



Exponents and Exponential Functions

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DIAGNOSING READINESS

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- $\frac{7}{10} = 0.7$
- $6\frac{2}{5} = 6\frac{4}{10} = 6.4$
- $3 \cdot \frac{8}{1000} = 0.008$
- $\frac{7}{2} = 3\frac{1}{2} = 3.5$
- $5 \cdot \frac{3}{11} = 0.272727\dots = 0.\overline{27}$
- $(9 \div 3 + 4)^2 = (3 + 4)^2 = 7^2 = 49$
- $7 \cdot 5 + (0.3)^3 = 5 + 0.027 = 5.027$
- $8 \cdot 3 - (1.5)^2 = 3 - 2.25 = 0.75$
- $9. 64 \div 2^4 = 64 \div 16 = 4$
- $10. [(-2)(5)]^2 = (-10)^2 = 100$
- $11. (-2 - 5)^2 = (-7)^2 = 49$
- $12. (-2)^3 + 5^2 = -8 + 25 = 17$
- $13. 5 - [3(-2)]^2 = 5 - (-6)^2 = 5 - 36 = -31$
- $14. I = Prt = 1000 \cdot 0.03 \cdot 4 = 120$ [\$120]
- $15. I = Prt$
 $P = \frac{I}{rt} = \frac{672}{0.07 \cdot 12} = 800$ [\$800]

- $f(-2) = -2(-2)^2 = -8; f(0) = -2(0)^2 = 0;$
 $f(3.5) = -2(3.5)^2 = -24.5;$ range = $\{-24.5, -8, 0\}$
- $g(-2) = 10 - (-2)^3 = 10 + 8 = 18; g(0) = 10 - 0^3 = 10 - 0 = 10; g(3.5) = 10 - 3.5^3 = 10 - 42.875 = -32.875;$ range = $\{-32.875, 10, 18\}$
- $y(-2) = 5(-2) - 1 = -10 - 1 = -11; y(0) = 5 \cdot 0 - 1 = -1; y(3.5) = 5 \cdot 3.5 - 1 = 17.5 - 1 = 16.5;$ range = $\{-11, -1, 16.5\}$
- $19. 9, 11$
- $20.$ differences = 1, 2, 3, 4; next differences = 5, 6; next terms = 14, 20
- $21. 31, 37$

8-1 Zero and Negative Exponents

pages 394–399

Check Skills You'll Need For complete solutions see *Daily Skills Check and Lesson Quiz Transparencies or Presentation Pro CD-ROM*.

1. 8 2. $\frac{1}{16}$ 3. 4 4. -27 5. -27 6. 3 7. $\frac{1}{2}$ 8. -1 9. 4

Investigation

1a.

2^x	5^x	10^x
$2^4 = 16$	$5^4 = 625$	$10^4 = 10,000$
$2^3 = 8$	$5^3 = 125$	$10^3 = 1000$
$2^2 = 4$	$5^2 = 25$	$10^2 = 100$

1b. Left column: each term is (previous term) $\div 2$; middle column: each term is (previous term) $\div 5$; right column: each term = (previous term) $\div 10$.

2.

2^x	5^x	10^x
$2^1 = 2$	$5^1 = 5$	$10^1 = 10$
$2^0 = 1$	$5^0 = 1$	$10^0 = 1$
$2^{-1} = \frac{1}{2}$	$5^{-1} = \frac{1}{5}$	$10^{-1} = \frac{1}{10}$
$2^{-2} = \frac{1}{4}$	$5^{-2} = \frac{1}{25}$	$10^{-2} = \frac{1}{100}$

3. The values are all 1.

4a. $2^{-1} = 1\frac{1}{2}$ 4b. $2^{-2} = \frac{1}{2^2}$ 4c. $2^{-3} = \frac{1}{2^3}$

Check Understanding 1a. $3^{-4} = \frac{1}{3^4} = \frac{1}{81}$ 1b. $(-7)^0 = 1$

1c. $(-4)^{-3} = \frac{1}{(-4)^3} = \frac{1}{-64} = -\frac{1}{64}$ 1d. $7^{-1} = \frac{1}{7}$

1e. $-3^{-2} = -(3^{-2}) = -\frac{1}{3^2} = -\frac{1}{9}$ 2a. $11m^{-5} = \frac{11}{m^5}$

2b. $7s^{-4}t^2 = \frac{7t^2}{s^4}$ 2c. $\frac{2}{a^{-3}} = 2a^3$ 2d. $\frac{n^{-5}}{v^2} = \frac{1}{n^5v^2}$

3a. $n^{-3}w^0 = \frac{1}{n^3} = \frac{1}{(-2)^3} = \frac{1}{-8} = -\frac{1}{8}$ 3b. $\frac{n^{-1}}{w^2} = \frac{1}{nw^2} = \frac{1}{(-2)^5} = -\frac{1}{50}$

3c. $\frac{w^0}{n^4} = \frac{1}{n^4} = \frac{1}{(-2)^4} = \frac{1}{16}$ 3d. $\frac{1}{nw^{-2}} = \frac{w^2}{n} = \frac{5^2}{-2} = -12.5$

4. $5400 \cdot 3^{-2} = \frac{5400}{3^2} = \frac{5400}{9} = 600$;
 $5400 \cdot 3^0 = 5400 \cdot 1 = 5400$. 5400 = bacterial population at beginning of 0th month. 600 = population 2 months earlier.

Exercises 1. $-(2.57)^0 = -1$ 2. $4^{-2} = \frac{1}{4^2} = \frac{1}{16}$

3. $(-5)^{-2} = \frac{1}{(-5)^2} = \frac{1}{25}$ 4. $-5^{-2} = -\frac{1}{5^2} = -\frac{1}{25}$

5. $(-4)^{-2} = \frac{1}{(-4)^2} = \frac{1}{16}$ 6. $-3^{-4} = -\frac{1}{3^4} = -\frac{1}{81}$

7. $2^{-6} = \frac{1}{2^6} = \frac{1}{64}$ 8. $-12^{-1} = -\frac{1}{12}$ 9. $\frac{1}{2^0} = \frac{1}{1} = 1$

10. $78^{-1} = \frac{1}{78}$ 11. $(-4)^{-3} = \frac{1}{(-4)^3} = \frac{1}{-64} = -\frac{1}{64}$

12. $-4^{-3} = -\frac{1}{4^3} = -\frac{1}{64}$ 13. $4n^{-2} = \frac{4}{n^2}$ 14. $\frac{x^3}{2y^4} = \frac{1}{2x^{-3}y^4}$

15. $\frac{a^0}{3b^{-3}} = \frac{b^3}{3}$ 16. $3xy^{-5} = \frac{3x}{y^5}$ 17. $3ab^0 = 3a \cdot 1 = 3a$

18. $5x^{-4} = \frac{5}{x^4}$ 19. $\frac{1}{x^{-7}} = x^7$ 20. $\frac{1}{c^{-1}} = c$ 21. $\frac{5^{-2}}{p} = \frac{1}{25p}$

22. $a^{-4}c^0 = \frac{1}{a^4}$ 23. $\frac{3x^{-2}}{y} = \frac{3}{x^2y}$ 24. $\frac{7ab^{-2}}{3w} = \frac{7a}{3b^2w}$

25. $x^{-5}y^{-7} = \frac{1}{x^5y^7}$ 26. $x^{-5}y^7 = \frac{y^7}{x^5}$ 27. $\frac{8}{2c^{-3}} = 4c^3$

28. $\frac{7s}{5t^{-3}} = \frac{7st^3}{5}$ 29. $\frac{6a^{-1}c^{-3}}{d^0} = \frac{6}{ac^3}$ 30. $2^{-3}x^2z^{-7} = \frac{x^2}{8z^7}$

31. $9^0y^7t^{-11} = \frac{y^7}{t^{11}}$ 32. $\frac{7s^0t^{-5}}{2^{-1}m^2} = \frac{14}{m^2t^5}$ 33. $s^{-2} = \frac{1}{s^2} = \frac{1}{5^2} = \frac{1}{25}$

34. $(-3)^{-2} = \frac{1}{(-3)^2} = \frac{1}{9}$ 35. $-(-3)^{-2} = -\frac{1}{(-3)^2} = -\frac{1}{9}$

36. $s^0 = 1$ 37. $3 \cdot 5^{-2} = \frac{3}{5^2} = \frac{3}{25}$

38. $(2 \cdot 5)^{-2} = \frac{1}{10^2} = \frac{1}{100}$ 39. $(-3)^{-4}5^2 = \frac{5^2}{(-3)^4} = \frac{25}{81}$

40. $\frac{1}{(-3)^{-4}5^2} = \frac{(-3)^4}{5^2} = \frac{81}{25}$ 41. $5^2(-3)^{-3} = \frac{25}{(-3)^3} = \frac{25}{-27} = -\frac{25}{27}$

42. $(-3)^05^{-2} = \frac{1}{5^2} = \frac{1}{25}$ 43. $5(-3)^35^{-1} = \frac{5(-27)}{5} = -27$

44. $2^{-4}(-3)^35^{-2} = \frac{(-3)^3}{2^45^2} = \frac{-27}{16 \cdot 25} = -\frac{27}{400}$

45a. Let w = number of weeks after this week.
 $\text{Allowance} = a = 2.56 \cdot 2^w = 2.56 \cdot 2^3 = 2.56 \cdot 8 = 20.48$ [\$20.48]; $2.56 \cdot 2^{-3} = \frac{2.56}{8} = 0.32$ [\$0.32]

45b. No; after a year, the allowance would increase by a factor of $2^{52} = 4,500,000,000,000,000$. 46. neg. 47. pos.

48. pos. 49. neg. 50. neg. 51. $\frac{1}{10} = 0.1 = 10^{-1}$

52. $\frac{1}{100} = 0.01 = 10^{-2}$ 53. $\frac{1}{1000} = 10^{-3}$ 54. $\frac{1}{10,000} = 10^{-4}$

55. $\frac{1}{100,000} = 10^{-5}$ 56. $10^{-3} = 0.001$ 57. $10^{-6} =$

0.000001 58. $7 \cdot 10^{-1} = 0.7$ 59. $3 \cdot 10^{-2} = 0.03$

60. $5 \cdot 10^{-4} = 0.0005$ 61a. $\frac{1}{5^2} = 5^{-2}$; $\frac{1}{5^1} = 5^{-1}$; $\frac{1}{5^0} = 5^0$;
 $\frac{1}{5^{-1}} = 5^1$; $\frac{1}{5^{-2}} = 5^2$ 61b. $\frac{1}{5^{-4}} = 5^4$ 61c. $\frac{1}{a^{-n}} = \frac{a^n}{1}$

62. The expression -3^0 means $-(3^0) = -(1) = -1$; the expression $(-3)^0$ means (any nonzero number) $^0 = 1$.

63. $45 \cdot (0.5)^0 = 45 \cdot 1 = 45$ 64. $54 \cdot 3^{-2} = \frac{54}{3^2} = \frac{54}{9} = 6$

65. $\frac{5^{-2}}{10^{-3}} = \frac{10^3}{5^2} = \frac{1000}{25} = 40$ 66. $\frac{4^{-1}}{9^0} = \frac{1}{4}$ 67. $\frac{(-3)^{-4}}{-3} =$
 $\frac{1}{(-3)^5} = -\frac{1}{243}$ 68. $c^b = (-4)^2 = 16$ 69. $3^{-2} \cdot 2 = \frac{2}{3^2} = \frac{2}{9}$

70. $2^{-3} = \frac{1}{2^3} = \frac{1}{8}$ 71. $2^{-4} = \frac{1}{2^4} = \frac{1}{16}$ 72. $(-4)^{-3} \cdot 2^{3 \cdot 2} =$
 $\frac{2^6}{(-4)^3} = -\frac{64}{64} = -1$

73.

a	4	$\frac{1}{3}$	6	$\frac{7}{8}$	2
a^{-1}	$\frac{1}{4}$	3	$\frac{1}{6}$	$\frac{8}{7}$	0.5

74a. $a^n \cdot a^{-n} = a^{n+(-n)} = a^0 = 1$, $a \neq 0$ 74b. a^n and a^{-n} are

reciprocals for $a \neq 0$; $\frac{1}{a^n} = a^{-n}$ and $\frac{1}{a^{-n}} = a^n$. 75. A. $4^{-1} = \frac{1}{4}$ B. $2^{-2} = \frac{1}{2^2} = \frac{1}{4}$ C. $-4^1 = -4$ D. $\frac{1}{2^2} = \frac{1}{4}$ E. $1^4 = 1$

F. $-2^{-2} = -\frac{1}{2^2} = -\frac{1}{4}$; A, B, D 76. Check students' work.

77. No; when you form the reciprocal of an expression on the line you move the *entire* expression to the denominator; the reciprocal of $3x^{-2}$ is $\frac{1}{3x^{-2}}$. 78. b^0 is b raised to the power 0, which equals 1, not $b \cdot 0$.

79a.

Number correct	Expression	Probability
0	$p^0 q^4$	$\left(\frac{1}{5}\right)^0 \left(\frac{4}{5}\right)^4 = 0.4096$
1	$4p^1 q^3$	$4\left(\frac{1}{5}\right)^1 \left(\frac{4}{5}\right)^3 = 0.4096$
2	$6p^2 q^2$	$6\left(\frac{1}{5}\right)^2 \left(\frac{4}{5}\right)^2 = 0.1536$
3	$4p^3 q^1$	$4\left(\frac{1}{5}\right)^3 \left(\frac{4}{5}\right)^1 = 0.0256$
4	$p^4 q^0$	$\left(\frac{1}{5}\right)^4 \left(\frac{4}{5}\right)^0 = 0.0016$

79b. 0 or 1; only blind guessing was allowed.

