Display each set of data in a frequency table.

1. 5146264513264546

Number				
Frequency		\ <u></u>		

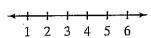
**2.** 43121331321

Number		•	
Frequency			

Draw a line plot and histogram for each frequency table. Find the range.

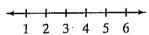
3. Number 1 2 3 4 5 6 Frequency 2 0 4 1 2 4

range:



4. Number 1 2 3 4 5 6 Frequency 4 4 0 0 3 2

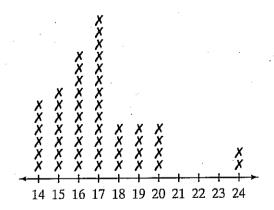
range:



Construct a frequency table from the line plot.

5.

State Average Pupils per Teacher



Pupils per Teacher						
Frequency						

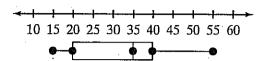
**6.** What is the range in pupil-teacher ratios?

Pre-Algebra Chapter 12

**Box-and-Whisker Plots** 

Use the box-and-whisker plot to answer each question.

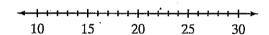
Weekly Mileage Totals, 24 Runners



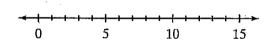
- 1. What is the highest weekly total? the lowest?
- **2.** What is the median weekly total?
- 3. What percent of runners run less than 40 miles a week?
- 4. How many runners run less than 20 miles a week?

Make a box-and-whisker plot for each set of data.

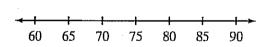
**5.** 16 20 30 15 23 11 15 21 30 29 13 16



**6.** 9 12 10 3 2 3 9 11 5 1 10 4 7 12 3 10



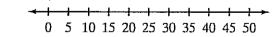
**7.** 70 77 67 65 79 82 70 68 75 73 69 66 70 73 89 72



Use box-and-whisker plots to compare data sets. Use a single number line for each comparison.

**8.** 1st set:

7 12 25 3 1 29 30 7 15 2 5 10 29 1 10 30 18 8 7 29



2nd set: 37 17 14 43 27 19 32 1 8 48

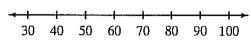
1st Set

26 16 28 6 25 18

2<sup>nd</sup> Set

**9.** Area in 1,000 mi<sup>2</sup>

Midwestern states:



45 36 58 97 56 65 87 82 77

Midwestern States

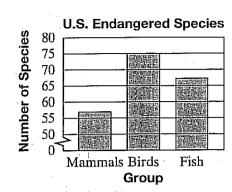
Southern states:

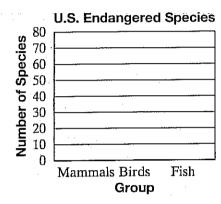
Southern

52 59 48 52 42 32 54 43 70 53 66

Use the graph at the right for Exercises 1-5.

- 1. Which group of animals appears to have more than twice as many endangered species as mammals?
- 2. Does one group actually have twice as many endangered species as mammals?
- 3. What gives the impression that one group has twice as many endangered species as mammals?
- 4. Redraw the graph without a break.
- 5. Describe the effect the change in scale has on what the graph suggests.

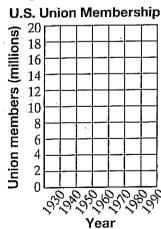




### Use the data in the table for Exercises 6-8.

U.S. U	nion N	1embe	ership				
Year	1930	1940	1950	1960	1970	1980	1990
Union members (millions)	3	9	14	17	19	20	17

**6.** Draw a line graph of the data using the grid below.



7. Draw a line graph of the data using the grid below.



8. What gives the different impressions in the two graphs?

**Counting Outcomes and Theoretical Probability** 

A computer store sells 4 models of a computer (m1, m2, m3, and m4). Each model can be fitted with 3 sizes of hard drive (A, B, and C).

- 1. Find the sample space.
- **2.** What is the probability of choosing a computer with a size C hard drive at random?
- **3.** What is the probability of choosing a model 2 computer with a size A hard drive at random?

