark \quad 1 \cdot 81$$
- $$(2p+1)(2p+81) = 4p^2 + 164p + 81$$

- $$38. 13c^2 - 52 = 13(c^2 - 4) = 13(c+2)(c-2)$$
- $$39. \blacksquare = 2(1)(7) = 14 \quad 40. 12 = 2(3)(\blacksquare); \blacksquare = 2$$
- $$41. 2(3)(5) = 30, \text{ so } \blacksquare = 5^2 = 25 \quad 42. \blacksquare = 2(2)(9) = 36$$
- $$43. 3x^2; -4 \quad 44. 4n^2; -1 \quad 45. 12n^3 + 15n^2 + 4n + 5 =$$
- $$3n^2(4n+5) + (4n+5) = (3n^2+1)(4n+5)$$
- $$46. 4x^2 - 10x + 6 = 2(2x^2 - 5x + 3) =$$
- $$2(2x-3)(x-1) \quad 47. x^3 - 5x^2 + 5x - 25 =$$
- $$x^2(x-5) + 5(x-5) = (x^2+5)(x-5)$$
- $$48. 6r^3 - 9r^2 - 4r + 6 = 3r^2(2r-3) - 2(2r-3) =$$
- $$(3r^2-2)(2r-3) \quad 49. 12y^3 + 28y^2 - 3y - 7 =$$
- $$4y^2(3y+7) - (3y+7) = (4y^2-1)(3y+7) =$$
- $$(2y+1)(2y-1)(3y+7) \quad 50. 3n^3 - 4n^2 - 6n + 8 =$$
- $$n^2(3n-4) - 2(3n-4) = (n^2-2)(3n-4)$$

51. Answers may vary. Sample:

$$x^2 + ax + 30 = (x+1)(x+30); a = 31$$

$$(x+2)(x+15); a = 17$$

$$(x+3)(x+10); a = 13$$

$$(x+5)(x+6); a = 11$$

### STANDARDIZED TEST PREP

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- $1. 20,000(1.05)^3 = 23,152.50$ ; the answer is C.
- The answer is G.
- The answer is B.
- $4. 4,870(1.04)^3 = 5478$ ;  $0.25 \cdot 23,152 = 5788$ ; the answer is F.
- $5a. 1000(1.06)^{10} \approx 1790.85$ ; \$1790.85
- $5b. \text{Interest} = 1790.85 - 1000 = 790.85$ ;  $0.23 \cdot 790.85 = 181.90$  [\$].