80. $\frac{30}{1 + 29 \cdot 2^{-2}} = \frac{30}{1 + 29\left(\frac{1}{2^2}\right)} = \frac{30}{1 + \frac{29}{4}} = 4\left(\frac{30}{4 + 29}\right) =$

3.63; $\frac{30}{1 + 29 \cdot 2^{-5}} = \frac{30}{1 + 29\left(\frac{1}{2^5}\right)} = \frac{30}{1 + \frac{29}{32}} =$

$32\left(\frac{30}{32 + 29}\right) = 15.74$; $\frac{30}{1 + 29 \cdot 2^{-10}} = \frac{30}{1 + 29\left(\frac{1}{2^{10}}\right)} =$

$\frac{30}{1 + \frac{29}{1024}} = 1024\left(\frac{30}{1024 + 29}\right) = 29.17$;

about 4 students; about 16 students; about 29 students

81. $2^3(5^0 - 6m^2) = 8(1 - 6m^2) = 8 - 48m^2$

82. $(-5)^2 - (0.5)^{-2} = 25 - \frac{1}{(0.5)^2} = 25 - \frac{1}{0.25} =$

$25 - 4 = 21$ 83. $\frac{6}{m^2} + \frac{5m^{-2}}{3^{-3}} = \frac{6}{m^2} + \frac{5(3^3)}{m^2} = \frac{6}{m^2} + \frac{135}{m^2} =$

84. $(0.8)^{-3} + 19^0 - 2^{-6} = \frac{1}{0.8^3} + 1 - \frac{1}{2^6} =$

$\frac{1}{0.512} + 1 - \frac{1}{64} = 1.953125 + 1 - 0.015625 = 2.9375$

85. $\frac{2r^{-5}y^3}{n^2} \div \frac{r^2y^5}{2n} = \frac{2r^{-5}y^3}{n^2} \cdot \frac{2n}{r^2y^5} = \frac{4}{n^{2-1}r^{5+2}y^{5-3}} = \frac{4}{nr^7y^2}$

86. $2^{-1} - \frac{1}{3^{-2}} + 5\left(\frac{1}{2^2}\right) = \frac{1}{2} - 3^2 + \frac{5}{4} = \frac{2}{4} - 9 + \frac{5}{4} = -7\frac{1}{4}$

87. $n^{-3} = \left(\frac{1}{n}\right)^5$

$\frac{1}{n^3} = \frac{1}{n^5}$

$1 = \frac{1}{n^2}$

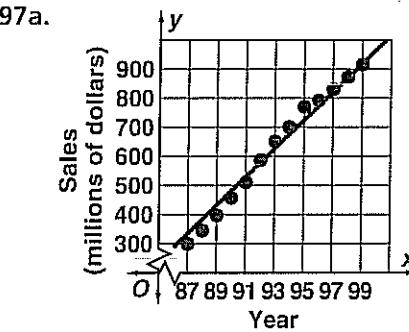
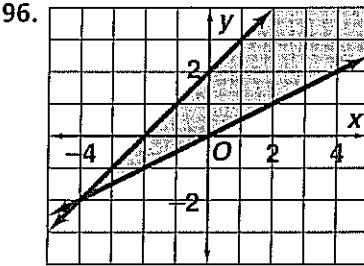
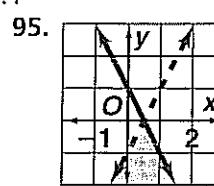
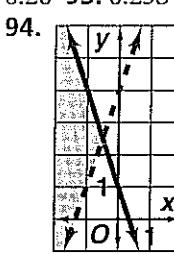
$n^2 = 1$

$n = 1$ and -1

88. $2 \cdot 3^{-1} = \frac{2}{3}$ 89. $\frac{3^{-2}b^2}{a^0 b^2} = \frac{1}{3^2} = \frac{1}{9}$ 90. $(4 \cdot 2 \cdot 1)^{-2} =$

$8^{-2} = \frac{1}{8^2} = \frac{1}{64}$ 91. $-6(-6)^{-1} = -\frac{6}{6} = 1$ 92. $26 \cdot 10^{-2} =$

0.26 93. $0.2584 \cdot 10^3 = 258.4$



97b. Let $x = 87$ correspond to 1987 and $y =$ sales in \$millions. Trend line goes through points (87, 300) and (99, 915). 97c. Slope is $\frac{915 - 300}{99 - 87} = \frac{615}{12} = 51$; $y = 51x - 4137$.

97d. In 2005, $x = 18$; $y = 51 \cdot 105 - 4137 = 1218$; sales are predicted to be \$1,218,000,000. 98. $y = -x + 4$

99. $y = 5x - 2$ 100. $y = \frac{2}{5}x - 3$ 101. $y = -\frac{3}{11}x - 17$

102. $y = \frac{5}{9}x + \frac{1}{3}$ 103. $y = 1.25x - 3.79$

8-2 Scientific Notation pages 400-404

Check Skills You'll Need For complete solutions see Daily Skills Check and Lesson Quiz Transparencies or Presentation Pro CD-ROM.

1. 60,000 2. 0.07 3. 820,000 4. 0.003 5. 34 6. 524

7. 367.8

- $(1.025)^{2-2} = (1.025)^0 = 1$ $7 \cdot c^{-2}c^7 = c^{-2+7} = c^5$
8. $3r \cdot r^4 = 3r^{1+4} = 3r^5$ $9. 5t^{-2} \cdot 2t^{-5} =$
 $(5 \cdot 2)(t^{-2} \cdot t^{-5}) = 10t^{-2-5} = 10t^{-7}$ $10. (7x^5)(8x) =$
 $(7 \cdot 8)(x^{5+1}) = 56x^6$ $11. 3x^2 \cdot x^2 = 3x^{2+2} = 3x^4$
12. $(-2.4n^4)(2n^{-1}) = (-2.4 \cdot 2)(n^4 \cdot n^{-1}) =$
 $-4.8n^{4-1} = -4.8n^3$ $13. b^{-2} \cdot b^4 \cdot b = b^{-2+4+1} = b^3$
14. $(-2m^3)(3.5m^{-3}) = (-2 \cdot 3.5)(m^{3-3}) = -7m^0 =$
 $-7 \cdot 1 = -7$ $15. (15a^3)(-3a) = (15 \cdot -3)(a^{3+1}) =$
 $-45a^4$ $16. (x^5y^2)(x^{-6}y) = (x^5 \cdot x^{-6})(y^2 \cdot y) =$
 $x^{5-6} \cdot y^{2+1} = x^{-1} \cdot y^3 = \frac{y^3}{x}$ $17. (5x^5)(3y^6)(3x^2) =$
 $5x^5 \cdot 3x^2 \cdot 3y^6 = 45x^{5+2}y^6 = 45x^7y^6$
18. $(4c^4)(ac^3)(3a^5c) = 12a^{1+5}c^{4+3+1} = 12a^6c^8$
19. $x^6 \cdot y^2 \cdot x^4 = x^6 \cdot x^4 \cdot y^2 = x^{6+4}y^2 = x^{10}y^2$
20. $a^6b^3 \cdot a^2b^{-2} = a^{6+2}b^{3-2} = a^8b^1 = a^8b$
21. $-m^2 \cdot 4r^3 \cdot 12r^{-4} \cdot 5m =$
 $-4 \cdot 12 \cdot 5 \cdot m^{2+1} \cdot r^{3-4} = -240m^3r^{-1} = -240\frac{m^3}{r}$
22. $(2 \times 10^3)(3 \times 10^2) = (2 \cdot 3)(10^3 \cdot 10^2) =$
 $6 \times 10^{3+2} = 6 \times 10^5$ **23.** $(2 \times 10^6)(3 \times 10^3) =$
 $(2 \cdot 3) \cdot 10^{6+3} = 6 \times 10^9$ **24.** $(4 \times 10^6) \cdot 10^{-3} =$
 $4 \times 10^{6-3} = 4 \times 10^3$ **25.** $(1 \times 10^3)(3.4 \times 10^{-8}) =$
 $1 \cdot 3.4 \cdot 10^{3-8} = 3.4 \times 10^{-5}$ **26.** $(8 \times 10^{-5})(7 \times 10^{-3}) =$
 $8 \cdot 7 \cdot 10^{-5-3} = 56 \times 10^{-8} = 5.6 \times 10^{-7}$
27. $(5 \times 10^7)(3 \times 10^{14}) = 5 \cdot 3 \cdot 10^{7+14} = 15 \times 10^{21} =$
 1.5×10^{22} **28.** $5.88 \times 10^{12} \frac{\text{miles}}{\text{light-year}} \cdot 4.35 \text{ light-years} =$
 $(5.88 \cdot 4.35) \times 10^{12} \text{ miles} = 25.578 \times 10^{12} \text{ miles} \approx$
 $2.56 \times 10^{13} \text{ miles}$ **29.** $120 \times 10^{12} \cdot 9 \times 10^6 =$
 $120 \cdot 9 \cdot 10^{12+6} = 1080 \times 10^{18} = 1.08 \times 10^{21} \text{ [dollars]}$
30. distance $= (3 \times 10^5 \text{ km/s}) \cdot (1.28 \times 10^0 \text{ s}) =$
 $3.84 \times 10^5 \text{ km}$ **31.** $5^2 \cdot 5^9 = 5^{11}$
32. $5^7 \cdot 5^{-4} = 5^3$ **33.** $2^{-3} \cdot 2^4 = 2^1$ **34.** $c^{-5} \cdot c^{11} = c^6$
35. $m^{-5} \cdot m^{-4} = m^{-9}$ **36.** $a \cdot a \cdot a^3 = a^5$ **37.** $a^{-4} \cdot a^4 =$
 1 **38.** $a^{12} \cdot a^0 = a^{12}$ **39.** $x^3y^2 \cdot x^{-3} = y^2$ **40.** area $=$
 $2x(3x^2 + x) = 6x^3 + 2x^2$ **41.** $(2x^2)^2 = 4x^4$ **42.** area $=$
base \cdot height $= 4y^2(y^3 + 2) = 4y^5 + 8y^2$ **43.** area $=$
 $\frac{1}{2}bh = \frac{1}{2}(2c^3)(4c) = 4c^4$ **44.** The error is in multiplying
the exponents instead of adding them. $(3x^2)(-2x^4) =$
 $3(-2)x^{2+4} = -6x^6$ **45.** The error is in adding the
coefficients instead of multiplying them. $4a^2 \cdot 3a^5 =$
 $(4 \cdot 3)a^{2+5} = 12a^7$ **46.** The error is in overlooking the
exponent of 1 on x: $x^6 \cdot x \cdot x^3 = x^6 \cdot x^1 \cdot x^3 = x^{6+1+3} =$
 x^{10} **47.** The error is in overlooking the fact that the
exponent 4 applies only to the 3, and the 2 exponent applies
only to the 2. You can't really simplify this expression
unless you multiply it out. **48.** $(9 \times 10^7)(3 \times 10^{-16}) =$
 $(9 \cdot 3)(10^7 \cdot 10^{-16}) = 27 \times 10^{7-16} = 27 \times 10^{-9} =$
 2.7×10^{-8} **49.** $(8 \times 10^{-3})(0.1 \times 10^9) = 8 \cdot 0.1 \times 10^6 =$
 8×10^{-5} **50.** $(0.7 \times 10^{-12})(0.3 \times 10^8) = 0.21 \times 10^{-4} =$
 2.1×10^{-5} **51.** $(0.4 \times 10^0)(3 \times 10^{-4}) = 1.2 \times 10^{-4}$
52. $(0.2 \times 10^5)(4 \times 10^{-12}) = 0.8 \times 10^{-7} = 8 \times 10^{-8}$
53. $(0.5 \times 10^{13})(0.3 \times 10^{-4}) = 0.15 \times 10^9 = 1.5 \times 10^8$
54. $(1 \text{ mole}) \left(6.02 \times 10^{23} \frac{\text{atoms}}{\text{mole}} \right) \left(1.67 \times 10^{-24} \frac{\text{gram}}{\text{atom}} \right) =$
 $(6.02 \cdot 1.67)(10^{23} \cdot 10^{-24}) \text{ g} = (10.0534 \times 10^{-1}) \text{ g} \approx$
 1.01 g **55a.** $y^8 = y^1y^7 = y^2y^6 = y^3y^5 = y^4y^4$
55b. Answers may vary. Sample: $y = y^{-1}y^9 = y^{-2}y^{10} =$
 $y^{-3}y^{11} = y^{-4}y^{12} = \dots$ **55c.** An infinite number; the
sequence in Problem 55b could be carried on indefinitely.

- $y^8 = y^{-n}y^{8+n}, n = 1, 2, 3, 4, 5, \dots$ **56a.** $1000 \cdot 1 \times 10^{-10} =$
 $1 \times 10^{3-10} = 1 \times 10^{-7}$ [meter] **56b.** Longer; all
numbers have the same power of ten; 4 > 1 and 7.5 > 1.
A larger wavelength means a longer wavelength. **57.** x
and y represent two different bases; fewer bases can be
used if two terms have the same base, such as $x^3 \cdot x^5 =$
 x^8 . **58.** $(6.5 \times 10^8)(9 \times 10^{-6}) = (6.5 \cdot 9)(10^{8-6}) =$
 $58.5 \times 10^2 = 5.85 \times 10^3$ [meters] **59.** $(6.12 \times 10^5) \cdot$
 $(12.5 \times 10^8) = 6.125 \times 12.5 \times 10^{13} = 7.65 \times 10^{14}$
60. $(1.98 \times 10^{-3})(2.04 \times 10^{11}) = 4.0392 \times 10^8$
61. $(9.55 \times 10^7)(7.371 \times 10^{-15}) = 7.039305 \times 10^{-7}$
62. $(6.934 \times 10^{-9})(2.579 \times 10^{-4}) = 1.7882786 \times 10^{-12}$
63. $(3.35 \times 10^{25})(2 \times 10^8) = 6.7 \times 10^{33}$ [molecules]
64. $(8.4 \times 10^{11})(1.7 \times 10^{21}) = 14.28 \times 10^{32} \approx 1.4 \times 10^{33}$
[molecules] **65.** $\frac{1}{x^2 \cdot x^{-5}} = \frac{1}{x^{2-5}} = \frac{1}{x^{-3}} = x^3$
66. $\frac{1}{a^3 \cdot a^{-2}} = \frac{1}{a^{3-2}} = \frac{1}{a} \quad \mathbf{67.} \frac{5}{c^1 \cdot c^{-4}} = \frac{5}{c^{1-4}} = \frac{5}{c^{-3}} = 5c^3$
68. $2a^2(3a + 5) = 2 \cdot 3 \cdot a^{2+1} + 2 \cdot 5a^2 = 6a^3 + 10a^2$
69. $8m^3(m^2 + 7) = 8m^{3+2} + 8 \cdot 7m^3 = 8m^5 + 56m^3$
70. $-4x^3(2x^2 - 9x) = -8x^5 + 36x^4$ **71.** $3^x \cdot 3^{2-x} \cdot 3^2 =$
 $3^{x+2-x+2} = 3^4 = 81$ **72.** $2^n \cdot 2^{n+2} \cdot 2 = 2^{n+n+2+1} =$
 2^{2n+3} **73.** $3^x \cdot 2^y \cdot 3^2 \cdot 2^x = 2^{x+y} \cdot 3^{x+2}$ **74.** $(a + b)^2 \cdot$
 $(a + b)^{-3} = (a + b)^{2-3} = (a + b)^{-1} = \frac{1}{a + b}$
75. $(t + 3)^7(t + 3)^{-5} = (t + 3)^{7-5} = (t + 3)^2$
76. $5^{x+1} \cdot 5^{1-x} = 5^{x+1+1-x} = 5^2 = 25$
77a. $(1.3 \times 10^{-3})(1.5 \times 10^{-3})(9.4 \times 10^{-4}) =$
 $1.3 \cdot 1.5 \cdot 9.4 \cdot 10^{-3-3-4} = 18.33 \times 10^{-10} =$
 1.833×10^{-9} [km³] **77b.** $(1.3 \text{ m})(1.5 \text{ m})(0.94 \text{ m}) =$
 1.833 m^3 **78.** $\left(\frac{7.7 \text{ cm}}{1.1 \times 10^{-4} \text{ m}} \right) \left(\frac{1 \text{ m}}{100 \text{ cm}} \right) = 700$; 700 times
79. $(2x^2y^3)(4xy^{-2}) = 8x^{2+1}y^{3-2} = 8x^3y$; the answer is D.
80. Answer is E. **81.** A. $(3.84 \times 10^{-2})(3.84 \times 10^2) =$
 $3.84^2 = 14.7$ B. $\frac{1}{12} \cdot 12 = 1$; the answer is A. **82.** A. slope $= -\frac{1}{3}$ B. $3^5 \cdot 3^2 \cdot 3^{-9} = 3^{-2}$; B is greater, being positive;
the answer is B. **83.** [2] $365 \cdot 4.7 \times 10^7 = 1715.5 \times 10^7 \approx$
 1.7×10^{10} [diapers] [1] no work shown OR answer not
written in scientific notation **84.** [4] a. $A = 4r^2$
b. $4(5)^2 = 100$ [in.²] c. $A = d^2; d = \sqrt{A} = \sqrt{144} =$
12 [in.] [3] radius found in (c) but not the diameter
[2] only two questions answered correctly [1] only one
question answered correctly
85. $1,280,000 = 1.28 \times 10^6$ **86.** $0.0035 = 3.5 \times 10^{-3}$
87. $0.00009 = 9 \times 10^{-5}$ **88.** 6.2 million $= 6.2 \times 10^6$
89. $8.76 \times 10^8 = 876,000,000$ **90.** $1.052 \times 10^{-3} =$
 0.001052 **91.** $9.1 \times 10^{11} = 910,000,000,000$
92. $2.9 \times 10^{-4} = 0.00029$
93.
94.