### Solve each problem by drawing a tree diagram.

- 4. A ballot offered 3 choices for president (A, B, C) and 2 choices for vice president (M, N). How many choices for a combination of the two offices did it offer? List them.
- 5. The Cougar baseball team has 4 pitchers (P1, P2, P3, P4) and 2 catchers (C1, C2). How many pitcher-catcher combinations are possible? List them.

### Solve each problem by using the counting principle.

- **6.** There are 5 roads from Allen to Baker, 7 roads from Baker to Carlson, and 4 roads from Carlson to Dodge. How many different routes from Allen to Dodge by way of Baker and Carlson are possible?
- 7. Drapery is sold in 4 different fabrics. Each fabric comes in 13 different patterns. Each pattern is offered in 9 different colors. How many fabric-pattern-color combinations are there?

Name	Class	Date				
Practice 12-5	Independent and Dependent Events					
A shelf holds 3 novels, 2 biographies, and turn choose a book at random. What is th choose each of the following?	1 history boo e probability	ok. Two students in that the students				
1. both novels	<b>2.</b> both l	piographies				
3. a history, then a novel	<b>4.</b> both l	nistory books				
Meg flipped a penny the given number of the results were as follows?	times. What	is the probability				
<b>5.</b> 2; two heads	<b>6.</b> 3; thre	ee tails.				
7. 2; a tail, then a head	<b>8.</b> 5; five	tails				
Two puppies are chosen at random from a mall. What is the probability of these outcomes the probability of these outcomes.	a box at the comes?	Free Puppies for Adoption!  5 black retrievers 3 brown hounds 4 black setters				
	<b>11</b> a setti	er, then a hound				
<ul><li>10. both brown</li><li>12. a retriever, then a setter</li></ul>						
Are the events independent or dependent	t? Explain.					
<b>14.</b> A guest at a party takes a sandwich from takes a sandwich.	om a tray. A se	cond guest then				
	-					
15. Sam flips a coin and gets heads. He flip	os again and g	ets tails.				
You can select only two cards from the rig probability of selecting a T and an N for e		MATH				
16. You replace the first card before drawi	ing the second	FUN				
17. You do not replace the first card before	e drawing the	second.				

Permutations and Combinations

Simplify each expression.

- **1.**  $_{7}P_{2}$  \_\_\_\_\_

- **4.** <sub>9</sub>P<sub>4</sub> \_\_\_\_\_ **5.** <sub>3</sub>C<sub>2</sub> \_\_\_\_\_
- **6.** <sub>10</sub>C<sub>4</sub>
- 7. Art, Becky, Carl, and Denise are lined up to buy tickets.
  - a. How many different permutations of the four are possible?
  - **b.** Suppose Ed was also in line. How many permutations would there be?
  - c. In how many of the permutations of the five is Becky first?
  - **d.** What is the probability that a permutation of this five chosen at random will have Becky first?
- 8. Art, Becky, Carl, Denise, and Ed all want to go to the concert. However, there are only 3 tickets. How many ways can they choose the 3 who get to go to the concert?
- 9. A combination lock has 36 numbers on it. How many different 3number combinations are possible if no number may be repeated?

Numbers are to be formed using the digits 1, 2, 3, 4, 5, and 6. No digit may be repeated.

- **10.** How many two-digit numbers can be formed?
- 11. How many three-digit numbers can be formed?
- **12.** How many four-digit numbers can be formed?
- **13.** How many five-digit numbers can be formed?
- **14.** How many six-digit numbers can be formed?

**Experimental Probability** 

Color

red

white

orange

blue

Number

of shirts

6

4

2

The table shows the colors of Rahmi's soccer shirts. For each color, find the experimental probability that a random shirt from Rahmi's collection is that color. Write the probability as a percent, to the nearest tenth of a percent.

- **1.** red
- 2. white
- 3. orange 4. blue
- **5.** red or blue \_\_\_\_\_ **6.** not white \_\_\_\_\_
- 7. not orange or red \_\_\_\_\_\_ **8.** green

Your school's basketball team has an equal chance of winning or losing the first three games of the season. You simulate the probability by tossing a coin 60 times, letting heads stand for a win and tails stand for a loss. Use the data below. Find each experimental probability as a percent.