- 95.
96. $A(3) = 10 + (3 - 1)(4) = 10 + 2 \cdot 4 = 18$; $A(7) = 10 + (7 - 1)(4) = 10 + 6 \cdot 4 = 34$; $A(10) = 10 + (10 - 1)(4) = 10 + 9 \cdot 4 = 46$ 97. $A(3) = -5 + (3 - 1)(2) = -5 + 2 \cdot 2 = -1$; $A(7) = -5 + (7 - 1)(2) = -5 + 6 \cdot 2 = 7$; $A(10) = -5 + 6 \cdot 2 = 7; A(10) = -5 + (10 - 1)(2) = -5 + 9 \cdot 2 = 13$ 98. $A(3) = 12 + (3 - 1)(-4) = 12 + 2 \cdot -4 = 4$; $A(7) = 12 + (7 - 1)(-4) = 12 + 6 \cdot -4 = -12$; $A(10) = 12 + (10 - 1)(-4) = 12 + 9 \cdot -4 = -24$; 99. $A(3) = 1.2 + (3 - 1)(-4) = 1.2 + 2(-4) = -6.8$; $A(7) = 1.2 + (7 - 1)(-4) = 1.2 + 6(-4) = -22.8$; $A(10) = 1.2 + (10 - 1)(-4) = 1.2 + 9(-4) = -34.8$

8-4 More Multiplication Properties of Exponents pages 411–416

Check Skills You'll Need For complete solutions see *Daily Skills Check and Lesson Quiz Transparencies or Presentation Pro CD-ROM*.

$$1. 3^6 \quad 2. 2^{12} \quad 3. 5^{28} \quad 4. 7^3 \quad 5. x^6 \quad 6. a^6 \quad 7. \frac{1}{y^6} \quad 8. \frac{1}{n^6}$$

Investigation 1. $(3^6)^2 = 3^6 \cdot 3^6 = 3^{6+6} = 3^{12}$
 2. $(5^4)^3 = 5^4 \cdot 5^4 \cdot 5^4 = 5^{4+4+4} = 5^{12}$ 3. $(2^7)^4 = 2^7 \cdot 2^7 \cdot 2^7 \cdot 2^7 = 2^{7+7+7+7} = 2^{28}$ 4. $(a^3)^2 = a^3 \cdot a^3 = a^{3+3} = a^{3 \cdot 2} = a^6$ 5. $(g^4)^3 = g^4 \cdot g^4 \cdot g^4 = g^{4+4+4} = g^{4 \cdot 3} = g^{12}$ 6. $(c^3)^4 = c^3 \cdot c^3 \cdot c^3 \cdot c^3 = c^{3+3+3+3} = c^{3 \cdot 4} = c^{12}$ 7a. The power of the result is the product of the powers in the original expression.

$$7b. (8^6)^3 = 8^{6 \cdot 3} = 8^{18}$$

Check Understanding 1. $(a^4)^7 = a^{4 \cdot 7} = a^{28}$; $(a^{-4})^7 = a^{-4 \cdot 7} = a^{-28} = \frac{1}{a^{28}}$ 2a. $(n^4)^3 \cdot n^5 = n^{4 \cdot 3} n^5 = n^{12+5} = n^{17}$ 2b. $t^2(t^7)^{-2} = t^2 \cdot t^{7(-2)} = t^2 \cdot t^{-14} = t^{2-14} = t^{-12} = \frac{1}{t^{12}}$ 2c. $(a^4)^2 \cdot (a^2)^5 = a^{4 \cdot 2} \cdot a^{2 \cdot 5} = a^8 \cdot a^{10} = a^{18}$ 3a. $(2z)^4 = 2^4 \cdot z^4 = 16z^4$ 3b. $(4g^5)^{-2} = 4^{-2} \cdot (g^5)^{-2} = \frac{1}{4^2} \cdot g^{5(-2)} = \frac{1}{16} \cdot g^{-10} = \frac{1}{16g^{10}}$ 3c. $(3t^0)^4 = 3^4 = 81$ 4a. $(c^2)^3(3c^5)^4 = (c^2)^3 \cdot 3^4 \cdot (c^5)^4 = c^6 \cdot 81 \cdot c^{20} = 81c^6c^{20} = 81c^{26}$ 4b. $(2a^3)^5(3ab^2)^3 = 2^5(a^3)^5 \cdot 3^3 \cdot a^3 \cdot (b^2)^3 = 2^5a^{15} \cdot 27a^3 \cdot b^6 = 864a^{18}b^6$ 4c. $(6mn)^3(5m^{-3})^2 = 6^3m^3n^3 \cdot 5^2m^{-6} = 5400m^{-3}n^3 = 5400\frac{n^3}{m^3}$ 5a. $(1.45 \times 10^{-1})(3.6 \times 10^6) = (1.45 \cdot 3.6)(10^{-1} \cdot 10^6) = 5.22 \times 10^5$ [joules]

$$5b. \frac{9 \times 10^{13} \text{ joules}}{5.22 \times 10^5 \text{ joules/hour}} \approx 1.7 \times 10^8 \text{ hours}$$

Exercises 1. $(c^5)^2 = c^{5 \cdot 2} = c^{10}$ 2. $(c^2)^5 = c^{2 \cdot 5} = c^{10}$ 3. $(n^8)^4 = n^{8 \cdot 4} = n^{32}$ 4. $(q^{10})^{10} = q^{10 \cdot 10} = q^{100}$ 5. $(c^5)^3c^4 = c^{5 \cdot 3}c^4 = c^{15}c^4 = c^{19}$ 6. $(d^3)^5(d^3)^0 = d^{3 \cdot 5} \cdot 1 = d^{15}$ 7. $(t^2)^{-2}(t^2)^{-5} = t^{2(-2)}t^{2(-5)} = t^{-4}t^{-10} = t^{-14} = \frac{1}{t^{14}}$ 8. $(x^3)^{-1}(x^2)^5 = x^{3(-1)}x^{2 \cdot 5} = x^{-3}x^{10} = x^7$ 9. $(5y)^4 = 5^4 \cdot y^4 = 625y^4$ 10. $(4m)^5 = 4^5 \cdot m^5 = 1024m^5$ 11. $(7a)^2 = 7^2 \cdot a^2 = 49a^2$ 12. $(12g^4)^{-1} =$

13. $(6y^2)^2 = 6^2 \cdot (y^2)^2 = 36y^4$ 14. $(3n^6)^4 = 3^4n^{6 \cdot 4} = 81n^{24}$ 15. $(2y^4)^{-3} = 2^{-3}y^{4(-3)} = \frac{1}{2^3}y^{-12} = \frac{1}{8y^{12}}$ 16. $(2p^6)^0 = 1$ 17. $(x^2)^5(x^3)^2 = x^{2 \cdot 5}x^{3 \cdot 2} = x^{10}x^6 = x^{16}$ 18. $(2xy)^3x^2 = 2^3x^3y^3x^2 = 8x^5y^3$ 19. $(mg^4)^{-1}(mg^4) = (mg^4)^0 = 1$ 20. $(c^{-2})^3c^{-12} = c^{-2 \cdot 3}c^{-12} = c^{-6}c^{-12} = c^{-18} = \frac{1}{c^{18}}$ 21. $(3b^{-2})^2(a^2b^4)^3 = 3^2b^{-4}a^6b^{12} = 9a^6b^8$ 22. $(2a^2c^4)^{-5}(c^{-1}a^7)^6 = 2^{-5}a^{-10}c^{-20}c^{-6}a^{42} = \frac{1}{32}a^{32}c^{-26} = \frac{a^{32}}{32c^{26}}$ 23. $(4 \times 10^5)^2 = 4^2 \cdot (10^5)^2 = 16 \cdot 10^{5 \cdot 2} = 16 \cdot 10^{10} = 1.6 \times 10^{11}$ 24. $(3 \times 10^5)^2 = 3^2 \cdot 10^{5 \cdot 2} = 9 \times 10^{10}$ 25. $(2 \times 10^{-10})^3 = 2^3 \cdot 10^{-10 \cdot 3} = 8 \times 10^{-30}$ 26. $(2 \times 10^{-3})^3 = 2^3 \cdot 10^{-3 \cdot 3} = 8 \times 10^{-9}$ 27. $(7 \times 10^4)^2 = 7^2 \cdot 10^{4 \cdot 2} = 49 \cdot 10^8 = 4.9 \times 10^9$ 28. $(6 \times 10^{12})^2 = 6^2 \cdot 10^{12 \cdot 2} = 36 \cdot 10^{24} = 3.6 \times 10^{25}$ 29. $(4 \times 10^8)^{-2} = 4^{-2} \cdot 10^{8(-2)} = \frac{1}{16} \cdot 10^{-16} = 0.0625 \cdot 10^{-16} = 6.25 \times 10^{-18}$ 30. $(3.5 \times 10^{-4})^3 = 3.5^3 \cdot 10^{-4 \cdot 3} = 42.875 \cdot 10^{-12} = 4.2875 \times 10^{-11}$ 31. $(9.5 \times 10^{-4})^3 = 9.5^3 \cdot 10^{-4 \cdot 3} = 857.375 \cdot 10^{-12} = 8.57375 \times 10^{-10}$ [m³] 32. $(x^2)^3 = x^6$ 33. $(m^{-4})^3 = m^{-12}$ 34. $(b^2)^4 = b^8$ 35. $(y^{-4})^{-3} = y^{12}$ 36. $(n^9)^0 = 1$ 37. $7(c^1)^8 = 7c^8$ 38. $(5x^{-2})^2 = 25x^{-4}$ 39. $(3x^3y^0)^3 = 27x^9$ 40. $(m^2n^3)^{-3} = \frac{1}{m^6n^9}$ 41. $x^5 + x^5$ is correct; x^{10} equals $x^5 \cdot x^5$. 42. $(4.1)^5 \cdot (4.1)^{-5} = (4.1)^{5+(-5)} = (4.1)^0 = 1$ 43. $3^2(3x)^3 = 9 \cdot 3^3x^3 = 243x^3$ 44. $(b^5)^3b^2 = b^{5 \cdot 3}b^2 = b^{15}b^2 = b^{17}$ 45. $(-5x)^2 + 5x^2 = (-5)^2x^2 + 5x^2 = 25x^2 + 5x^2 = 30x^2$ 46. $(2x^{-3})^2 \cdot (0.2x)^2 = 2^2x^{-6} \cdot 0.2^2x^2 = 4 \cdot 0.04x^{-6+2} = 0.16x^{-4} = \frac{0.16}{x^4}$ 47. $(-2a^2b)^3(ab)^3 = (-2)^3a^6b^3a^3b^3 = -8a^9b^6$ 48. $(3^7)^2 \cdot (3^{-4})^3 = 3^{14} \cdot 3^{-12} = 3^2 = 9$ 49. $(10^3)^4(4.3 \times 10^{-8}) = 10^{12} \cdot 4.3 \times 10^{-8} = 4.3 \times 10^{12-8} = 4.3 \times 10^4$ 50. $(4xy^2)^4(-y)^{-3} = 4^4x^4y^8(-y^3) = -256x^4y^5$ 51a. $6(2x)^2 = 6 \cdot 2^2x^2 = 6 \cdot 4x^2 = 24x^2$; 6(4x)² = $6 \cdot 4^2x^2 = 96x^2$ 51b. $\frac{96x^2}{24x^2} = 4$ [times] 51c. $(2x)^3 = 2^3x^3 = 8x^3$; $(4x)^3 = 4^3x^3 = 64x^3$ 51d. $\frac{64x^3}{8x^3} = 8$ [times] 52. $m^4 \cdot n^4 = (mn)^4$ 53. $(a^5)(b^5)(a^0) = (ab)^5$ 54. $49x^2y^2z^2 = (7xyz)^2$ 55. $\frac{12x^2}{3y^{-2}} = 4x^2y^2 = (2xy)^2$ 56. If $(a^c)^d = a^{c \cdot d} = a^n$, then $cd = n$; n must be factorable in four different ways.
 Example: $n = 24 = 2 \cdot 12 = 3 \cdot 8 = 4 \cdot 6 = 1 \cdot 24$
 57a. $\frac{1 \text{ m}}{1 \text{ cm}} = 100$; $100^3 = (10^2)^3 = 10^6$
 57b. $\frac{1 \text{ m}}{1 \text{ mm}} = 1000$; $1000^3 = (10^3)^3 = 10^9$
 57c. $\frac{1 \text{ km}}{1 \text{ m}} = 1000$; $1000^3 = 10^9$
 57d. $\frac{1 \text{ km}}{1 \text{ mm}} = 10^6$; $(10^6)^3 = 10^{6 \cdot 3} = 10^{18}$
 58a. $2^3 \cdot 2^{20} = 2^{3+20} = 2^{23}$ [bits] 58b. $2^{10} \cdot 2^{20} = 2^{30}$ [bytes]; $2^3 \cdot 2^{30} = 2^{33}$ [bits] 59a. $S = 4\pi r^2 = 4\pi(6.4 \times 10^6)^2 = 4\pi(6.4)^2 \cdot 10^{6 \cdot 2} \approx 514.7 \times 10^{12} \approx 5.15 \times 10^{14}$ [m²] 59b. $0.70 \cdot 5.15 \times 10^{14} \approx 3.6 \times 10^{14}$ [m²]

- 59c. $3795 \cdot 3.6 \times 10^{14} \approx 13,662 \times 10^{14} \approx 1.37 \times 10^{18} [\text{m}^3]$
 60. A. $2^5 \cdot 2 = 32 \cdot 2 = 64$ B. $2^6 = 64$ C. $2^2 \cdot 2^3 = 2^{2+3} = 2^5 = 32$ D. $(2^3)^2 = 2^{3 \cdot 2} = 2^6 = 64$ E. $(2^2)(2^2)^2 = 2^2 \cdot 2^{2 \cdot 2} = 2^2 \cdot 2^4 = 2^6 = 64$; the answer is C.
61. Add exponents for products of powers as in a^2a^4 . Multiply exponents for powers of powers, as in $(a^2)^4$.

62.

$$\begin{aligned} 5^6 &= 25^x \\ 5^6 &= (5^2)^x \\ 5^6 &= 5^{2x} \\ 6 &= 2x \\ 3 &= x \end{aligned}$$

63.

$$\begin{aligned} 8^2 &= 2^x \\ (2^3)^2 &= 2^x \\ 2^6 &= 2^x \\ 6 &= x \end{aligned}$$

64.

$$\begin{aligned} 3^x &= 27^4 \\ 3^x &= (3^3)^4 \\ 3^x &= 3^{12} \\ x &= 12 \end{aligned}$$

65.

$$\begin{aligned} 4^x &= 2^6 \\ (2^2)^x &= 2^6 \\ 2^{2x} &= 2^6 \\ 2x &= 6 \\ x &= 3 \end{aligned}$$

66.

$$\begin{aligned} 3^{2x} &= 9^4 \\ 3^{2x} &= (3^2)^4 \\ 3^{2x} &= 3^8 \\ 2x &= 8 \\ x &= 4 \end{aligned}$$

67.

$$\begin{aligned} 2^x &= \frac{1}{32} \\ 2^x &= \frac{1}{2^5} \\ 2^x &= 2^{-5} \\ x &= -5 \end{aligned}$$

68. $(x^3)^4 = x^{12}$, $x^{34} = x^{81}$; no

69. The area $= \frac{1}{2}$ (base)(height) $= \frac{1}{2}(3x)(3x) = 4.5x^2$; the answer is B.

70. $3(5.1 \times 10^{-5})^2 = 3 \cdot 5.1^2 \cdot 10^{-10} = 78.03 \times 10^{-10} = 7.803 \times 10^{-9}$; the answer is I.

71. $(7^{-2})^3 = 7^{-2 \cdot 3} = 7^{-6} = \frac{1}{7^6} = 0.0000085$; the answer is C.

72. H. $25(n^3)^9 = 25n^{3 \cdot 9} = 25n^{27}$; the answer is H.

73. [2] No, $(x^2 + 3y)^2 \neq x^4 + 9y^2$; for $x = 2$, $y = 4$, $(x^2 + 3y)^2 = (4 + 12)^2 = 16^2 = 256$; $x^4 + 9y^2 = 2^4 + 9(4)^2 = 16 + 9 \cdot 16 = 160$ (OR equivalent explanation) [1] appropriate conclusion but no work to support conclusion

74. $bc^{-6} \cdot b = b b c^{-6} = \frac{b^2}{c^6}$

75. $(a^2b^3)(a^6) = a^2a^6b^3 = a^8b^3$

76. $9m^3(6m^2n^4) = 54m^5n^4$

77. $2t(-2t^4) = -4t^5$

78. $3x + 5 = -4x + 12$

$7x + 5 = 12$

$7x = 7$

$x = 1$

$y = 3 \cdot 1 + 5 = 8$

79. $0.5x - 1 = 0.2x + 0.4$

$5x - 10 = 2x + 4$

$3x - 10 = 4$

$$\begin{aligned} 3x &= 14 \\ x &= \frac{14}{3} = 4\frac{2}{3} \\ y &= 0.5\left(\frac{14}{3}\right) - 1 \\ y &= \frac{7}{3} - 1 = \frac{4}{3} = 1\frac{1}{3} \end{aligned}$$

80.

$$\begin{aligned} 5x - 9 &= 3x + 5 \\ 2x - 9 &= 5 \\ 2x &= 14 \\ x &= 7 \\ y &= 3 \cdot 7 + 5 = 26 \end{aligned}$$

81.

$$\begin{aligned} x + 4 &= -5 \\ x &= -9 \\ y &= -5 \end{aligned}$$

82. Points are (x_1, y_1) , (x_2, y_2) ; slope $= \frac{y_2 - y_1}{x_2 - x_1} = \frac{0 - 3}{4 - 0} = -\frac{3}{4}$

83. slope $= \frac{1 - (-5)}{3 - 2} = 6$

84. $\frac{0 - 6}{1 - (-3)} = \frac{-6}{4} = -\frac{3}{2}$

85. $\frac{-9 - 0}{11 - 0} = -\frac{9}{11}$

CHECKPOINT QUIZ 1

page 416

1. $5^{-1}(3^{-2}) = \frac{1}{5 \cdot 3^2} = \frac{1}{5 \cdot 9} = \frac{1}{45}$
2. $(r^{-5})^{-4} = r^{20}$
3. $(2x^5)(3x^{12}) = 2 \cdot 3x^{5+12} = 6x^{17}$
4. $\frac{mn^{-4}}{p^0q^{-2}} = \frac{mq^2}{n^4}$
5. $a^2b^0(a^{-3}) = a^{2-3} = \frac{1}{a}$
6. $(3^2)^{-1}(4m^2)^3 = 3^{-2} \cdot 4^3m^{2 \cdot 3} = \frac{64m^6}{9}$
7. $(2m^3)(3m^6) = 2 \cdot 3m^{3+6} = 6m^9$
8. $(3t^2)^3(2t^0)^{-3} = 3^3t^{2 \cdot 3}2^{-3} = \frac{27t^6}{8}$
9. $500 \cdot 2^0 = 500$; $500 \cdot 2^2 = 500 \cdot 4 = 2000$; $500 \cdot 2^5 = 500 \cdot 32 = 16,000$
- 10a. $6800 \text{ km} = 6.8 \times 10^3 \text{ km}$
- 10b. radius $= 3.4 \times 10^3 \text{ km}$; $S = 4\pi r^2 = 4\pi(3.4 \times 10^3)^2 = 4\pi(3.4)^2 \cdot 10^{3 \cdot 2} \approx 145 \times 10^6 = 1.45 \times 10^8 [\text{km}^2]$
- 10c. $1.45 \times 10^8 = 145,000,000 [\text{km}^2]$

8-5 Division Properties of Exponents

pages 417–423

Check Skills You'll Need For complete solutions see *Daily Skills Check and Lesson Quiz Transparencies or Presentation Pro CD-ROM*.

1. $\frac{1}{4}$ 2. 5 3. $\frac{3}{5}$ 4. 31 5. $\frac{2}{5}$ 6. $\frac{4}{15}$ 7. $\frac{2}{7}$ 8. $\frac{2}{7}$ 9. $\frac{y}{3}$ 10. $\frac{2y^2}{x}$

11. $\frac{6}{4}$ 12. $\frac{4}{n^2}$

Check Understanding 1a. $\frac{b^4}{b^9} = \frac{1}{b^{9-4}} = \frac{1}{b^5}$

1b. $\frac{z^{10}}{z^5} = z^{10-5} = z^5$

1c. $\frac{a^2b}{a^4b^3} = \frac{1}{a^{4-2}b^{3-1}} = \frac{1}{a^2b^2}$

1d. $\frac{m^{-1}n^2}{m^3n} = \frac{n^{2-1}}{m^{3+1}} = \frac{n}{m^4}$

1e. $\frac{x^2y^{-1}z^4}{xy^4z^{-3}} = \frac{x^{2-1}z^{4+3}}{y^{4+1}} = \frac{xz^7}{y^5}$

2a. $\frac{2 \times 10^3}{8 \times 10^8} = \frac{2}{8} \cdot 10^{3-8} = 0.25 \times 10^{-5} = 2.5 \times 10^{-6}$

2b. $\frac{7.5 \times 10^{12}}{2.5 \times 10^{-4}} = \frac{7.5}{2.5} \cdot 10^{12+4} = 3 \times 10^{16}$

2c. $\frac{4.2 \times 10^5}{12.6 \times 10^2} = \frac{4.2}{12.6} \cdot 10^{5-2} = \frac{1}{3} \times 10^3 = 3.\bar{3} \times 10^2$

2d. $\frac{3.2 \text{ million}}{270.5 \text{ million}} = 0.0118 = 1.18 \times 10^{-2}$ [tons per person]

3a. $\left(\frac{3}{x^2}\right)^2 = \frac{3^2}{(x^2)^2} = \frac{9}{x^4}$

3b. $\left(\frac{x}{y^2}\right)^3 = \frac{x^3}{(y^2)^3} = \frac{x^3}{y^{2 \cdot 3}} = \frac{x^3}{y^6}$

3c. $\left(\frac{t^7}{2^3}\right)^2 = \frac{(t^7)^2}{(2^3)^2} = \frac{t^{7 \cdot 2}}{8^2} = \frac{t^{14}}{64}$

4a. $\left(\frac{3}{4}\right)^{-3} = \frac{4^3}{3^3} = \frac{64}{27}$

65. $\frac{m^7}{n^7} = \left(\frac{m}{n}\right)^7$ 66. $\frac{d^8}{d^5} = d^{8-5} = d^3$ 67. $\frac{10^7 \cdot 10^0}{10^{-3}} =$

$10^{7+3} = 10^{10}$ 68. $\frac{27x^3}{8y^3} = \frac{3^3x^3}{2^3y^3} = \left(\frac{3x}{2y}\right)^3$

69. $\frac{4m^2}{169m^4} = \frac{4}{169m^2} = \frac{2^2}{13^2m^2} = \left(\frac{2}{13m}\right)^2$

70. $\frac{49m^2}{25n^2} = \left(\frac{7m}{5n}\right)^2$ 71. $\frac{125c^7}{216c^4} = \frac{5^3c^3}{6^3} = \left(\frac{5c}{6}\right)^3$

72a. $\frac{2.4 \times 10^{12} \text{ cells}}{2 \times 10^6 \frac{\text{cells}}{\text{second}}} = \frac{2.4}{2} \cdot 10^6 \text{ seconds} =$

$1.2 \times 10^6 \text{ seconds}$ 72b. $(1.2 \times 10^6 \text{ s})\left(\frac{1 \text{ h}}{3600 \text{ s}}\right)\left(\frac{1 \text{ day}}{24 \text{ h}}\right) \approx$

13.9 days 73a,b. Check students' work. 73c. No.

$\frac{x \times 10^n}{2} = \frac{x}{2} \times 10^n$. In scientific notation, the exponent of 10 remains unchanged if $\frac{x}{2} \geq 1$; the exponent of 10 is reduced by 1 if $\frac{x}{2} < 1$. 74. $2^{-3} = \frac{1}{2^3}$; definition of negative exponent 75. $\frac{2^2}{2^5} = \frac{1}{2^3}$; dividing powers with the same base 76. $\left(\frac{1}{2}\right)^3 = \frac{1}{2^3}$; raising a quotient to a power

77. $\frac{1}{2^{-4}2^7} = \frac{1}{2^3}$; multiplying powers with the same base

78. $\frac{(2^4)^3}{2^{15}} = \frac{2^{4 \cdot 3}}{2^{15}} = \frac{2^{12}}{2^{15}} = \frac{1}{2^{15-12}} = \frac{1}{2^3} = \frac{1}{8}$; raising a power to a power; dividing powers with the same base

79. $n^{x+2} \div n^x = \frac{n^{x+2}}{n^x} = n^{x+2-x} = n^2$ 80. $n^{5x} \div n^x = \frac{n^{5x}}{n^x} = n^{5x-x} = n^{4x}$ 81. $\left(\frac{x^m}{x^{m-2}}\right)^2 = [x^{m-(m-2)}]^2 = (x^2)^2 = x^{2 \cdot 2} = x^4$ 82. $\frac{\left(\frac{n^5}{n^4}\right)}{n^3} = \frac{n^{5-4}}{n^3} = \frac{n}{n^3} = \frac{1}{n^{3-1}} = \frac{1}{n^2}$

83a.

Distance From the Sun (kilometers)

Planet	Maximum : Minimum
Mercury	$6.97 \times 10^7 : 4.59 \times 10^7 \approx 1.52$
Venus	$1.089 \times 10^8 : 1.075 \times 10^8 \approx 1.01$
Earth	$1.521 \times 10^8 : 1.471 \times 10^8 \approx 1.03$
Mars	$2.491 \times 10^8 : 2.067 \times 10^8 \approx 1.21$
Jupiter	$8.157 \times 10^8 : 7.409 \times 10^8 \approx 1.10$
Saturn	$1.507 \times 10^9 : 1.347 \times 10^9 \approx 1.12$
Uranus	$3.004 \times 10^9 : 2.735 \times 10^9 \approx 1.10$
Neptune	$4.537 \times 10^9 : 4.457 \times 10^9 \approx 1.02$
Pluto	$7.375 \times 10^9 : 4.425 \times 10^9 \approx 1.67$

83b. A perfectly circular orbit would have a maximum minimum ratio of 1. The greater the ratio, the more elongated (egg-shaped, or elliptical) the orbit. 83c. Pluto has the least circular orbit; Venus's orbit is closest to a circle.

84. $\frac{(-6)^5}{6^5} = \frac{-6^5}{6^5} = -1$; the answer is B.

85. $\frac{-5x^3y^5}{15x^{-7}y^5z^{-2}} = \frac{-x^{10}z^2}{3} = \frac{-(-1)^{10}3^2}{3} = -3$; the answer is G.

86. $2^{-1} = 0.5$; the answer is D. 87. A. $\left(-\frac{7}{5}\right)^{-3} = \left(-\frac{5}{7}\right)^{-3}$ = negative B. Positive; the answer is B.