HHH THH THT TTH THH HTH THH THH HTH HHH THH TTH THH HTT TTT HTT HHT TTH HTH THH

**9.** *P*(win all 3)

- **10.** *P*(win exactly 2)
- **11.** *P*(win exactly 1) \_\_\_\_\_
- **12.** *P*(win none) \_\_\_\_\_
- **13.** *P*(win at least 2)
- **14.** P(win at least 1) '\_\_\_\_\_
- **15.** *P*(win less than 2)

Students were surveyed about the number of children living in their household. The table shows the results. Write each experimental probability as a fraction in simplest form.

- **16.** *P*(one child) \_\_\_\_\_\_
- **17.** *P*(2 or more children) \_\_\_\_\_\_
- **18.** *P*(at least 3 children) \_\_\_\_\_\_

Number	Number
of children	of students
0	0
1	11
2	. 15
3	3
4 or more	4

**Random Samples and Surveys** 

A school has 800 students. Two random surveys are conducted to determine students' favorite sport. Use the data in the table to estimate the total number of students who prefer each sport.

	S	port Sample	es			
C1-	Number	Favorite sport				
Sample	Sampled	Basketball	Football	Baseball		
A	40	16	14	10		
В	50	· 22	16	12		

- 1. basketball based on Sample A
- 2. basketball based on Sample B
- 3. baseball based on Sample A
- 4. baseball based on Sample B

You want to find out if a school bond issue for a new computer center is likely to pass in the next election. State whether each survey plan describes a good sample. Explain your reasoning.

- 5. You interview people coming out of a computer store in your town.
- **6.** You choose people to interview at random from the city telephone book.

7. You interview every tenth person leaving each voting place in your school district.

#### Simulate a Problem

## Solve by simulating the problem.

- 1. Twenty people seated in a circle counted to seven, beginning with the number one. The seventh person dropped out and those remaining counted to seven again. If every seventh person dropped out, what was the number of the last person remaining in the circle? Use the number circle to simulate the problem.
- Start

  20 1 2

  19 1 7 3

  18 4

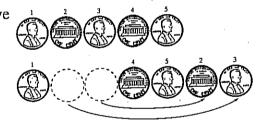
  17 -5

  16 -6

  15 7

  14 9 Out

  13 12 11 10
- 2. The Rockets played their first volleyball game on Friday, October 18, and played a game every Friday thereafter.
  - a. What was the date of their ninth game?
  - **b.** What was the number of the game they played on February 7?
- 3. Five coins are placed side by side as shown. A move consists of sliding two adjacent coins to an open spot without changing the order of the two coins. (The move "2-3 right" is illustrated.) Find three successive moves that will leave the coins in this order: 3-1-5-2-4



4. An irresponsible TV weatherperson forecasts the weather by throwing a number cube and consulting the weather key shown here. The weather during one 5-day stretch is given in the table. What is the probability that the forecaster was right at least 3 days out of 5? Use a number cube to simulate the forecaster's predictions. A successful trial occurs when you roll the correct weather three or more times out of five.

Mon	Tue	Wed	Thu	Fri
continual rain	continual rain	clear and cool	cloudy and cool	snow

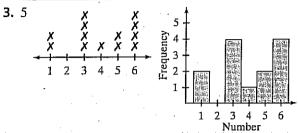
Weather Key
1–clear and warm
2-clear and cool
3-cloudy and cool
4-intermittent showers
5–continual rain
6–snow

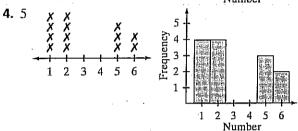
Work with a partner. Carry out 50 trials. Write the probability after the given number of trials.

- **a.** 10 \_\_\_\_\_
- **b.** 30 \_\_\_\_\_
- **c.** 50

1.	Number	1	2	3	4	5	6
	Frequency	2	2	1	4	3.	4

2.	Number	1	2	3	4
	Frequency	4	2	4	1





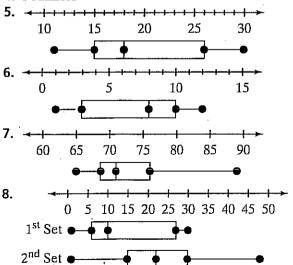
5	1			
Pupils per   14   15   16   17   18	19	18	20	21
Frequency   6   7   10   13   4	4	4	4	0