88. A. $\left(\frac{-1}{2^2}\right)^{-2} = \left(\frac{2^2}{-1}\right)^2 = \text{same as B; the answer is C.}$

89. A. $\left(\frac{2 \cdot 5}{10^2}\right)^2 = \left(\frac{10}{10^2}\right)^2 = \left(\frac{1}{10}\right)^2 = \frac{1}{10^2}$

B. $\left(\frac{2 \cdot 2 \cdot 5}{5^2}\right)^{-2} = \left(\frac{2 \cdot 2 \cdot 5}{5 \cdot 5}\right)^{-2} = \left(\frac{4}{5}\right)^{-2} = \left(\frac{5}{4}\right)^2 = 1.25^2$;

the answer is B. 90. [4] $\frac{7.43 \times 10^8 \text{ miles}}{2.5 \times 10^4 \frac{\text{miles}}{\text{hour}}} =$

$2.972 \times 10^4 \text{ hours} \approx 30,000 \text{ hours};$

$30,000 \text{ hours} \cdot \frac{1 \text{ day}}{24 \text{ hours}} \cdot \frac{1 \text{ year}}{365 \text{ days}} \approx 3.4 \text{ years}$

[3] one computational error [2] missing or incorrect conversion factor [1] no work shown

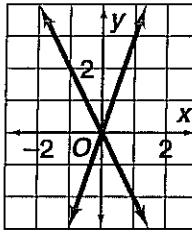
91. $(3y^2)^3 = 3^3(y^2)^3 = 27(y^{2 \cdot 3}) = 27y^6$ 92. $(2m^{-7})^3 =$

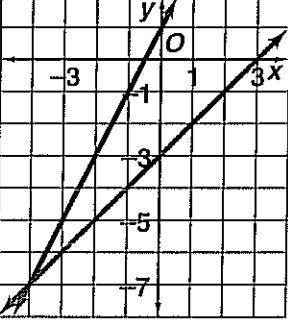
$2^3\left(\frac{1}{m^7}\right)^3 = \frac{8}{m^{7 \cdot 3}} = \frac{8}{m^{21}}$ 93. $(r^2t^{-5})^{-4} = \left(\frac{r^2}{t^5}\right)^{-4} =$

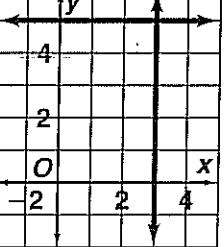
$\left(\frac{t^5}{r^2}\right)^4 = \frac{t^{20}}{r^8}$ 94. $2(3s^{-2})^{-3} = 2\left(\frac{3}{s^2}\right)^{-3} = 2\left(\frac{s^2}{3}\right)^3 = \frac{2s^6}{27}$

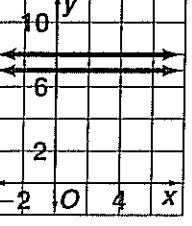
95. $(2^3c^{2-1}) = \frac{1}{2^3c^2} = \frac{1}{8c^2}$ 96. $(-3)^2(-r^3)^2 = 9r^{3 \cdot 2} = 9r^6$

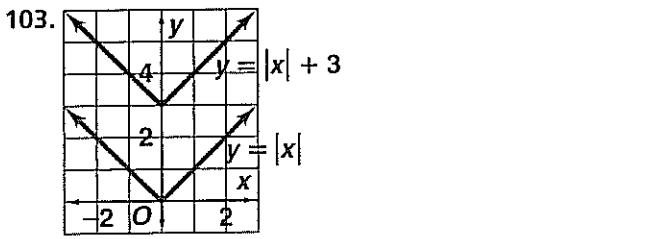
97. $(7^0n^{-3})^2(n^5)^2 = n^{-6}n^{10} = n^4$ 98. $(7^2y^{12})^0 = 1$

99.  (0, 0)

100.  (-4, -7)

101.  (3, 5)

102.  no solution



8.6 Geometric Sequences

pages 424–429

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1. 2. -2 3. -1.2 4. 3.5 5. 32, 64 6. 108, 324 7. 3.2, 6.4
8. 12.5, 6.25

Check Understanding 1a. $\frac{150}{750} = \frac{1}{5}, \frac{6}{30} = \frac{1}{5}$ 1b. $\frac{-6}{-3} = 2; \frac{-24}{-12} = 2$ 1c. $\frac{6}{4} = \frac{3}{2}; \frac{13.5}{9} = \frac{3}{2}$ 2a. common ratio = 3; $3 \cdot 27 = 81; 3 \cdot 81 = 243; 3 \cdot 243 = 729$ 2b. common ratio = -0.5; $-0.5(-15) = 7.5; -0.5 \cdot 7.5 = -3.75; -0.5(-3.75) = 1.875$ 2c. common ratio = 2; $2 \cdot 8.8 = 17.6; 2 \cdot 17.6 = 35.2; 2 \cdot 35.2 = 70.4$ 3a. differences = 2, 2, 2; arithmetic 3b. ratios = 2, 2, 2; geometric 3c. differences = 2, 2, 2; arithmetic 4a. $A(1) = 4 \cdot 3^{1-1} = 4 \cdot 1 = 4; A(6) = 4 \cdot 3^{6-1} = 4 \cdot 3^5 = 972; A(12) = 4 \cdot 3^{12-1} = 4 \cdot 3^{11} = 708,588$ 4b. $A(1) = -2 \cdot 5^{1-1} = -2 \cdot 1 = -2; A(6) = -2 \cdot 5^{6-1} = -2 \cdot 5^5 = -6250; A(12) = -2 \cdot 5^{12-1} = -2 \cdot 5^{11} = -97,656,250$ 5. $A(n) = 200 \cdot (0.56)^{n-1}; A(3) = 200 \cdot 0.56^{4-1} = 200 \cdot 0.56^3 \approx 35.1$ [cm]

Exercises 1. $\frac{8}{2} = 4$ 2. $\frac{-12}{-3} = 4$ 3. 0.1 4. 2.5 5. -0.25
6. 2 7. 40, 80, 160 8. 48, 96, 192 9. 20.25, 30.375, 45.5625
10. -0.5, 0.25, -0.125 11. 0.36, 0.072, 0.0144 12. -48, 96, -192 13. geometric; common ratio = 7
14. arithmetic; common difference = -4 15. geometric; common ratio = $-\frac{4}{3}$ 16. arithmetic; common difference = -5 17. arithmetic; common difference = 0.7
18. geometric; common ratio = $\frac{4}{3}$ 19. $A(1) = 5 \cdot 3^{1-1} = 5 \cdot 3^0 = 5 \cdot 1 = 5; A(4) = 5 \cdot 3^{4-1} = 5 \cdot 3^3 = 5 \cdot 27 = 135; A(8) = 5 \cdot 3^{8-1} = 5 \cdot 3^7 = 5 \cdot 2187 = 10,935$
20. $A(1) = -5 \cdot 3^{1-1} = -5 \cdot 3^0 = -5 \cdot 1 = -5; A(4) = -5 \cdot 3^{4-1} = -5 \cdot 3^3 = -5 \cdot 27 = -135; A(8) = -5 \cdot 3^{8-1} = -5 \cdot 3^7 = -5 \cdot 2187 = -10,935$
21. $A(1) = 5 \cdot (-3)^{1-1} = 5 \cdot (-3)^0 = 5; A(4) = 5 \cdot (-3)^{4-1} = 5 \cdot (-3)^3 = 5(-27) = -135; A(8) = 5 \cdot (-3)^{8-1} = 5 \cdot (-3)^7 = 5(-2187) = -10,935$
22. $A(1) = 0.5 \cdot 3^{1-1} = 0.5 \cdot 3^0 = 0.5; A(4) = 0.5 \cdot 3^{4-1} = 0.5 \cdot 3^3 = 0.5 \cdot 27 = 13.5; A(8) = 0.5 \cdot 3^{8-1} = 0.5 \cdot 3^7 = 0.5 \cdot 2187 = 1093.5$ 23. $A(1) = -2 \cdot 5^{1-1} = -2 \cdot 5^0 = -2 \cdot 1 = -2; A(4) = -2 \cdot 5^{4-1} = -2 \cdot 5^3 = -2 \cdot 125 = -250; A(8) = -2 \cdot 5^{8-1} = -2 \cdot 5^7 = -2 \cdot 78,125 = -156,250$ 24. $A(1) = -1.1 \cdot (-4)^{1-1} = -1.1 \cdot (-4)^0 = -1.1; A(4) = -1.1 \cdot (-4)^{4-1} = -1.1 \cdot (-4)^3 = -1.1(-64) = 70.4; A(8) =$

-1.1 · (-4)⁸⁻¹ = -1.1(-16,384) = 18,022.4 25. $A(n) = 6 \cdot 0.5^{n-1}; A(5) = 6 \cdot 0.5^{5-1} = 6 \cdot 0.5^4 = 0.375$
26. $A(n) = -6 \cdot 2^{n-1}; A(10) = -6 \cdot 2^{10-1} = -6 \cdot 2^9 = -3072$ 27. $A(n) = 7 \cdot 1.1^{n-1}; A(4) = 7 \cdot 1.1^{4-1} = 7 \cdot 1.1^3 = 9.317$ 28. $A(n) = 1 \cdot (-4)^{n-1}; A(7) = (-4)^{7-1} = (-4)^6 = 4096$ 29a. $A(n) = 100 \cdot (0.64)^{n-1}$
29b. $A(6) = 100 \cdot 0.64^{6-1} = 100 \cdot 0.64^5 \approx 10.74$; about 10.74 cm 30. $\frac{8}{3}, \frac{8}{9}, \frac{8}{27}; A(n) = 216 \cdot \left(\frac{1}{3}\right)^{n-1}$

31. 1, 0.2, 0.04; $A(n) = 625 \cdot (0.2)^{n-1}$ 32. 656,1,5904.9, 53,144.1; $A(n) = 0.1 \cdot 9^{n-1}$ 33. 1, -0.5, 0.25; $A(n) = 16 \cdot (-0.5)^{n-1}$ 34. Check students' work. 35. If all consecutive terms have a common difference, the sequence is arithmetic. If all consecutive terms have a common ratio, the sequence is geometric.

36a.

Number of Folds	Number of Rectangles
0	1
1	2
2	4
3	8
4	16
5	32

36b. $A(n) = 2 \cdot 2^{n-1} = 1 \cdot 2^n$
36c. $A(10) = 2^{10} = 1024$; 1024 rectangles
37. arithmetic; 3, 1, -1
38. neither; -3, -8, -14 39. geometric; 1.125, 0.5625, 0.28125
40. arithmetic; 20, 22, 24 41a. $A(n) = 36 \cdot (0.9)^{n-1}$

41b. 6; $n = 1$ corresponds to the first swing, because $A(1) = 36$. 41c. $A(6) = 36 \cdot (0.9)^{6-1} = 36 \cdot (0.9)^5 \approx 21.3$ [cm] 42a. $\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}$ 42b. $2^{-1}, 2^{-2}, 2^{-3}, 2^{-4}$
42c. $r = 2^{-n}$ 42d. 2^{-10} or $\frac{1}{2^{10}}$ 43. No; if one term were 0, then all terms would be 0. Terms are $A(n) = a \cdot r^{n-1}$; we can have $A = 0$ only if a or $r = 0$; then all A 's = 0.
44a. $1, \frac{3}{4}, \frac{9}{16}, \frac{27}{64}$ 44b. $r(n) = 1 \cdot \left(\frac{3}{4}\right)^{n-1}$ 44c. $r(6) = \left(\frac{3}{4}\right)^{6-1} = \left(\frac{3}{4}\right)^5 = \frac{3^5}{4^5} = \frac{243}{1024}$ 44d. $0, \frac{1}{4}, \frac{7}{16}, \frac{37}{64}$
44e. $r_{\text{not shaded}} = 1 - r_{\text{shaded}} = 1 - 1 \cdot \left(\frac{3}{4}\right)^{n-1}$
44f. $r_{\text{not shaded}} = 1 - \left(\frac{3}{4}\right)^{8-1} = 1 - \left(\frac{3}{4}\right)^7 = 1 - \frac{3^7}{4^7} = 1 - \frac{2187}{16,384} = \frac{14,197}{16,384}$ 45. $x; x^5, x^6, x^7$ 46. $3x; 27x^4, 81x^5, 243x^6$ 47. $xy^2; x^5y^9, x^6y^{11}, x^7y^{13}$
48. $ab; 2a^4b^2, 2a^5b^3, 2a^6b^4$ 49. 0.06; $2.592 \times 10^2, 1.5552 \times 10^4, 9.3312 \times 10^{-1}$
50. $A(n) = 2 \cdot 4^{n-1} = 512$
 $4^{n-1} = 256$
 $4^{n-1} = 4^4$
 $n - 1 = 4$
 $n = 5$

The fifth term is 512.

51. The answer is D. 52. Number of cans in each tier = 1, 4, 9, 16, 25, 36; total number of cans in display = 1, 5, 14, 30, 55, 91; the answer is H. 53. The answer is B. 54. [2] $A(n) = 350 \cdot 2^{n-1}; A(1) = 350 \checkmark; A(5) = 350 \cdot 2^{5-1} = 350 \cdot 2^4 = 5600$; 5600 bacteria
[1] no work shown

55. $\left(\frac{a^2}{a^3}\right)^{-4} = \left(\frac{1}{a}\right)^{-4} = a^4$

56. $\left(\frac{1}{2}\right)^{-4} = 2^4 = 16$

57. $\left(\frac{x^2 z}{z^{-3}}\right)^{-5} = (x^2 z^4)^{-5} = \left(\frac{1}{x^2 z^4}\right)^5 = \frac{1}{x^{10} z^{20}}$

58. $\left(\frac{m^{-3}}{n^4}\right)^0 = 1$

59. $\left(\frac{8}{9}\right)^{-2} = \left(\frac{9}{8}\right)^2 = \frac{81}{64}$

60. $\left(\frac{m^4}{m^2}\right)^{-7} = (m^2)^{-7} = \left(\frac{1}{m^2}\right)^7 = \frac{1}{m^{14}}$

61. $\left(\frac{pq^0}{p^4}\right)^5 = \left(\frac{1}{p^3}\right)^5 = \frac{1}{p^{15}}$

62. $\left(\frac{c^2 d^{-2}}{d^3}\right)^{-1} = \left(\frac{c^2}{d^5}\right)^{-1} = \frac{d^5}{c^2}$

63. $0.002467 = 2.467 \times 10^{-3}$

64. $1 \times 10^6 \text{ acre-ft} \cdot 3.26 \times 10^5 \frac{\text{gal}}{\text{acre-ft}} = 3.26 \times 10^{11} \text{ gal}$

65. $y = \frac{8}{3}x$

66. $y = -\frac{2}{5}x = -\frac{2}{5}x$

67. $y = -\frac{7}{6}x = -\frac{7}{6}x$

68. $y = -\frac{5}{3}x = \frac{5}{3}x$

69. $y = \frac{7}{4}x$

70. $y = -\frac{4}{16}x = -\frac{1}{4}x$

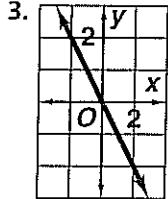
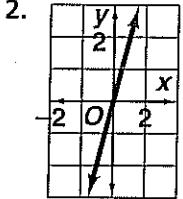
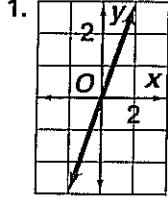
71. $y = \frac{5}{9}x$

72. $y = -\frac{2}{4}x = -\frac{1}{2}x$

8.7 Exponential Functions

pages 430–436

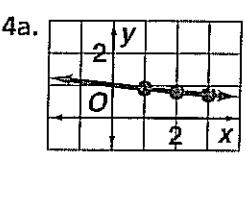
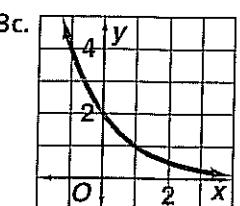
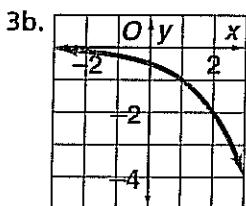
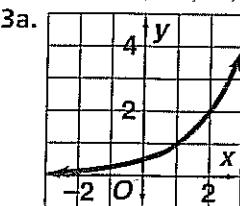
Check Skills You'll Need For complete solutions see *Daily Skills Check and Lesson Quiz Transparencies or Presentation Pro CD-ROM*.



4. 9 5. $\frac{1}{125}$ 6. 162 7. $\frac{2}{9}$ 8. $\frac{3}{2}$ 9. 90

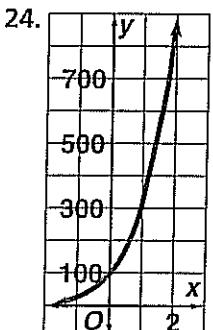
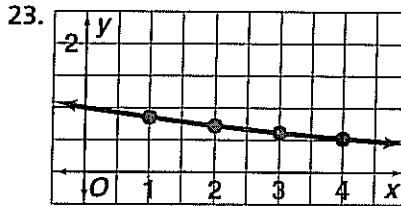
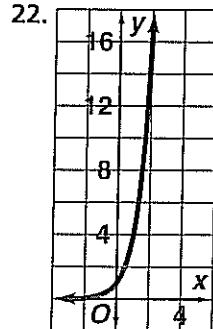
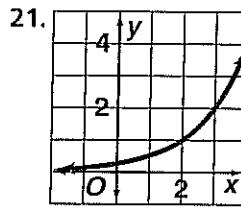
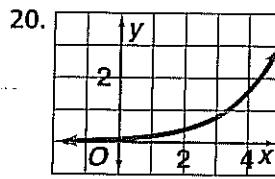
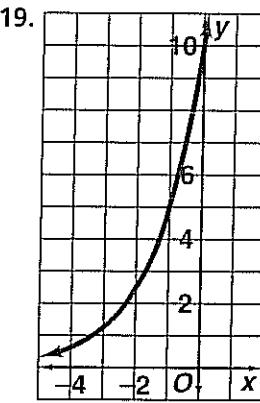
Check Understanding 1a. $y(x) = 4^x$; $y(-2) = 4^{-2} = \frac{1}{4^2} = \frac{1}{16}$; $y(0) = 4^0 = 1$; $y(3) = 4^3 = 64$

1b. $f(-2) = 10 \cdot 5^{-2} = \frac{10}{5^2} = \frac{2}{5}$; $f(0) = 10 \cdot 5^0 = 10$; $f(3) = 10 \cdot 5^3 = 1250$ 1c. $g(-2) = -2 \cdot 3^{-2} = \frac{-2}{3^2} = -\frac{2}{9}$; $g(0) = -2 \cdot 3^0 = -2$; $g(3) = -2 \cdot 3^3 = -54$ 2. $f(6) = 10 \cdot 4^6 = 40,960$; 40,960 animals



4b. Since $f(0) = (1.5)^0 = 1$, this represents copies being made at the same size as the original, or at 100%.

- Exercises** 1. $f(x) = 6^x$; $f(3) = 6^3 = 216$ 2. $g(-2) = 2 \cdot 3^{-2} = \frac{2}{3^2} = \frac{2}{9}$ 3. $20 \cdot (0.5)^3 = 2.5$ 4. $0.5 \cdot 4^3 = 32$ 5. $50 \cdot (0.3)^2 = 4.5$ 6. $1.8 \cdot 2^6 = 115.2$ 7. $100 \cdot \left(\frac{1}{2}\right)^{-4} = 100 \cdot 2^4 = 1600$ 8. $9 \cdot \left(\frac{5}{2}\right)^{-3} = 9 \cdot \left(\frac{2}{5}\right)^3 = 0.576$ 9. $f(x) = 10,000 \cdot 2^{\frac{x}{13}}$; $f(52) = 10,000 \cdot 2^{\frac{52}{13}} = 10,000 \cdot 2^4 = 160,000$ [\\$]; $f(65) = 10,000 \cdot 2^{\frac{65}{13}} = 10,000 \cdot 2^5 = 320,000$ [\\$] 10. $f(x) = 500 \cdot 2^{\frac{x}{15}}$; $f(30) = 500 \cdot 2^{\frac{30}{15}} = 500 \cdot 2^2 = 2000$ [\\$]; $f(45) = 500 \cdot 2^{\frac{45}{15}} = 500 \cdot 2^3 = 4000$ [\\$] 11. $f(x) = 2000 \cdot 2^{\frac{x}{8}}$; $f(24) = 2000 \cdot 2^{\frac{24}{8}} = 2000 \cdot 2^3 = 16,000$ [\\$]; $f(32) = 2000 \cdot 2^{\frac{32}{8}} = 2000 \cdot 2^4 = 32,000$ [\\$] 12. A 13. C 14. B 15. B 16. D 17. C 18. A



25. $f(-2) = 5^{-2} = \frac{1}{5^2} = \frac{1}{25} = 0.04$,
 $5^{-1} = 0.2$, $5 \cdot 0.2 = 1$; 5, 25, 125;
increase 26. $2.5^{-2} = \frac{1}{2.5^2} = \frac{1}{6.25} = 0.16$, $2.5 \cdot 0.16 = 0.4$; 1, 2.5, 6.25, 15.625; increase 27. $0.1^{-2} = \frac{1}{0.1^2} = 100$, $0.1 \cdot 100 = 10$; 1, 0.1, 0.01, 0.001; decrease 28. $5 \cdot 4^{-2} = \frac{5}{4^2} = 0.3125$, $5 \cdot 4^{-1} = 1.25$, $4 \cdot 1.25 = 5$; 20, 80, 320; increase 29. $0.5^{-2} = 2^2 = 4$, $0.5 \cdot 4 = 2$, 1, 0.5, 0.25, 0.125; decrease

30. $\left(\frac{2}{3}\right)^{-2} = \left(\frac{3}{2}\right)^2 = \frac{9}{4}, \frac{2}{3} \cdot \frac{9}{4} = \frac{3}{2}, \frac{2}{3} \cdot \frac{3}{2} = 1; \frac{2}{3}, \frac{4}{9}, \frac{8}{27}$; decrease 31. $4 \cdot 10^{-2} = 0.04$, $10 \cdot 0.04 = 0.4$; 4, 40, 400, 4000; increase 32. $100 \cdot 0.3^{-2} = 100 \cdot \frac{1}{0.3^2} = 100 \cdot \frac{1}{0.09} = 1111.\bar{1}$, $100 \cdot 0.3^{-1} = 333.\bar{3}$; 100, 30, 9, 2.7; decrease

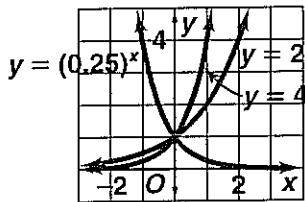
33a. Any function $y = a \cdot b^x$, where $a > 0$ and $b > 1$ or $a < 0$ and $0 < b < 1$. **33b.** Any function $y = a \cdot b^x$, where $a > 0$ and $0 < b < 1$ or $a < 0$ and $b > 1$.

34a.

Time	Number of 20-min Time Periods	Pattern	Number of Bacteria Cells
Initial	0	75	75
20 min	1	$75 \cdot 2$	$75 \cdot 2^1 = 150$
40 min	2	$75 \cdot 2 \cdot 2$	$75 \cdot 2^2 = 300$
60 min	3	$75 \cdot 2 \cdot 2 \cdot 2$	$75 \cdot 2^3 = 600$
80 min	4	$75 \cdot 2 \cdot 2 \cdot 2 \cdot 2$	$75 \cdot 2^4 = 1200$
100 min	5	$75 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2$	$75 \cdot 2^5 = 2400$
120 min	6	$75 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2$	$75 \cdot 2^6 = 4800$
140 min	7	$75 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2$	$75 \cdot 2^7 = 9600$

34b. $y = 75 \cdot 2^x$, where x = number of 20-minute time periods; or $y = 75 \cdot 2^{\frac{x}{20}}$, where t = time in minutes.

35a.



35b. $(0, 1)$ **35c.** No, there is no value of x where $y = 0$.

35d. $y = a \cdot b^x$; if $b > 1$, the graph gets steeper as b increases. If $b < 1$, the graph gets steeper as b decreases.

36a. $y = 1 \cdot 1000^{\frac{150}{50}} = 1000^3 = 10^9$ plants

36b. $1000^{\frac{200}{50}} = 1000^4 = 10^{12}$ plants

37a.

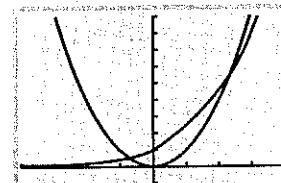
x	y
1	-2
2	4
3	-8
4	16
5	-32

37b. Every other value is negative. The absolute value of each term is double the previous term. **37c.** No; in $y = a \cdot b^x$, an exponential function requires $b > 0$. In this case $b = -2 < 0$, so $y = (-2)^x$ is not exponential.

38. $5^3 = 125$; $3^5 = 243$; $y = x^5$ is greater. **39.** $10 \cdot 2^7 = 1280$; $200 \cdot 7^2 = 9800$; $f(t) = 200 \cdot t^2$ is greater. **40.** $3^4 = 81$; $4^3 = 64$; $y = 3^x$ is greater. **41.** $2^{10} = 1024$; $100 \cdot 10^2 = 10,000$; $f(x) = 100x^2$ is greater. **42.** $f(x) = 500 \cdot 1^x = 500$ for $x = 1, 2, 3, 4$, and 5. Range = [500].

The definition of an exponential function excludes the case $b = 1$ because in that case $f(x)$ is a constant, and does not show exponential behavior.

43a.



Xmin=-4 Ymin=-1
Xmax=4 Ymax=9

44. $3^x = 9$

$3^x = 3^2$

$x = 2$

45.

$$3^x = \frac{1}{27}$$

$$3^x = \frac{1}{3^3} = 3^{-3}$$

$x = -3$

46. $2^x = 64$

$2^x = 2^6$

$x = 6$

47.

$$3 \cdot 2^x = 24$$

$$2^x = 8$$

$$2^x = 2^3$$

$x = 3$

48. $2 \cdot 3^x = 162$

$3^x = 81$

$3^x = 3^4$

$x = 4$

49. $5 \cdot 2^x - 152 = 8$

$5 \cdot 2^x = 160$

$2^x = 32$

$2^x = 2^5$

$x = 5$

50a. $y = a \cdot b^x$

$4 = a \cdot b^0$

$4 = a$

50b.

$$36 = 4 \cdot b^2$$

$$9 = b^2$$

$$3^2 = b^2$$

$$3 = b$$

50c. $y = 4 \cdot 3^x$ **50d.** $4 \cdot 3^{-2} = \frac{4}{9}$; $4 \cdot 3^4 = 324$

51. $y = -3^{-2} = -\frac{1}{3^2} = -\frac{1}{9}$; the answer is B.

52. F. $1.675 \cdot 1 + 1.325 = 3 \checkmark$; H. $1.675 \cdot 3 + 1.325 = 6.75 \checkmark$ I. $1.675 \cdot 1 + 1.675 = 3 \checkmark$; J. $1.325 \cdot 3 + 1.675 = 5.65$ no; the answer is G. **53.** When $x = 0$, $y = 2^0 = 1$; the answer is A. **54.** The answer is H. **55.** [2]

x	$y = 20 \cdot 0.5^x$	$y = 0.5 \cdot 4^x$
0	20	0.5
1	10	2
2	5	8

The graphs intersect between $x = 1$ and $x = 2$.

[1] no work shown

56. 5; 1250, 6250, 31,250 **57.** -3; 567, -1701, 5103

58. 2; -3.2, -6.4, -12.8 **59.** $-\frac{1}{3}, \frac{1}{3}, -\frac{1}{9}, \frac{1}{27}$ **60.** 0.1; 0.045, 0.0045, 0.00045

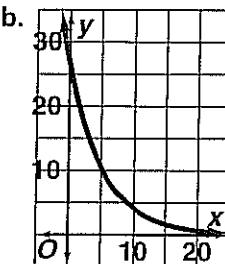
61. 0.25; 28, 7, 1.75 **62.** Point = (x_1, y_1) ; equation is $y - y_1 = m(x - x_1)$; $m = -5$; $y - 0 = 5(x - 0)$ or $y = 5x$ **63.** $y - 1 = 3(x - 0)$ or $y = 3x + 1$ **64.** $y - 0 = -2(x - 4)$ or $y = -2x + 8$

65. $y - (-3) = 0.4(x - 2)$ or $y = 0.4x - 3.8$

1. $\left(\frac{3^2}{3^{-1}}\right)^4 = (3^3)^4 = 3^{3 \cdot 4} = 3^{12}$ 2. $\left(\frac{x^2}{y^3}\right)^{-5} = \left(\frac{y^3}{x^2}\right)^5 = \frac{y^{3 \cdot 5}}{x^{2 \cdot 5}} = \frac{y^{15}}{x^{10}}$ 3. $\left(\frac{10m^{-3}}{25n^{-6}}\right)^2 = \left(\frac{2n^6}{5m^3}\right)^2 = \frac{(2n^6)^2}{(5m^3)^2} = \frac{4n^{12}}{25m^6}$
4. $\left(\frac{6^2t^{-3}}{6^2r^0t^2}\right)^2 = \left(\frac{1}{t^5}\right)^2 = \frac{1}{t^{10}}$ 5. common ratio = 2; geometric 6. common ratio = $\frac{1}{2}$; geometric 7. common difference = 5; arithmetic 8a. -100 8b. $-\frac{1}{5}$ or -0.2 8c. $A(n) = -100(-0.2)^{n-1}$ 8d. $A(5) = -100(-0.2)^{5-1} = -100(-0.2)^4 = -100 \cdot 0.0016 = -0.16$; $A(7) = -100(-0.2)^{7-1} = -100(-0.2)^6 = -100 \cdot 0.000064 = -0.0064$ 9a. The length of the n th swing is $A(n) = 40(0.85)^{n-1}$ 9b. $A(5) = 40(0.85)^{5-1} = 40(0.85)^4 \approx 209$; 209 mm 10a. 108 million = $108 \times 10^6 = 1.08 \times 10^8$ 10b. 249 million = 2.49×10^8 10c. $\frac{\$2.49 \times 10^8}{1.08 \times 10^8 \text{ vehicles}} \approx \2.31 per vehicle

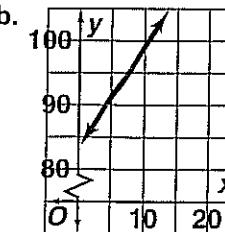
TECHNOLOGY

1a. $y = 26.87(0.83)^x$



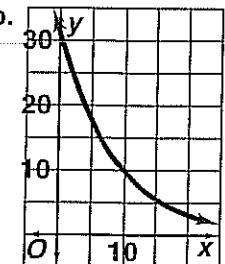
1c. $y(20) = 26.87(0.83)^{20} \approx 0.65$

2a. $y = 83.59(1.02)^x$



2c. $y(20) = 83.59(1.017)^{20} \approx 117.1$

3a. $y = 31.53(0.89)^x$



3c. $y(60) = 31.53(0.89)^{60} \approx 0.029$

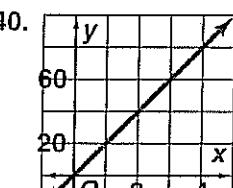
8.8 Exponential Growth and Decay

Check Skills You'll Need For complete solutions see *Daily Skills Check and Lesson Quiz Transparencies* or *Presentation Pro CD-ROM*.