22	23	24
0	0	2

6. 10 pupils per teacher

### Practice 12-2

- 1. 55 miles, 15 miles 2. 35 miles 3. 75%
- 4. 6 runners

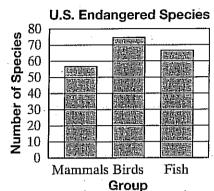


9. 30 40 50 60 70 80 90 100 Midwestern States

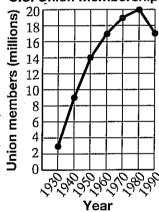
Southern States

### Practice 12-3

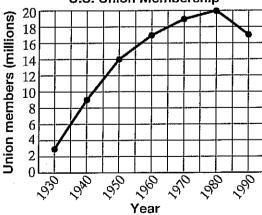
1. birds 2. no 3. the break in the vertical axis



- 5. The differences seem much less.
- 6. U.S. Union Membership



7. U.S. Union Membership



8. The horizontal scales are different.

# Chapter 12 Answers (continued)

### Practice 12-4

1. m1A, m1B, m1C, m2A, m2B, m2C, m3A, m3B, m3C, m4A, m4B, m4C 2.  $\frac{1}{3}$  3.  $\frac{1}{12}$  4. 6 choices; AM, AN, BM, BN, CM, CN 5. 8 combinations; P1C1, P1C2, P2C1, P2C2, P3C1, P3C2, P4C1, P4C2 6. 140 routes 7. 468 combinations

#### Practice 12-5

1.  $\frac{1}{5}$  2.  $\frac{1}{15}$  3.  $\frac{1}{10}$  4. 0 5.  $\frac{1}{4}$  6.  $\frac{1}{8}$  7.  $\frac{1}{4}$  8.  $\frac{1}{32}$  9.  $\frac{6}{11}$  10.  $\frac{1}{22}$  11.  $\frac{1}{11}$  12.  $\frac{5}{33}$  13.  $\frac{1}{11}$ 

14. Dependent; the second guest's choice is limited by the first guest's choice. 15. Independent; the second flip is not affected by the first. 16.  $\frac{1}{81}$  17.  $\frac{1}{72}$ 

### Practice 12-6

**1.** 42 **2.** 21 **3.** 336 **4.** 3,024 **5.** 3 **6.** 210 **7.a.** 24 **b.** 120 **c.** 24 **d.**  $\frac{1}{5}$  **8.** 10 **9.** 42,840 **10.** 30 **11.** 120 **12.** 360 **13.** 720 **14.** 720

### Practice 12-7

1. 40% 2. 26.7% 3. 20% 4. 13.3% 5. 53.3% 6. 73.3% 7. 40% 8. 0% 9. 10% 10. 55% 11. 30% 12. 5% 13. 65% 14. 95% 15. 35% 16.  $\frac{1}{3}$  17.  $\frac{2}{3}$  18.  $\frac{7}{33}$ 

### Practice 12-8

1. 320 students 2. 352 students 3. 200 students 4. 192 students 5. The views of people coming out of a computer store may not represent the views of other voters. This is not a good sample because it is not random. 6. The city telephone book may cover more than one school district. It would also include people who do not vote. This is not a good sample because it does not represent the population. 7. This is a good sample. It is selected at random from the population you want to study.

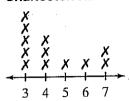
#### Practice 12-9

**1.** 3 **2.a.** December 13 **b.** 17 **3.** Sample answer is shown. 1-2 right, 4-5 right, 2-4 right **4.** Sample answers are shown. **a.**  $\frac{1}{10}$  **b.**  $\frac{1}{15}$  **c.**  $\frac{1}{25}$ 

### Reteaching 12-1

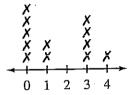
1.	Inches	3	4	5	6	7
	Frequency	5 .	3	1	1	2

#### **Charleston Rainfall**



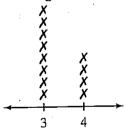
2.	Inches	0	1	2	3	4
	Frequency	5	-2	0	. 4	1

#### San Francisco Rainfall



3.	Inches	3	4
	Frequency	8	4

#### Wilmington Rainfall



### Reteaching 12-2