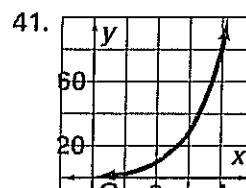
1. \$100 2. \$64.80 3. \$225 4. \$352.80 5. \$324

- Check Understanding** 1a. $y = 4512 \cdot 1.025^x$ 1b. $y = 4512 \cdot 1.025^3 \approx 4859$ [students] 2a. $y = 1500 \cdot 1.08^{18} = 5994.03$ [\$] 2b. $B = 1500(1 + 0.08)^{18} = 5994.03$ [\$] 2c. $(1 + r)$ is the same as 100% + 100r% written as a decimal. 3a. interest rate per month = $\frac{6.5\%}{12} = 0.54167\%$; number of months = $18 \cdot 12 = 216$; $y = 1500 \cdot 1.0054167^{216} = 4817.75$ [\$] 3b. interest rate per month = $\frac{5}{12} = 0.41667\%$; after $x = 12$ months $y = 200 \cdot 1.0041667^{12} = 210.23$ [\$]; after $x = 24$ months $y = 200 \cdot 1.0041667^{24} = 220.99$ [\$]; after $x = 60$ months $y = 200 \cdot 1.0041667^{60} = 256.67$ [\$] 4a. $\frac{32}{8} = 4$ [half-lives] 4b. $(50 \text{ mCi}) \cdot \frac{1}{2} = 25 \text{ mCi}; (50 \text{ mCi}) \cdot \frac{1}{2} \cdot \frac{1}{2} = 12.5 \text{ mCi}$ 4c. $(30 \text{ mCi}) \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = 3.75 \text{ mCi}$ 5a. 604,000 5b. decay factor = $100\% - 1.8\% = 1 - 0.018 = 0.982$ 5c. $y = 604,000(0.982)^x$ 5d. $y = 604,000(0.982)^{20} \approx 420,017$; about 420,017 people

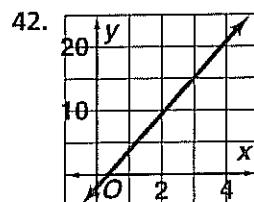
- Exercises** 1. initial amount = $a = 20$; growth factor = $b = 2$ 2. $a = 200$; $b = 1.0875$ 3. 10,000; 1.01 4. 1; 1.5 5a. $a = 50,000$ 5b. $b = 100\% + 3\% = 1 + 0.03 = 1.03$ 5c. 1.03 5d. $y = 50,000 \cdot 1.03^x$ 5e. $y = 50,000 \cdot 1.03^{25} \approx 104,689$ [people] 6. 100% + 4% = $1 + 0.04 = 1.04$ 7. $1 + 0.05 = 1.05$ 8. $1 + 0.037 = 1.037$ 9. $1 + 0.0875 = 1.0875$ 10. $1 + 0.005 = 1.005$ 11. $\frac{3\%}{4} = 0.75\%; \frac{3\%}{12} = 0.25\%$ 12. $\frac{4\%}{4} = 1\%; \frac{4\%}{12} = \frac{1}{3}\%$ 13. $\frac{4.5\%}{4} = 1.125\%$; $\frac{4.5\%}{12} = 0.375\%$ 14. $\frac{7.6\%}{4} = 1.9\%; \frac{7.6\%}{12} = 0.63\%$ 15. $\frac{6.25\%}{4} = 1.5625\%; \frac{6.25}{12} = 0.52083\%$ 16. $4000 \cdot 1.06^5 = 5352.90$ [\$] 17. $12,000 \cdot 1.048^7 = 16,661.35$ [\$] 18. rate = 1% per quarter; period = 24 quarters; $500 \cdot 1.01^{24} = 634.87$ [\$] 19. rate = $\frac{3.5\%}{4} = 0.875\%$ per quarter; period = 40 quarters; $20,000 \cdot 1.00875^{40} = 28,338.18$ [\$] 20a. $\frac{16 \text{ days}}{4 \text{ days}} = 4$ [half-lives] 20b. $(40 \text{ mCi}) \left(\frac{1}{2}\right)^4 = 2.5 \text{ mCi}$ 21a. $\frac{60 \text{ min}}{30 \text{ min}} = 3$ [half-lives] 21b. $(25 \text{ mCi}) \left(\frac{1}{2}\right)^3 = 3.125 \text{ mCi}$ 22. 0.5 23. 0.1 24. $\frac{2}{3}$ 25. 0.9 26. $2 > 1$; growth 27. $0.68 < 1$; decay 28. $2 > 1$; growth 29. $0.2 < 1$; decay 30a. \$22,000; $1 - 20\% = 0.8$ 30b. $y = 22,000 \cdot (0.8)^x$ 30c. $22,000 \cdot 0.8^6 \approx 5767.17$ 31. $y = 130,000(1.01)^x$; $x = 9$; $y \approx 142,179$ 32. $y = 3,000,000(0.985)^x$; $x = 10$; $y \approx 2,579,191$ 33. $y = 2400(1.07)^x$; $x = 10$; $y = 4721.16$ [\$] 34. $\frac{7\%}{12} = 0.583\%$; $y = 2400(1.00583)^x$; $x = 120$; $y = 4823.19$ [\$] 35a. $y = 584(1.065)^x$; $x = 20$; $y \approx 2058$ [\$] 35b. Check students' work. 36. Linear; it is a straight line. 37. Neither; it is not a single straight line. 38. Curve resembles an exponential function; $y(x)$ increases with an ever-increasing slope. 39. Neither; y decreases and then increases.



linear function



exponential function



linear function **45.** $\frac{300 \text{ years}}{75 \text{ years}} = 4$ half-lives

46a. about 4 h **46b.** $\frac{1}{2} \cdot \frac{1}{2} = \frac{1}{4}$ **46c.** by estimate, $\frac{15 \text{ mg}}{4} =$

3.75 mg; by function, $(15 \text{ mg})0.84^8 \approx 3.72 \text{ mg}$

47a. $y = 6,284,000(1.01)^x$ **47b.** $y = 6,284,000(1.01)^{20} \approx 7,667,674$ **48.** $1 - 6\% = 94\%$ **49.** $1 - 12\% = 88\%$

50. $1 - 3.5\% = 96.5\%$ **51.** $1 - 53.9\% = 46.1\%$

52a. Initial level = 500 mCi; level drops to half of this (250 mCi) after 2 years. **52b.** $\frac{200 \text{ mCi}}{800 \text{ mCi}} = \frac{1}{4} = \frac{1}{2} \cdot \frac{1}{2}$; two half-lives = 4 years **53a.** $250 - 30 = 220$ [All amounts are in dollars.] **53b.** $220 \cdot 0.018 = 3.96$ **53c.** $220 + 3.96 = 223.96$ **53d.** $223.96 - 30 = 193.96$ **53e.** Repeating this calculation, find account paid off after 9 months. **53f.** Interest payments add up to \$18.07. **54.** approximate rule: $x = \frac{72}{r}$; exact: $y = (1 + r)^x$

Rate r (%)	Years to double, x (rule of 72)	Exact increase, y
1	72	2.047
2	36	2.040
3	24	2.033
4	18	2.026
6	12	2.012
8	9	1.999
9	8	1.992
12	6	1.974
18	4	1.939
24	3	1.907
36	2	1.850

The rule of 72 becomes inaccurate only for extremely high interest rates.

55.

End of Year	x	$40,000(1.07)^x$	$60,000(0.96)^x$
2000	1	42,800	57,600
2001	2	45,796	55,296
2002	3	49,002	53,084
2003	4	52,432	50,961

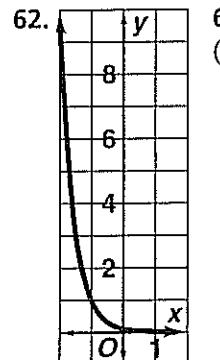
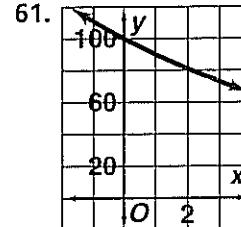
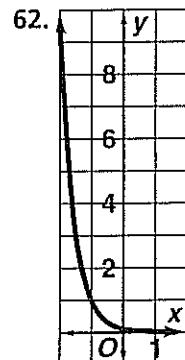
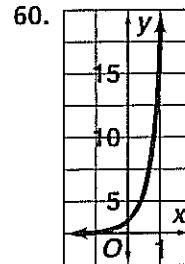
Chessville's population exceeds Checkersville's during 2003.

56. Only C has a base < 1; the answer is C.

57. $1000 \cdot 1.03^{10} = 1343.92$; the answer is H.

58. $24 \cdot 1.045^{374} = 339,000,000$; the answer is A.

59. [2] $1.0125^{20} = 1.282$; $1.055^5 = 1.307$; account paying 5.5% will be larger. [1] minor computational error



63. $(1.4 \times 10^4)(5.2 \times 10^7) = (1.4 \cdot 5.2)(10^{4+7}) = 7.28 \times 10^{11} [\text{gal}]$

READING MATH

page 445

- a. about 9 or 10 words b. $40 \cdot 0.75^5 \approx 9.49$; 9 or 10 words

TEST-TAKING STRATEGIES

page 446

- Test terms $x - 2$, x , and $x + 3$. A. 2, 4, 7, no B. 4, 6, 9 ✓
- C. 6, 8, 11, no D. 8, 10, 13, no. The answer is B.
- E. $\frac{1}{2} + \frac{1}{(-2)^2} = -\frac{1}{4}$, no G. $\frac{1}{-1} + \frac{1}{(-1)^2} = 0$ ✓
- H. $1 + 1 = 2$, no I. $\frac{3}{4}$; the answer is G. 3. A. $(0.00011)^2 = 1.21 \times 10^{-8}$, no B. $(0.0011)^2 = 1.21 \times 10^{-6}$, no C. $(0.011)^2 = 1.21 \times 10^{-4}$ ✓ D. $(0.11)^2 = 1.21 \times 10^{-2}$, no; the answer is C. 4. Test terms x , $3x + 1$, and $6x - 1$. F. $-3, -8, -19$, no G. $-1, -2, -7$, no H. 1, 4, 17, no I. 3, 10, 17 ✓; the answer is I.

CHAPTER REVIEW

pages 447–449

- exponential growth 2. growth factor 3. scientific notation 4. exponential decay 5. decay factor 6. compound interest 7. common ratio 8. interest period, at the end of which the interest is compounded 9. geometrical sequence

10. exponential function 11. $b^{-4}c^0d^6 = \frac{d^6}{b^4}$ 12. $\frac{x^{-2}}{y^{-8}} = \frac{y^8}{x^2}$

13. $7k^{-8}h^3 = \frac{7h^3}{k^8}$ 14. $\frac{1}{p^2q^{-4}4^0} = \frac{q^4}{p^2}$ 15. $\left(\frac{2}{5}\right)^{-4} = \left(\frac{5}{2}\right)^4 =$

$\frac{5^4}{2^4} = \frac{625}{16}$ 16. $(-2)^{-3} = \frac{1}{(-2)^3} = \frac{1}{-8} = -\frac{1}{8}$ 17. $-2^{-3} =$

$-(2)^{-3} = -\frac{1}{2^3} = -\frac{1}{8}$ 18. $7^{-2}y^{-4} = \frac{1}{49y^4}$ 19. $\frac{9w^{-4}}{x^{-2}y^7} =$

$\frac{9x^2}{w^4y^7}$ 20. $2^2(-3)^2 = 4 \cdot 9 = 36$ 21. $(-2)^2(-3)^{-2} =$

$\frac{4}{(-3)^2} = \frac{4}{9}$ 22. $2^{-3}(-3)^2 = \frac{9}{2^3} = \frac{9}{8}$ 23. $2^0(-3)^0 = 1$

24. $-2^2(-3)^3 = -4 \cdot -27 = 108$ 25. A. $4^{-3} = \frac{1}{64}$

B. $(-3)^0 = 1$ C. $\frac{1}{(-3)^{-4}} = (-3)^4 = 81$ D. $\frac{4^0}{(-3)^0} = 1$

E. $\frac{0}{4^{-1}(-3)} = 0$; the answer is C. 26. No; $(-3b)^4 = 81b^4$, which (if $b \neq 0$) does not equal $-12b^4$. 27. No; $950 > 10$. 28. No; $72.35 > 10$. 29. yes 30. No; $0.84 < 1$.

31. $2,793,000 = 2.793 \times 10^6$ [mi] 32. $189,000,000 = 1.89 \times 10^8$ [cars and trucks] 33. $2d^2d^3 = 2d^{2+3} = 2d^5$

34. $(q^3r)^4 = q^{3 \cdot 4}r^4 = q^{12}r^4$ 35. $(5c^{-4})(-4m^2c^8) = -20m^2c^{8-4} = -20m^2c^4$ 36. $(1.34^2)^5(1.34)^{-8} = 1.34^{2 \cdot 5} \cdot 1.34^{-8} = 1.34^{10} \cdot 1.34^{-8} = 1.34^2$

$$37. (12x^2y^{-2})^5(4xy^{-3})^{-8} = \left(\frac{12x^2}{y^2}\right)^5 \left(\frac{4x}{y^3}\right)^{-8} =$$

$$\frac{12^5x^{10}}{y^{10}} \cdot \left(\frac{y^3}{4x}\right)^8 = \frac{345x^{10}}{y^{10}} \cdot \frac{y^{24}}{4^8x^8} = \frac{3^5x^2y^{14}}{4^3} = \frac{243x^2y^{14}}{64}$$

$$38. (-2r^{-4})^2(-3r^2z^8)^{-1} = \left(\frac{-2}{r^4}\right)^2 \left(\frac{1}{-3r^2z^8}\right) = \frac{4}{r^8} \cdot \frac{1}{-3r^2z^8} = \frac{4}{3r^{10}z^8}$$

$$39. \left(6.5 \times 10^2 \frac{\text{pores}}{\text{in.}^2}\right) \cdot (0.12 \times 10^2 \text{ in.}^2) =$$

$$(6.5 \cdot 0.12) \times 10^{2+2} \text{ pores} = 0.78 \times 10^4 \text{ pores} = 7.8 \times 10^3 \text{ pores}$$

40. Answers may vary. Sample:
 $(2a^{-2})^{-2}(-3a)^2 = \left(\frac{1}{2a^{-2}}\right)^2 \cdot 9a^2 = \left(\frac{a^2}{2}\right)^2 \cdot 9a^2 = \frac{9a^6}{4}$

41. $\frac{w^2}{w^5} = \frac{1}{w^{5-2}} = \frac{1}{w^3}$ 42. $(8^3) \cdot 8^{-5} = 8^{3+(-5)} = 8^{-2} =$

$\frac{1}{64}$ 43. $\left(\frac{21x^3}{3x}\right) = 7x^{3-1} = 7x^2$ 44. $\left(\frac{n^5}{v^3}\right)^7 = \frac{n^{5 \cdot 7}}{v^{3 \cdot 7}} = \frac{n^{35}}{v^{21}}$

45. $\frac{e^{-6}c^3}{e^5} = \frac{c^3}{e^{5+6}} = \frac{c^3}{e^{11}}$ 46. $\frac{4.2 \times 10^8}{2.1 \times 10^{11}} = \frac{4.2}{2.1} \cdot 10^{8-11} =$

2×10^{-3} 47. $\frac{3.1 \times 10^4}{12.4 \times 10^2} = \frac{1}{4} \cdot 10^{4-2} = \frac{1}{4} \times 10^2 =$

2.5×10^1 48. $\frac{4.5 \times 10^3}{9 \times 10^7} = \frac{1}{2} \cdot 10^{-4} = 5 \times 10^{-5}$

49. $\frac{5.1 \times 10^5}{1.7 \times 10^2} = 3 \times 10^{5-2} = 3 \times 10^3$

50. $\left(\frac{5a^8}{10a^6}\right)^{-3} = \left(\frac{a^{8-6}}{2}\right)^{-3}$ Simplify; div. prop. of exp.

$$= \left(\frac{a^2}{2}\right)^{-3}$$
 Simplify.

$$= \left(\frac{2}{a^2}\right)^3$$
 Raise quotient to neg. power.

$$= \frac{2^3}{(a^2)^3}$$
 Raise quotient to power.

$$= \frac{8}{a^6}$$
 Simplify; raise power to a power.

51. $\frac{75}{750} = 0.1$ 52. $\frac{0.36}{0.12} = 3$ 53. $\frac{-5}{5} = -\frac{1}{2}$ 54. geometric;

$\frac{25}{4}, \frac{25}{16}, \frac{25}{64}$ 55. Neither; differences are 1, 2, 3, 4, and 5; next terms are -30 , -25 , and -19 . 56. arithmetic; 42, 49, 56

57. $f(1) = 3 \cdot 2^1 = 6$; $3 \cdot 2^2 = 3 \cdot 4 = 12$; $3 \cdot 2^3 =$

$3 \cdot 8 = 24$; $3 \cdot 2^4 = 3 \cdot 16 = 48$ 58. $y(1) =$

$10 \cdot (0.75)^1 = 7.5$; $10 \cdot (0.75)^2 = 5.625$; $10 \cdot (0.75)^3 =$

4.21875 59a. Number of tripling periods = $\frac{120}{30} = 4$;

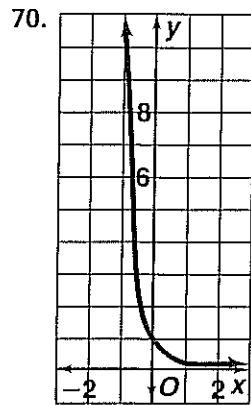
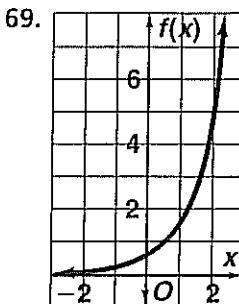
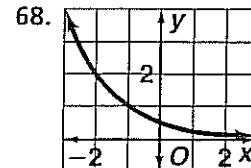
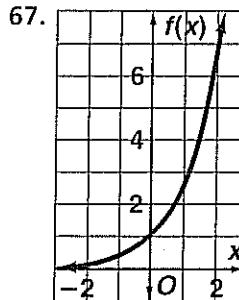
$30 \cdot 3^4 = 2430$ [bacteria] 59b. $\frac{20,000}{30} \approx 667 = 3^x$; $3^5 = 243$; $3^6 = 729$; after about 6 tripling periods or 180 min

60. $y = a \cdot b^x$; $a = 100$, $b = 1.025$ 61. $a = 32$, $b = 0.75$

62. $a = 0.4$, $b = 2$ 63. growth factor = 3 (> 1)

64. growth factor = 1.5 (> 1) 65. decay factor =

0.32 (< 1) 66. decay factor = $\frac{1}{4}$ (< 1)



71. $25 \cdot 0.805 \approx 8.2$ [mg]

CHAPTER TEST

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1. $\frac{r^3t^{-7}}{r^5} = \frac{r^3}{r^{5+7}} = \frac{r^3}{r^{12}} = \frac{1}{r^9}$ 2. $(\frac{a^3}{m})^{-4} = (\frac{m}{a^3})^4 = \frac{m^4}{a^{3 \cdot 4}} = \frac{m^4}{a^{12}}$

3. $\frac{t^{-8}m^2}{m^{-3}} = \frac{m^{2+3}}{t^8} = \frac{m^5}{t^8}$ 4. $c^3v^9c^{-1}c^0 = c^{3-1}v^9 = c^2v^9$

5. $h^2k^{-5}d^3k^2 = h^2d^3k^{-5+2} = h^2d^3k^{-3} = \frac{h^2d^3}{k^3}$

6. $9y^4j^2y^{-9} = 9j^2y^{-5} = \frac{9j^2}{y^5}$ 7. $(w^2k^0p^{-5})^{-7} =$

$$\left(\frac{w^2}{p^5}\right)^{-7} = \left(\frac{p^5}{w^2}\right)^7 = \frac{p^{35}}{w^{14}}$$

8. $2y^{-9}h^2\left(\frac{2}{h^4}\right)^{-6} = 2y^{-9}h^2\left(\frac{h^4}{2}\right)^6 = 2y^{-9}h^2\left(\frac{h^{24}}{64}\right) = \frac{h^{26}}{32y^9}$

9. $(1.2)^5(1.2)^{-2} = (1.2)^{5-2} = (1.2)^3 = 1.728$

10. $(-3q^{-1})^3q^2 = \left(\frac{-3}{q}\right)^3q^2 = \left(\frac{-27}{q^3}\right)q^2 = \frac{-27}{q}$

11. A. $(-3)^2(-3)^0 = 9$ B. $(-3)^{-3} = \left(\frac{1}{-3}\right)^3 = -\frac{1}{27}$

C. $(-3)^8(-3)^{-5} = (-3)^3 = -27$ D. $-(-3)^{-3}(-3)^{-4} = -(-3)^{-7} = -\left(\frac{1}{-3}\right)^7 = \frac{1}{2187}$; the answer is C.

12. $44,909,000 = 4.4909 \times 10^7$ [votes] 13. $450,000 =$

4.5×10^5 14. No; $76 > 10$. 15. yes 16. No; there

are two powers of 10. 17. No; $32.5 > 10$.

18a. $(1.863 \times 10^5 \frac{\text{mi}}{\text{s}})\left(\frac{3600 \text{s}}{1 \text{h}}\right) = 6.7068 \times 10^8 \frac{\text{mi}}{\text{h}}$; about

6.7068×10^8 mi 18b. time = $\frac{\text{distance}}{\text{rate}} = \frac{1.03 \times 10^9 \text{ mi}}{6.7068 \times 10^8 \frac{\text{mi}}{\text{h}}} \approx$

1.5 h 19a. $\frac{-8}{16} = -\frac{1}{2}$ 19b. $-2, 1, -\frac{1}{2}$ 19c. $A(n) =$

$-32\left(-\frac{1}{2}\right)^{n-1}$ 19d. $A(9) = -32\left(-\frac{1}{2}\right)^{9-1} =$

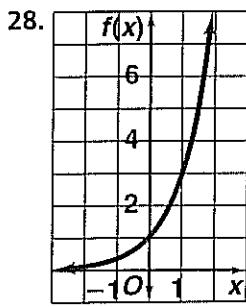
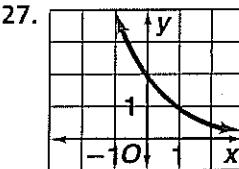
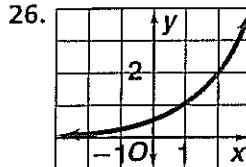
$-32\left(-\frac{1}{2}\right)^8 = -2^5\left(\frac{1}{2^8}\right) = -\frac{1}{2^3} = -\frac{1}{8}$ 20a. Height of

$(n-1)$ th bounce = $A(n) = 12 \cdot \left(\frac{3}{5}\right)^{n-1}$ 20b. after

third bounce ($n = 4$), $A(4) = 12 \cdot \left(\frac{3}{5}\right)^{4-1} = 12 \cdot (0.6)^3 =$

2.592 [ft] 21. $A(5) = -3(-2)^{5+1} = -3(-2)^6 = -3 \cdot 64 = -192$ 22. $y(1) = 3 \cdot 5^1 = 15; 3 \cdot 5^2 = 75; 3 \cdot 5^3 = 375$

23. $\frac{1}{2} \cdot 4^1 = 2; \frac{1}{2} \cdot 4^2 = 8; \frac{1}{2} \cdot 4^3 = 32$ 24. $4(0.95)^1 = 3.8; 4(0.95)^2 = 3.61; 4(0.95)^3 = 3.4295$ 25. $g(1) = 5(0.75)^1 = 3.75; 5(0.75)^2 = 2.8125; 5(0.75)^3 = 2.109375$



29. Answers may vary. Sample:
A computer loses 20% of its value each year. How much will a \$3000 computer be worth in 3 years? \$1792 30. growth for $b > 1$; decay for $0 < b < 1$
31. $1000 \cdot 1.01^8 = 1082.86$ [\$]; $1000 \cdot 1.01^{20} = 1220.19$ [\$]
32a. growth; growth factor $1.07 > 1$ 32b. $1.3 \cdot (1.07)^{25} \approx 7.1$

[kWh] 32c. $1.3 \cdot (1.07)^{-10} \approx 0.66$ [kWh]

32d.

Year	x	$1.3 \cdot (1.07)^x$ (kWh)
2002	17	4.1
2003	18	4.4
2004	19	4.7
2005	20	5.0
2006	21	5.4

33a. 0.85; the car's value depreciates 15% annually.

33b. $20,000(0.85)^1 = 17,000$ [\$] 33c. $20,000(0.85)^4 = 10,440$ [\$] 34a. 8% 34b. \$10,000; $10 \cdot 1.08^3 = 12.59712$; \$12,597.12

34c.

Year	x	$\$10,000 \cdot 1.08^x$
2003	6	\$15,869
2004	7	\$17,138
2005	8	\$18,509
2006	9	\$19,990
2007	10	\$21,589

STANDARDIZED TEST PREP

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1. The answer is C.

2. mean = $\frac{88 + 78 + 81 + 83 + 90 + x}{6} = 85$
 $420 + x = 6 \cdot 85 = 510$
 $x = 510 - 420$
 $x = 90$

The answer is F.

3. $5 - 6x < -x + 2$
 $5 - 5x < 2$
 $-5x < -3$
 $x > \frac{3}{5} = 0.6$

The answer is A.

4. Commision on \$500 is \$30, so sales were greater than \$500.

$$30 + 0.1(x - 500) = 130$$

$$0.1(x - 500) = 100$$

$$x - 500 = 1000$$

$$x = 1500$$

The answer is I.

5.

$$\begin{array}{rcl} \frac{1}{3}x - y & = & 4 \\ x - 3y & = & 12 \\ x + 3y & = & 0 \\ \hline 2x & = & 12 \\ x & = & 6 \\ 6 + 3y & = & 0 \\ 3y & = & -6 \\ y & = & -2 \end{array}$$

The answer is C.

6. $P(\text{head, 3 or 6}) = \frac{1}{2} \cdot \frac{2}{6} = \frac{1}{6}$; answer is G.

7. The answer is D. $8. \frac{75h}{12.5h} = 6$; the answer is F.

9. $-3a^8cb^{-3}b^{12} \cdot 9c^5 = -27a^8b^{12-3}c^{1+5} = -27a^8b^9c^6$; the answer is B.

10. (1) $y > x + 4$
 $y > -x + 4$

The solutions of the system lie above both lines. Since the lines intersect at (0, 4), every solution satisfies $y > 4$. The answer is I.

11. The answer is A.

12. $1 + y = 9$
 $x + 3 = 6$
 $y = 8$
 $x = 3$

The answer is B.

13. $0.21 \cdot 9 = 1.89$ 14. $P = \frac{3}{6} = \frac{1}{2}$ 15. [2] x: 2000;
 $y: 1990; x = (1 + 0.132)y; y = \frac{x}{1.132} = \frac{281,421,906}{1.132} = 248,605,924$ [people]; [1] no work shown

16. $x - 2 \leq 9$ and $x - 2 \geq -9$
 $x \leq 11$ and $x \geq -7$
 $-7 \leq x \leq 11$

[2] $|x - 2| \leq 9$ [1] no work shown

17. [4] Yes; rectangles have opposite sides that are parallel and adjacent sides that are perpendicular, so 2 slopes must be equal and the remaining 2 slopes must be their negative reciprocals. [3] yes, with an explanation that neglects to mention either parallel or perpendicular [2] yes, with a vague explanation [1] yes, with no explanation